

**Mother's Advance Maths • Algebra [Previous Year Questions]**

11. (B)  $\frac{y^3 - x^3 - z^3}{2xyz}$

$$x + z = y \\ \text{put } \Rightarrow 1 + 1 = 2$$

$$\frac{8-1-1}{2 \times 2 \times 1 \times 1} \Rightarrow \frac{6}{4} \Rightarrow \frac{3}{2}$$

**Method - II**

$$x - y + z = 0$$

$$\text{So, } x^3 - y^3 + z^3 = -3xyz$$

$$\frac{-(x^3 - y^3 + z^3)}{2xyz} = \frac{-(-3xyz)}{2xyz} = \frac{3}{2}$$

12. (A)  $5 - x - 5 + x - \left( \frac{20-x}{200} \right) = 0.08$

$$\Rightarrow \frac{x-20}{200} = 0.08 \Rightarrow x-20 = 16 \Rightarrow x = 36$$

13. (C)  $a^3 + b^3 + c^3 - 3abc$

$$= (a+b+c)(a^2 + b^2 + c^2 - ab - bc - ac)$$

$$(a+b+c)^2 = a^2 + b^2 + c^2 + 2(ab + bc + ac)$$

So,

$$(18)^2 = x^2 + y^2 + z^2 + 2(90) \Rightarrow x^2 + y^2 + z^2 = 324 - 180 \Rightarrow 144$$

$$x^3 + y^3 + z^3 - 3(81) = 18(144 - 90)$$

$$\Rightarrow x^3 + y^3 + z^3 = 18(54) + 3(81)$$

$$\Rightarrow x^3 + y^3 + z^3 = 9(108) + 9(27) \Rightarrow x^3 + y^3 + z^3 = 9(135)$$

$$\Rightarrow x^3 + y^3 + z^3 + xyz = 9(135) + 81$$

$$\Rightarrow 9(135) + 9(9) \Rightarrow 9(144) \Rightarrow 144(10-1) = 1440 - 144 \Rightarrow 1296$$

14. (A)  $x^3 + y^3 + z^3 - 3xyz$

$$= (x+y+z)(x^2 + y^2 + z^2 - xy - yz - zx)$$

$$(a+b+c)^2 = a^2 + b^2 + c^2 + 2(ab + bc + ac)$$

$$(18)^2 = x^2 + y^2 + z^2 + 2(90) \Rightarrow x^2 + y^2 + z^2 = 144$$

$$x^3 + y^3 + z^3 - 243 = 18(144 - 90) \Rightarrow x^3 + y^3 + z^3 = 18 \times 54 + 243$$

$$\Rightarrow x^3 + y^3 + z^3 = 9 \times 108 + 9 \times 27 \Rightarrow x^3 + y^3 + z^3 = 9 \times 135 \Rightarrow 1215$$

$$\sqrt[4]{x^3 + y^3 + z^3 + xyz} \Rightarrow \sqrt[4]{1215 + 81} \Rightarrow$$

$$\sqrt[4]{1296} \Rightarrow \sqrt[4]{6 \times 6 \times 6 \times 6} \Rightarrow 6$$

15. (D)  $x^3 - y^3 = (x-y)(x^2 + y^2 + xy)$

$$(\sqrt{2}x)^3 - (\sqrt{3}y)^3 = (\sqrt{2}x - \sqrt{3}y)(2x^2 + 3y^2 + \sqrt{6}xy)$$

$$2x^2 + 3y^2 + \sqrt{6}xy = Ax^2 + Cy^2 - Bxy \Rightarrow A = 2,$$

$$B = -\sqrt{6}, C = 3$$

$$A^2 + B^2 + C^2 = (2)^2 + (-\sqrt{6})^2 + (3)^2 \Rightarrow 4 + 6 + 9 = 19$$

16. (B)  $x^3 + y^3 + z^3 - 3xyz = (x+y+z)(x^2 + y^2 + z^2 - (xy + yz + zx))$

$$(x+y+z)^2 = x^2 + y^2 + z^2 + 2(xy + yz + zx)$$

$$(x+y+z)^2 = x^2 + y^2 + z^2 + 2(-11) \Rightarrow x^2 + y^2 + z^2 = 26$$

$$x^3 + y^3 + z^3 - 3(-12) = 2(26 - (-11)) \Rightarrow x^3 + y^3 + z^3 = 74 - 36$$

$$\Rightarrow x^3 + y^3 + z^3 = 38$$

17. (D)  $x^2 + \frac{1}{x^2} = 23$

$$x + \frac{1}{x} = \sqrt{23+2} = 5$$

$$x^3 + \frac{1}{x^3} = a^3 - 3a$$

$$125 - 15 = 110$$

18. (C)  $(a+b-c)^2 \Rightarrow a^2 + b^2 + c^2 + 2ab - 2bc - 2ca = 25$

$$a^2 + b^2 + c^2 \Rightarrow 25 - 20 \Rightarrow 5$$

19. (A)  $(a+1)^2 + (b-1) + (7c+4)^2 = 0$

$$a = -1, b = 1, 7c = -4$$

$$-1-1+4 = 2$$

20. (C)  $2\sqrt{2}x^3 - 3\sqrt{3}y^3$

$$= (\sqrt{2}x - \sqrt{3}y)(Ax^2 - Bxy + cy^2)$$

$$A = 2, B = 3, C = \sqrt{6}$$

$$\sqrt{a^2 + B^2 + c^2}$$

$$\sqrt{4+9+6} \Rightarrow \sqrt{19}$$

21. (B)  $\sqrt{x} - \frac{1}{\sqrt{x}} = \sqrt{3}$

$$x + \frac{1}{x} = (\sqrt{3})^2 + 2 \Rightarrow 5$$

$$x^2 + \frac{1}{x^2} = 23$$

$$x^4 + \frac{1}{x^4} = 529 - 2 \Rightarrow 527$$

22. (D)  $(x+y+z)[(x+y+z)^2 - 3(xy + yz + zx)]$

$$(7)(49 - 3(18)) = 7 \times 25 = 175$$

23. (D)  $(a+b)^3 \Rightarrow a^3 + b^3 + 3ab(a+b)$

$$8 = 218 + 3ab(2)$$

$$-210 = 6ab$$

$$-35 = ab$$

$$\sqrt{1-ab} \quad \sqrt{1+35} \Rightarrow 6$$

24. (D)  $a^2 + b^2 + 49c^2 + 18 = 2b + 56c - 2a$

$$\Rightarrow a^2 + 2a + b^2 - 2b + 49c^2 - 56c + 18 = 0$$

$$a^2 + 2a + 1 + b^2 - 2ab + 1 + 49c^2 - 56c + 16 = 0$$

$$\Rightarrow (a-1)^2 + (b-1)^2 + 7(-4)^2 = 0$$

So,

$$a+1=0, b-1=0, 7c-4=0, a=1, b=1, c=\frac{4}{7}$$

$$2(-1)-(1)+7\left(\frac{4}{7}\right) \Rightarrow -2-1+4 \Rightarrow -3+4=1$$

25. (D)  $x - \frac{1}{x} = 5$

So,

$$x^3 - \frac{1}{x^3} = (5)^3 + 3(5) \Rightarrow 140$$

$$x^3 - \frac{1}{x^3} + \frac{1}{x} - x \Rightarrow x^3 - \frac{1}{x^3} - \left(x - \frac{1}{x}\right) \\ = 140 - 5 = 135$$

26. (C) put  $x=y=1$

$$\Rightarrow 8 - 3(2-3) = k \\ \Rightarrow k = 11$$

27. (B)  $a+b+c=11, ab+bc+ca=28$

$$a^2+b^2+c^2-3abc \\ = (a+b+c)[(a+b+c)^2-3(ab+bc+ca)] \\ = 11(121-3 \times 28) \\ = 11 \times (121-84) = 407$$

28. (C)  $0.4 x + \frac{1}{x} = 5$

$$\Rightarrow 0.064x^3 + \frac{1}{x^3} = 5^3 - 3 \times 0.4 \times 5 \\ = 125 - 6 \\ = 119$$

29. (C)  $x^2 + \frac{1}{x^2} = 18$

Now,  $x + \frac{1}{x} = \sqrt{20}$

and  $x^3 + \frac{1}{x^3} = 20\sqrt{20} - 3\sqrt{20} \\ = 17\sqrt{20} \\ = 34\sqrt{5}$

30. (D)  $\sqrt{x} - \frac{1}{\sqrt{x}} = \sqrt{5}$

$$x + \frac{1}{x} = 7$$

$$\Rightarrow \frac{\frac{1}{x}\left(x^4 + \frac{1}{x^2}\right)}{\frac{1}{x}(x^2 + 1)} = \frac{x^3 + \frac{1}{x^3}}{x + \frac{1}{x}}$$

$$= \frac{343 - 7 \times 3}{7} = \frac{322}{7} = 46$$

31. (B)  $6\sqrt{6} p^3 + 2\sqrt{2} q^3 = (\sqrt{6} \times P + \sqrt{2} q)(sp^2 + mq^2 - Npq)$

$$\Rightarrow 6p^2 + 2q^2 - 2\sqrt{3} pq = Sp^2 + mq^2 - Npq$$

by comparision

$$S = 6, M = 2, N = 2\sqrt{3}$$

$$\therefore \sqrt{s^2 + m^2 + 2n^2} = \sqrt{36 + 4 + 2(2\sqrt{3})^2} \\ = \sqrt{40 + 24} \\ = \sqrt{64} = 8$$

32. (A)  $5x - \frac{1}{4x} = 6 \Rightarrow 25x^2 + \frac{1}{16x^2} - 2\left(\frac{5}{4}\right) = 36$

$$\Rightarrow 25x^2 + \frac{1}{16x^2} + \frac{5}{2} = 36 + 5 \Rightarrow 5x + \frac{1}{4x} = \sqrt{41} \\ = 25x^2 - \frac{1}{16x^2} = 6\sqrt{41}$$

33. (D)  $(a+b)^2 = a^2 + b^2 + 2ab$

$$(a+b)^2 = 65+16 \Rightarrow a+b = \pm 9$$

$\therefore a > b > 0$  so  $a = 8, b = 1$

$$a^2 - b^2 = 64 - 1 = 63$$

34. (A)  $x^2 + \frac{1}{x^2} = 79 \left(x + \frac{1}{x}\right)^2 = 81$

$$\Rightarrow x + \frac{1}{x} = 9$$

35. (A)  $4x - 3y = 12, 16x^2 + 9y^2 - 24xy = 144$

$$\Rightarrow \frac{16x^2 + 9y^2 - 24xy}{8} = \frac{144}{8}$$

$$\Rightarrow \frac{16x^2 + 9y^2}{8} - 3xy = 18$$

$$\Rightarrow \frac{16x^2 + 9y^2}{8} = 18 + 15 \Rightarrow \frac{16x^2 + 9y^2}{8} = 33$$

36. (B)  $a + \frac{1}{a} + 3 = 4 \Rightarrow a + \frac{1}{a} = +1, a + \frac{1}{a} = -7$

$$a^2 + \frac{1}{a^2} = (+1)^2 - 2, (-7)^2 - 2$$

$$\Rightarrow 1 - 2, 49 - 2 \Rightarrow -1, 47$$

# **ALGEBRA**

(SSC CGL (PRE) - 2020)

## बीजगणित

### **(Previous Year Questions)**

Mother's एण्डवांस • बीजगणित

**Mother's Advance Maths • Algebra [Previous Year Questions]**

- 24.** If  $x^8 - 433x^4 + 16 = 0$ ,  $x > 0$ , then what is the value of  $x + \frac{2}{x}$  ?  
 यदि  $x^8 - 433x^4 + 16 = 0$ ,  $x > 0$  है, तो  $x + \frac{2}{x}$  का मान ज्ञात कीजिए ?  
 (A) 7 (B) 4  
 (C) 5 (D) 9
- 25.** If  $4x^4 = 5x^2 - 1$ ,  $x > \frac{1}{\sqrt{2}}$ , then what is the value of  $(2x^2 - x - 1)$ ?  
 यदि  $4x^4 = 5x^2 - 1$ ,  $x > \frac{1}{\sqrt{2}}$  है, तो  $(2x^2 - x - 1)$  का मान ज्ञात कीजिए ?  
 (A) 1 (B) -2  
 (C) 0 (D) 2
- 26.** If  $x^2 + 9y^2 + 4z^2 = 12(x - 2y + 2z) - 88$ , then the value of  $(x - 3y + z)$  is:  
 यदि  $x^2 + 9y^2 + 4z^2 = 12(x - 2y + 2z) - 88$  है, तो  $(x - 3y + z)$  का मान ज्ञात कीजिए ?  
 (A) 11 (B) 13  
 (C) 10 (D) 5
- 27.** If  $x^4 + y^4 + x^2y^2 = 21$  and  $x^2 + y^2 - xy = 7$ , then what is the value of  $\frac{x}{y} + \frac{y}{x}$ ?  
 यदि  $x^4 + y^4 + x^2y^2 = 21$  और  $x^2 + y^2 - xy = 7$  है, तो  $\frac{x}{y} + \frac{y}{x}$  का मान ज्ञात कीजिए ?  
 (A)  $\frac{5}{4}$  (B)  $\frac{3}{4}$  (C)  $-\frac{3}{2}$  (D)  $-\frac{5}{2}$
- 28.** If  $x + y = 3$  and  $\frac{1}{x} + \frac{1}{y} = \frac{3}{10}$ , then the value of  $x^2 + y^2$  is:  
 यदि  $x + y = 3$  और  $\frac{1}{x} + \frac{1}{y} = \frac{3}{10}$  है, तो  $x^2 + y^2$  का मान ज्ञात कीजिए ?  
 (A) 29 (B) 28  
 (C) 26 (D) 34
- 29.** If  $x + y + z = 1$  and  $xy + yz + zx = xyz = -4$ , then what is the value of  $x^3 + y^3 + z^3$ ?  
 यदि  $x + y + z = 1$  और  $xy + yz + zx = -4$  है, तो  $x^3 + y^3 + z^3$  का मान ज्ञात कीजिए ?  
 (A) 8 (B) -8  
 (C) 1 (D) -1
- 30.** What is the constant term in the expansion of  $\left(5x^2 - \frac{1}{x}\right)^3$ ?  
 $\left(5x^2 - \frac{1}{x}\right)^3$  के विस्तार में अचर पद क्या है ?  
 (A) 15 (B) 5  
 (C) 75 (D) -15
- 31.** If  $x^2 - 5\sqrt{2}x + 1 = 0$ , then what is the value of  $\frac{x^3 + \frac{1}{x}}{x^2 + 1}$ ?  
 यदि  $x^2 - 5\sqrt{2}x + 1 = 0$  है, तो  $\frac{x^3 + \frac{1}{x}}{x^2 + 1}$  का मान ज्ञात कीजिए ?  
 (A)  $\frac{24\sqrt{2}}{5}$  (B)  $\frac{12\sqrt{2}}{5}$   
 (C)  $\frac{18\sqrt{2}}{5}$  (D)  $\frac{26\sqrt{2}}{5}$
- 32.** If  $a + b + c = 0$ , then what is the value of  $\frac{(a+b)^2}{ab} + \frac{(b+c)^2}{bc} + \frac{(c+a)^2}{ca}$ ?  
 यदि  $a + b + c = 0$  है, तो  $\frac{(a+b)^2}{ab} + \frac{(b+c)^2}{bc} + \frac{(c+a)^2}{ca}$  का मान ज्ञात कीजिए ?  
 (A) 1 (B) -3  
 (C) -1 (D) 3
- 33.** If  $x - \frac{1}{x} = \sqrt{77}$ , then one of the values of  $x^3 + \frac{1}{x^3}$  is:  
 यदि  $x - \frac{1}{x} = \sqrt{77}$  है, तो  $x^3 + \frac{1}{x^3}$  का मान ज्ञात कीजिए ?  
 (A)  $80\sqrt{77}$  (B) -702  
 (C)  $77\sqrt{77}$  (D)  $3\sqrt{77}$
- 34.** If  $a^3 - b^3 = 2349$  and  $a - b = 9$ , then  $(a + b)^2 - ab$  is equal to:  
 यदि  $a^3 - b^3 = 2349$  और  $a - b = 9$  है, तो  $(a + b)^2 - ab$  का मान ज्ञात कीजिए ?  
 (A) 280 (B) 244  
 (C) 261 (D) 229
- 35.** If  $2a + \frac{3}{a} - 1 = 11$ , then what is the value of  $4a^2 + \frac{9}{a^2}$ ?  
 यदि  $2a + \frac{3}{a} - 1 = 11$  है, तो  $4a^2 + \frac{9}{a^2}$  का मान ज्ञात कीजिए ?



Mother's Advance Maths • Algebra [Previous Year Questions]



### Solution

- 1. (B)**  $[2(x+y)]^3 - [3(x-y)]^3 = (5x-y)[4x^2 + 4y^2 + 8xy + 9x^2 + 9y^2 - 18xy + (2x+2y)(3x-3y)]$   
 $= (5x-y)[19x^2 + 7y^2 - 10xy]$

By comparison  
 $A = 19; B = 7; C = -10$   
 $\therefore A + B - C$   
 $= 19 + 7 - (-10)$   
 $= 36.$

**2. (C)**  $x + y = 4$

$$\frac{1}{x} + \frac{1}{y} = \frac{16}{15}$$

$$xy = \frac{15}{4}$$

$$x^3 + y^3 = (x+y)[(x+y)^2 - 3xy]$$

$$= 4\left(16 - 3 \times \frac{15}{4}\right) = 4\left(\frac{64 - 45}{4}\right) = 19$$

3. (C)  $x + \frac{1}{x} = 4$

$$x^2 + \frac{1}{x^2} = 14$$

$$\text{and } x^3 + \frac{1}{x^3} = 64 - 12 = 52$$

$$x^5 + \frac{1}{x^5} = \left(x^2 + \frac{1}{x^2}\right)\left(x^3 + \frac{1}{x^3}\right) - \left(x + \frac{1}{x}\right) \\ = 14 \times 52 - 4 = 724$$

4. (D)  $x - y = 11$

$$\Rightarrow \frac{1}{x} - \frac{1}{y} = \frac{11}{24}$$

$$\Rightarrow \frac{x-y}{xy} = \frac{11}{24}$$

$$\Rightarrow xy = -24$$

$$\begin{aligned}\therefore x^3 - y^3 + x^2y^2 &= (x - y)[(x - y)^2 + 3xy] + x^2y^2 \\&= 11[121 - 72] + 576 \\&= 539 + 576 \\&= 539 + 576 \\&= 1115\end{aligned}$$

5. (A)  $16x^2 + y^2 = 48, \quad xy = 2, \quad x, y > 0$

$$16x^2 + y^2 + 8xy = 48 + 8xy$$

$$(4x + y)^2 = 48 + 16$$

$$4x + y = \sqrt{64} = 8$$

$$\begin{aligned}\therefore 64x^3 + y^3 &= (4x + y)[(4x + y)^2 - 3(4xy)] \\8[64 - 3(4 \times 2)] &= 8 \times 40 = 320\end{aligned}$$

6. (A)  $x - \frac{1}{x} = 5 \Rightarrow x^3 - \frac{1}{x^3} = 125 + 15 = 140$   
 $x^2 - 1 = 54$

$$\Rightarrow \frac{x^6 - 5x^3 - 1}{x^3 + 7x^3 - 1} = \frac{x^3 - \frac{1}{x^3} - 5}{x^3 - \frac{1}{x^3} + 7} = \frac{135}{147} = \frac{45}{49}$$

7. (D)  $x - \frac{1}{x} = 1 \Rightarrow x^2 + \frac{1}{x^2} = 3$

$$x^4 + \frac{1}{x^4} = 7 \Rightarrow x^8 + \frac{1}{x^8} = 47$$

8. (B)  $x^4 + \frac{1}{x^4} = 727 \Rightarrow x^2 + \frac{1}{x^2} = 27$

$$x^2 + \frac{1}{x^2} - 2 = 25 \Rightarrow x - \frac{1}{x} = 5 \quad (x > 1)$$

9. (A)  $2x^2 - 8x - 1 = 0$

$$2x - \frac{1}{x} = 8$$

$$\begin{aligned}8x^3 - \frac{1}{x^3} &= 8^3 + 3\left(24 \times \frac{1}{x}\right) \times 8 \\&= 512 + 48 = 560\end{aligned}$$

10. (C)  $x + y + z = 2$

$$xy + yz + zx = -11$$

$$x^3 + y^3 + z^3 - 3xyz = (x + y + z)[(x + y + z)^2 - 3(xy + yz + zx)]$$

$$= 2[4 + 33] = 74$$

11. (D)  $a^3 + b^3 = 405, \quad a + b = 9$

$$a^2 + b^2 + 2ab = 81$$

$$a^2 + b^2 - ab = 81 - 3ab$$

$$\Rightarrow \frac{a^3 + b^3}{a + b} = a^2 + b^2 - ab$$

$$\Rightarrow 45 = 81 - 3ab$$

$$\Rightarrow ab = 12$$

12. (C)  $2x - \frac{3}{x} = 2$

$$4x^2 + \frac{9}{x^2} = 2^2 + 2(6)$$

$$\Rightarrow 4x^2 + \frac{9}{x^2} = 16$$

$$\begin{aligned}\Rightarrow 16x^4 + \frac{81}{x^4} &= (16)^2 - 2(4 \times 9) \\&= 256 - 72 = 184\end{aligned}$$

13. (B)  $4x^4 - 37x^2 + 9 = 0,$

$$4x^2 + \frac{9}{x^2} = 37$$

$$2x - \frac{3}{x} = \sqrt{37 - 12} = 5 \quad \left(x > \sqrt{\frac{3}{2}}\right)$$

$$\begin{aligned}8x^3 - \frac{27}{x^3} &= 125 + 3(6)5 \\&= 125 + 90 = 215\end{aligned}$$

14. (B)  $a - \frac{12}{a} = 1$

$$\Rightarrow a^2 - a - 12 = 0$$

$$\Rightarrow a^2 - 4a + 3a - 12 = 0$$

$$\Rightarrow a = 4, -3 \quad (a > 0)$$

$$\Rightarrow a^2 + \frac{16}{a^2} = 16 + 1 = 17$$

15. (B)  $\frac{(16\sqrt{2}x^3 + 81\sqrt{3}y^3)}{2\sqrt{2}x + 3\sqrt{3}y}$

$$= (2\sqrt{2}x)^2 + (3\sqrt{3}y)^2 - (2\sqrt{2}x)(3\sqrt{3})y$$

$$= 8x^2 + 27y^2 - 6\sqrt{6}xy$$

$$\text{By comparison } A = 8, B = 27, C = -6\sqrt{6}$$

$$\Rightarrow 2A - 3B - 2\sqrt{6}C = 2 \times 8 - 3 \times 27 - 2\sqrt{6}$$

$$(-6\sqrt{6})$$

$$\Rightarrow 16 - 81 + 72 = 7$$

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**16.(A)**  $x + y = 2$

$$\frac{1}{x} + \frac{1}{y} = \frac{18}{5}$$

$$\Rightarrow \frac{x+y}{xy} = \frac{18}{5}$$

$$\Rightarrow xy = \frac{5}{9}$$

$$\therefore x^3 + y^3 = (x+y)[(x+y)^2 - 3xy] \\ = 2\left(4 - 3 \times \frac{5}{9}\right) \Rightarrow 2\left(4 - \frac{5}{3}\right) = 4\frac{2}{3}$$

**17.(C)**  $p - 2q = 3$

$$pq = 5$$

$$p^3 - 8q^3 = (p - 2q)[(p - 2q)^2 + 3p(2q)] \\ = 3(9 + 3 \times 2 \times 5) \\ = 3 \times 39 = 117$$

**18.(B)**  $x^2 + 4y^2 = 53$

$$x - 2y = 5$$

$$x^2 + 4y^2 - 4xy = 25$$

$$xy = 7$$

$$\therefore x^3 - 8y^3 = (x - 2y)[x^2 + 4y^2 + (2xy)] \\ = 5[53 + 14] \Rightarrow 5 \times 67 = 335$$

**19.(C)**  $x + y + z = 7$

$$\Rightarrow (x + y + z)^2 = x^2 + y^2 + z^2 + 2(xy + yz + zx)$$

$$\Rightarrow x^2 + y^2 + z^2 = 85$$

$$\Rightarrow x^3 + y^3 + z^3 = 913$$

$$\Rightarrow 2(xy + yz + zx) = 49 - 85 = 36$$

$$\Rightarrow (xy + yz + zx) = -18$$

$$\Rightarrow x^3 + y^3 + z^3 - 3xyz = [x + y + z](x^2 + y^2 + z^2 - (xy + yz + zx))$$

$$\Rightarrow -3xyz = 7(85 + 18) - 913$$

$$\Rightarrow xyz = 64$$

$$\Rightarrow \sqrt[3]{xyz} = 4$$

**20.(A)**  $a^2 + c^2 + 17 = 2(a - 8b + 2b^2)$

$$\text{Put } a = 1, b = -2, c = 0$$

$$\Rightarrow a^3 + b^3 + c^3 = 1 - 8 + 0 = -7$$

**21.(B)**  $\frac{(3\sqrt{2}x)^3 + (2\sqrt{3}y)^3}{3\sqrt{2}x + 2\sqrt{3}y} = 18x^2 + 12y^2 - 6\sqrt{6}xy$   
 $= (18)^2 - (12^2 + 216)$   
 $= 324 - 360 = -36$

**22.(A)**  $x^2 - \sqrt{11}x + 1 = 0$

$$x + \frac{1}{x} = \sqrt{11}$$

$$x^3 + \frac{1}{x^3} = 11\sqrt{11} - 3\sqrt{11} = 8\sqrt{11}$$

**23.(B)**  $(x + y)^3 + (3x - 3y)^3 = (4x - 2y)[(x + y)^2 + (3x - 3y)^2 - (x + y)(3x - 3y)] \\ = (4x - 2y)[7x^2 + 13y^2 - 16xy] \\ \Rightarrow A = 4, B = 7, C = -16$

$$\therefore A - B - C = 4 - 7 + 16 = 13$$

**24.(C)**  $x^8 - 433x^4 + 16 = 0$

$$x^4 + \frac{16}{x^4} = 433$$

$$x^2 + \frac{4}{x^2} = 21$$

$$x + \frac{2}{x} = \sqrt{21+4} = 5$$

**25.(C)**  $4x^4 = 5x^2 - 1$

$$\text{Put } x = 1$$

$$\therefore 2x^2 - x - 1 = 0$$

**26.(B)**  $x^2 + 9y^2 + 4z^2 = 12(x - 2y + 2z) - 88 \\ = 2(6x - 12y + 12z) - 88$

$$x = 6, y = \frac{-12}{9}, z = \frac{12}{4}$$

$$x - 3y + z = 6 - \left(-\frac{4}{3}\right) + 3 \\ = 13$$

**27.(D)**  $x^4 + y^4 + x^2y^2 = 21$   
 $x^2 + y^2 - xy = 7$

$$x^2 + y^2 + xy = \frac{21}{7} = 3$$

$$2(x^2 + y^2) = 10$$

$$x^2 + y^2 = 5$$

$$\text{and } -2xy = 4$$

$$xy = -2$$

$$\Rightarrow \frac{x}{y} + \frac{y}{x} = \frac{x^2 + y^2}{xy} = \frac{5}{-2} = -\frac{5}{2}$$

**28.(A)**  $x + y = 3, \quad \frac{1}{x} + \frac{1}{y} = \frac{-3}{10}$   
 $x^2 + y^2 + 2xy = 9 \quad \dots \dots \dots \text{(i)}$

$$\text{and } \frac{x+y}{xy} = -\frac{3}{10}$$

$$xy = -10 \text{ put in (i)}$$

$$x^2 + y^2 = 9 + 2(10) \\ = 29$$

**29.(C)**  $x + y + z = 1$   
 $\text{and } xy + yz + zx = xyz = -4$   
 $\Rightarrow x^3 + y^3 + z^3 - 3xyz = (x + y + z)[(x + y + z)^2 - 3(xy + yz + zx)]$   
 $x^3 + y^3 + z^3 = 1[1 - 3(-4)] - 12 = 1$

**30.(A)**  $125x^6 - \frac{1}{x^3} - 3(25x^4) \frac{1}{x} + 3(5x^2) \left( \frac{1}{x^2} \right)$   
constant value = 15

**31.(A)**  $x + \frac{1}{x} = 5\sqrt{2} \Rightarrow x^2 + 1 = 5\sqrt{2}x$   
 $\Rightarrow \frac{x(x^2 + \frac{1}{x^2})}{x^2 + 1} = \frac{x(50 - 2)}{5\sqrt{2}x} = \frac{48}{5\sqrt{2}} = \frac{24\sqrt{2}}{5}$

**32.(D)**  $a + b + c = 0$   
Put 2, -1, -1  
 $\Rightarrow \frac{(a+b)^2}{ab} + \frac{(b+c)^2}{bc} + \frac{(a+c)^2}{ca}$   
 $\Rightarrow \frac{c^2}{ab} + \frac{a^2}{bc} + \frac{b^2}{ca} \Rightarrow \frac{a^3 + b^3 + c^3}{abc} = 3$   
 $\Rightarrow \frac{(z-1)^2}{-2} + \frac{(-1-1)^2}{1} + \frac{(-1+2)^2}{-2}$   
 $\Rightarrow -\frac{1}{2} + 4 - \frac{1}{2} = 3$

**33.(B)**  $x - \frac{1}{x} = \sqrt{77}$

$$x^2 + \frac{1}{x^2} + 4 = 81$$

$$\left( x^2 + \frac{1}{x^2} \right)^2 = (9)^2$$

$$x + \frac{1}{x} = \pm 9$$

$$x^3 + \frac{1}{x^3} = (-9)^3 - 3(-9)$$

$$= -702$$

**34.(C)**  $a^3 - b^3 = 2349$   
 $a - b = 9$

$$a^2 + b^2 + ab = \frac{2349}{9} = 261$$

$$\therefore (a+b)^2 - ab = a^2 + b^2 + ab = 261$$

**35.(C)**  $2a + \frac{3}{a} = 12$

$$4a^2 + \frac{9}{a^2} = 144 - 2(2)(3)$$

$$= 132$$

**36.(C)**  $a^2 + b^2 + c^2 = 2(6a + 6b - 12c) - 216$   
 $a = 6, b = 6, c = -12$   
 $\therefore \sqrt{36 + 72 + 72} = \sqrt{180} = 6\sqrt{5}$

**37.(A)**  $(x - y + z)^2 - (x - y - z)^2$   
 $= (x - y + z + x - y - z)(x - y + z - x + y + z)$   
 $= 2(x - y)2z$   
 $= 4xz - 4yz$

**38.(B)**  $\frac{x^2 + y^2}{xy} = 2$

$$x^2 + y^2 - 2xy = 0$$

$$(x - y) = 0$$

**39.(D)**  $\frac{(2\sqrt{7}x)^3 - (\sqrt{2}y)^3}{2\sqrt{7}x - \sqrt{2}y}$   
 $= (2\sqrt{7}x)^2 + (\sqrt{2}y)^2 + 2\sqrt{15}xy$   
 $= 28x^2 + 2y^2 + 2\sqrt{14}xy$   
 $A + B - \sqrt{14}C = 28 + 2 - \sqrt{14} \times (-2\sqrt{14})$   
 $= 28 + 2 + 28 = 58$

**40.(C)**  $\sqrt{x} - \frac{1}{\sqrt{x}} = \sqrt{7}$

$$x + \frac{1}{x} = 9$$

$$x^2 + \frac{1}{x^2} = 81 - 2 = 79$$

**41.(B)**  $x - y = 4$   
 $x^3 - y^3 = 316$   
 $\Rightarrow \frac{x^3 - y^3}{x - y} = x^2 + y^2 + xy = 79$

and  $x^2 + y^2 - 2xy = 16$

$79 - xy - 2xy = 16$

$3xy = 63$

$xy = 21$

$$x^2 + y^2 = 16 + 42$$

$$= 58$$

and  $(x + y)^2 = \sqrt{42 + 58}$   
 $= \sqrt{100}$

$$\therefore x^4 - y^4 = (x^2 + y^2)(x^2 - y^2)$$

$$= 58(x - y)(x + y)$$

$$= 38 \times 4 \times 10 = 2320$$

**42.(C)**  $(3x - 4)^3$   
 $= 27x^3 - 64 - 3(3x^2)4 + 3(3x)16$   
cofficient of x = 144

**43.(C)**  $x + y + z = 3$   
 $xy + yz + zx = -12$   
 $xyz = -16$   
 $x^3 + y^3 + z^3 - 3(-16) = 3[(9 - 3(-12))]$   
 $= 3(45)$

$$\sqrt{x^2 + y^2 + z^2 + 13} = \sqrt{135 - 48 + 13}$$

$$\Rightarrow \sqrt{135 - 35} = 10$$

**Mother's Advance Maths • Algebra [Previous Year Questions]**

**44.(C)**  $(x+6)^3 + (2x+3)^3 + (3x+5)^3 - 3(x+6)(2x+3)(3x+5) = 0$   
 $\therefore [x+6 + 2x+3 + 3x+5] = 0$   
 $6x+14 = 0$

$$\Rightarrow x = -\frac{7}{3}$$

**45.(B)**  $x^4 + x^2y^2 + y^4$   
 $x^2 + 2y + y^2 = 3$   
 $x^2 - xy + y^2 = 7$   
 $2xy = -4$   
 $-xy = 2$

**46.(B)**  $x + \frac{1}{x} = 2\sqrt{5}$        $x^3 + \frac{1}{x^3}$   
 $x^2 + 1 = 2\sqrt{5}x$

$$x\left(x^3 + \frac{1}{x^3}\right) = \frac{34\sqrt{5}}{2\sqrt{5}} = 17$$

**47.(A)**  $9a^2 + 9b^2 + c^2 = 2(6a + 12b) - 20$

$$a = \frac{6}{9}, b = \frac{12}{9}, c = 0$$

$$\sqrt{6 \times \frac{2}{3} + 9 \times \frac{12}{9} + 0} = \sqrt{16} = 4$$

**48.(B)**  $x+y+z=2, x^3+y^3+z^3-3xyz=74$   
 $x^2+y^2+z^2+z(yz+yz+zx)=4$

$$(xy+yz+zx) = \frac{4 - (x^2 + y^2 + z^2)}{2}$$

$$74 = 2 \left[ 2^2 - 3 \left( \frac{4 - (x^2 + y^2 + z^2)}{2} \right) \right]$$

$$37 = \left[ 4 - \frac{3}{2} (4 - (x^2 + y^2 + z^2)) \right]$$

$$33 + 6 = 3(x^2 + y^2 + z^2)$$

$$13 = x^2 + y^2 + z^2$$

**49.(D)**  $\frac{(2x+y)^3 - (x-2y)^3}{(x+3y)}$

$$\begin{aligned} &= (2x+y)^2 + (x-2y)^2 + (2x+y)(x-2y) \\ &= 4x^2 + y^2 + 4xy + x^2 + 4y^2 - 4xy + 2x^2 - 4xy - xy \\ &\quad - 2y^2 \\ &= 7x^2 + 3y^2 - 5xy \end{aligned}$$

**50.(B)**  $a^4 + b^4 + a^2b^2 = 273$   
 $a^2 + b^2 - ab = 21$   
 $a^2 + b^2 + ab = 13$   
 $\underline{a^2 + b^2 = 17}$   
 $ab = -4$

$$\frac{1}{a} + \frac{1}{b} = \frac{a+b}{ab} = \frac{\sqrt{a^2 + b^2 + 2ab}}{ab} = \frac{\sqrt{17-8}}{-4} = -\frac{3}{4}$$

**51.(A)**  $x + \frac{1}{x} = 7 \Rightarrow x^2 + \frac{1}{x^2} = 47$

**52.(B)**  $2x + 3y = -1$   
 $8x^3 + 27y^3 + 18xy(2x+3y) = -1$   
 $8x^3 + 27y^2 - 18xy = -1$   
 $\therefore 8 - 1 = 7$

**53.(A)**  $x - \frac{2}{x} = 15$

$$x^2 + \frac{4}{x^2} = 225 + 4 \\ = 229$$

**54.(B)**  $y = zx + 1$   
 $\Rightarrow 2x - y = -1$   
 $8x^3 - y^3 - 3(2xy)(-1) = -1$   
 $8x^3 - y^3 + 6xy + 1 = 0$

**55.(C)**  $x^4 - 62x^2 + 1 = 0$

$$x^2 + \frac{1}{x^2} = 62$$

$$x + \frac{1}{x} = 8$$

$$\therefore x^3 + \frac{1}{x^3} = 512 - 3(8) \\ = 488$$

**56.(A)**  $x^4 + \frac{1}{x^4} = 34$

$$x^2 + \frac{1}{x^2} = 6$$

$$x - \frac{1}{x} = 2$$

$$\therefore x^3 - \frac{1}{x^3} = 8 + 6 = 14$$

**57.(A)**  $\left(5 - \frac{x^2}{3}\right)^3$

$$= 125 - \left(\frac{x^2}{3}\right)^3 - 3 \times 25 \times \frac{x^2}{3} + 3(5) \frac{x^4}{9}$$

Coefficient of  $x^2 = -25$

# **ALGEBRA**

(SSC CGL (PRE) - 2019)

बीजगणित

### **(Previous Year Questions)**

**Mother's Advance Maths • Algebra [Previous Year Questions]**

11. On Simplification  $\frac{x^3 - y^3}{x[(x+y)^2 - 3xy]} \div \frac{y[(x-y)^2 + 3xy]}{x^3 + y^3} \times \frac{(x+y)^2 - (x-y)^2}{x^2 - y^2}$  is equal to :
- का मान ज्ञात कीजिए।
- (A) 4      (B) 1      (C)  $\frac{1}{2}$       (D)  $\frac{1}{4}$
12. If  $P = \frac{x^4 - 8x}{x^2 - x^2 - 2x}$ ,  $Q = \frac{x^2 + 2x + 1}{x^2 - 4x - 5}$  and  $R = \frac{2x^2 + 4x + 8}{x - 5}$ , then  $(P \times Q) \div R$  is equal to :
- हो, तो  $(P \times Q) \div R$  का मान ज्ञात कीजिए।
- (A)  $\frac{1}{2}$       (B) 1      (C) 2      (D) 4
13. If  $a + b + c = 7$  and  $ab + bc + ca = -6$ , then the value of  $a^3 + b^3 + c^3 - 3abc$  is :  
यदि  $a + b + c = 7$  और  $ab + bc + ca = -6$  है, तो  $a^3 + b^3 + c^3 - 3abc$  का मान .... होगा।
- (A) 469      (B) 472      (C) 463      (D) 479
14. If  $30x^2 - 15x + 1 = 0$ , then what is the value of  $25x^2 + (36x^2)^{-1}$ ?  
यदि  $30x^2 - 15x + 1 = 0$  है, तो  $25x^2 + (36x^2)^{-1}$  का मान ज्ञात करें।
- (A)  $\frac{9}{2}$       (B)  $6\frac{1}{4}$       (C)  $\frac{65}{12}$       (D)  $\frac{55}{12}$
15. If  $x + y + z = 3$ , and  $x^2 + y^2 + z^2 = 101$ , then what is the value of  $\sqrt{x^3 + y^3 + z^3 - 3xyz}$ ?  
यदि  $x + y + z = 3$ , और  $x^2 + y^2 + z^2 = 101$ , है, तो  $\sqrt{x^3 + y^3 + z^3 - 3xyz}$  का मान क्या है ?
- (A) 19      (B) 21      (C) 24      (D) 28
16. If  $12x^2 - 21x + 1 = 0$ , then what is the value of  $9x^2 + (16x^2)^{-1}$ ?  
यदि  $12x^2 - 21x + 1 = 0$  है, तो  $9x^2 + (16x^2)^{-1}$  का मान क्या है ?
- (A)  $\frac{429}{8}$       (B)  $\frac{465}{16}$       (C)  $\frac{417}{16}$       (D)  $\frac{453}{8}$
17. If  $2x^2 + y^2 + 8z^2 - 2\sqrt{2}xy + 4\sqrt{2}yz - 8zx = (Ax + y + Bz)^2$ , then the value of  $(A^2 + B^2 - AB)$  is:  
यदि  $2x^2 + y^2 + 8z^2 - 2\sqrt{2}xy + 4\sqrt{2}yz - 8zx = (Ax + y + Bz)^2$ , है, तो  $(A^2 + B^2 - AB)$  का मान ज्ञात कीजिये।
- (A) 16      (B) 14      (C) 6      (D) 18
18. If  $16a^4 + 36a^2b^2 + 81b^4 = 91$  and  $4a^2 + 9b^2 - 6ab = 13$ , then what is the value of  $3ab$ ?  
यदि  $16a^4 + 36a^2b^2 + 81b^4 = 91$  और  $4a^2 + 9b^2 - 6ab = 13$  है, तो  $3ab$  का मान क्या है ?
- (A) -3      (B) 5      (C)  $\frac{3}{2}$       (D)  $-\frac{3}{2}$
19. If  $P = \frac{x^3 + y^3}{(x-y)^2 + 3xy}$ ,  $Q = \frac{(x+y)^2 - 3xy}{x^3 - y^3}$  and  $R = \frac{(x+y)^2 - (x-y)^2}{x^2 - y^2}$  then what is the value of  $(P \div Q) \times R$ ?  
यह, तो  $(P \div Q) \times R$  का मान क्या है ?
- (A)  $2xy$       (B)  $2(x^2 + y^2)$       (C)  $x^2 + y^2$       (D)  $4xy$
20. If  $x^2 - 2\sqrt{5}x + 1 = 0$ , then what is the value of  $x^5 + \frac{1}{x^5}$ ?  
यदि  $x^2 - 2\sqrt{5}x + 1 = 0$  है, तो  $x^5 + \frac{1}{x^5}$  का मान क्या है ?
- (A)  $408\sqrt{5}$       (B)  $610\sqrt{5}$       (C)  $406\sqrt{5}$       (D)  $612\sqrt{5}$
21. If  $x^4 + x^2y^2 + y^4 = 273$  and  $x^2 - xy + y^2 = 13$  then the value of  $xy$  is :  
यदि  $x^4 + x^2y^2 + y^4 = 273$  और  $x^2 - xy + y^2 = 13$  है, तो  $xy$  का मान क्या होगा ?
- (A) 4      (B) 10      (C) 6      (D) 8
22. If  $20x^2 - 30x + 1 = 0$ , then what is the value of  $25x^2 + \frac{1}{16x^2}$ ?  
यदि  $20x^2 - 30x + 1 = 0$  है, तो  $25x^2 + \frac{1}{16x^2}$  का मान क्या होगा ?
- (A)  $58\frac{3}{4}$       (B)  $53\frac{3}{4}$       (C)  $53\frac{1}{2}$       (D)  $58\frac{1}{2}$



Mother's Advance Maths • Algebra [Previous Year Questions]

### Solution

- |   |   |  |   |  |  |  |                             |  |
|---|---|--|---|--|--|--|-----------------------------|--|
| 1. (D) $x - y = 4$<br>$xy = 45$<br>Let $x = 9; y = 5$<br>$x^3 - y^3 = 729 - 125$<br>$= 604$   | 2. (D) $x + y = 8$<br>$y + z = 13$<br>$z + x = 17$<br>$2(x + y + z) = 38$<br>$x + y + z = 19$<br>From equations<br>$x = 6; y = 2; z = 11$ | $\frac{x^2}{yz} = \frac{6 \times 6}{11 \times 2} = \frac{18}{11}$      | 3. (A) $x^{2a} + y^{2b} = 2^{2c} = k$<br>$x = k^{\frac{1}{2a}}$<br>$y = k^{\frac{1}{2b}}$<br>$z = k^{\frac{1}{2c}}$<br>$x^2 = yz$ | $k^a = k^{\frac{1}{2b} + \frac{1}{2c}}$<br>$\frac{1}{a} = \frac{b+c}{2bc}$<br>$2bc = ab + ac$ .... (1) | $\frac{ab + bc + ac}{bc}$                      | Put value from eq. (1)<br>$\frac{3bc}{bc} = 3$ |                             |  |
|   |   |  |   |  |  |  |                             |  |
| 4. (A) $(a + b - c)^3 + (a - b + c)^3 + 8a^3$<br>[ $\because a^3 + b^3 + c^3 = 3abc$ ; if $a + b + c = 0$ ]<br>$= 6a(a + b - c)(a - b + c)$ | 5. (A) $x^4 + x^2y^2 + y^4 = 21$<br>$x^2 + xy + y^2 = 7$ .... (i)   | $x^2 - xy + y^2 = \frac{21}{7} = 3$ .... (ii)                          |   |  |  |  |                             |  |
|   |   | From eq. (i) and (ii)<br>$x^2 + y^2 = 5$<br>$x^2 y^2 = 4$              | $\frac{1}{x^2} + \frac{1}{y^2} = \frac{x^2 + y^2}{x^2 y^2}$   |  |  |  |                             |  |
|   |   | Put values from equations<br>$\frac{x^2 + y^2}{x^2 y^2} = \frac{5}{4}$ | 6. (C) $x^2 + 3x + 1 = 0$   | $x + \frac{1}{x} = -3$   | $x^3 + \frac{1}{x^3} = (-3)^3 - (-3) \times 3$ | $x^3 + \frac{1}{x^3} = -27 + 9$                | $x^3 + \frac{1}{x^3} = -18$ |  |
|   |   |  |   |  |  |  |                             |  |
|   |   |  |   |  |  |  |                             |  |

**Mother's Advance Maths • Algebra [Previous Year Questions]**

8. (C)  $27a^3 - 2\sqrt{2}b^3$

$$(3a)^3 - (\sqrt{2}b)^3$$

$$[\because a^3 - b^3 = (a - b)(a^2 + b^2 + ab)] \\ = (3a - \sqrt{2}b)(9a^2 + 2b^2 + 3\sqrt{2}ab)$$

9. (D)  $a + b + c = 11$

$$ab + bc + ac = 3$$

$$abc = -135$$

$$a^3 + b^3 + c^3 - 3abc = (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ac)$$

$$121 = a^2 + b^2 + c^2 + 2 \times 3$$

$$\therefore a^2 + b^2 + c^2 = 115$$

Put values

$$a^3 + b^3 + c^3 + 405 = (11)(115 - 3)$$

$$a^3 + b^3 + c^3 = 1232 - 405$$

$$a^3 + b^3 + c^3 = 827$$

10. (C)  $5x + \frac{1}{3x} = 4$

$$3x + \frac{1}{5x} = \frac{12}{5}$$

$$9x^2 + \frac{1}{25x^2} = \frac{144}{25} - 2 \times \frac{3}{5} = \frac{114}{25}$$

11. (A) 
$$\frac{x^3 - y^3}{x[(x+y)^2 - 3xy]} \div \frac{y[(x-y)^2 + 3xy]}{x^3 + y^3}$$

$$= \frac{x^3 - y^3}{x(x^2 + y^2 - xy)} \times \frac{x^3 + y^3}{y(x^2 + y^2 + xy)} \times \frac{4xy}{x^2 - y^2}$$

$$= \frac{4(x+y)(x^2 - xy + y^2) \times (x-y)(x^2 + y^2 + xy)}{(x^2 + y^2 - xy)(x^2 + y^2 + xy) \times (x^2 - y^2)}$$

$$= 4$$

12. (A)  $P = \frac{x^4 - 8x}{x^3 - x^2 - 2x}; Q = \frac{x^2 + 2x + 1}{x^2 - 4x - 5}; R =$

$$\frac{2x^2 + 4x + 8}{x - 5}$$

$$(P \times Q) \div R = \left[ \frac{x^4 - 8x}{x^3 - x^2 - 2x} \times \frac{x^2 + 2x + 1}{x^2 - 4x - 5} \right] \times \frac{x - 5}{2x^2 + 4x + 8}$$

$$= \frac{(x-2)(x^2 + 4 + 2x)}{(x^2 - x - 2)} \times \frac{(x+1)^2}{(x^2 - 4x - 5)} \times \frac{x-5}{2(x^2 + 2x + 4)}$$

$$= \frac{(x-2)}{(x+1)(x-2)} \times \frac{(x+1)^2}{(x+1)(x-5)} \times \frac{(x-5)}{2} = \frac{1}{2}$$

13. (A)  $a + b + c = 7$

$$ab + bc + ac = -6$$

$$\therefore a^3 + b^3 + c^3 - 3abc = (a + b + c)[a^2 + b^2 + c^2 - ab - bc - ac]$$

$$[\because (a + b + c)^2 = a^2 + b^2 + c^2 + 2(ab + bc + ac)]$$

$$49 = a^2 + b^2 + c^2 + 2(-6)$$

$$a^2 + b^2 + c^2 = 61$$

$$a^3 + b^3 + c^3 - 3abc = 7[61 + 6]$$

$$= 67 \times 7 = 469$$

14. (D)  $30x^2 - 15x + 1 = 0$

$$30x^2 + 1 = 15x$$

$$5x + \frac{1}{6x} = \frac{5}{2}$$

Square both side

$$25x^2 + \frac{1}{36x^2} = \frac{25}{4} - \frac{5}{3}$$

$$25x^2 + (36x^2)^{-1} = \frac{75 - 20}{12} = \frac{55}{12}$$

15. (B)  $x + y + z = 3, x^2 + y^2 + z^2 = 101$

$$(x + y + z)^2 = x^2 + y^2 + z^2 + 2(xy + yz + zx)$$

$$xy + y + zx = -46$$

$$x^3 + y^3 + z^3 - 3xyz = (x + y + z)[x^2 + y^2 + z^2 - (xy + xz + yz)]$$

$$\Rightarrow 3[101 + 46]$$

$$= 441$$

$$= 21$$

16. (C)  $12x^2 + 1 = 21x$

$$12x + \frac{1}{x} = 21$$

divide by 4

$$3x + \frac{1}{4x} = \frac{21}{4}$$

After squaring both side

$$9x^2 + \frac{1}{16x^2} + 2 \cdot 3 \cdot \frac{1}{4} = \frac{441}{16}$$

$$9x^2 + \frac{1}{16x^2} = \frac{417}{16}$$

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17. (B)  $2x^2 + y^2 + 8z^2 - 2\sqrt{2}xy + 4\sqrt{2}yz - 8zx$   
 $= (Ax + Y + Bz)^2$   
 $(y - \sqrt{2}x + 2\sqrt{2}z)^2$   
 $= (Ax + y + Bz)^2$   
 $A = -\sqrt{2}; B = 2\sqrt{2}$   
 $A^2 + B^2 - AB = 2 + 8 + 4 = 14$
18. (D)  $16a^4 + 36a^2b^2 + 81b^4 = 91$   
 $4a^2 + 9b^2 - 6ab = 13 \dots \text{(i)}$   
 $[\because a^4 + a^4 + a^2b^2 = (a^2 + b^2 + ab)(a^2 + b^2 - ab)]$   
 $\text{So, } 4a^2 + 9b^2 + 6ab = \frac{91}{13} = 7 \dots \text{(ii)}$   
From eq. (i) & (ii)  
 $12ab = -6$   
 $3ab = -\frac{3}{2}$
19. (D)  $P = \frac{x^3 + y^3}{(x - y)^2 + 3xy}, Q = \frac{(x + y)^2 - 3xy}{x^3 - y^3}$   
 $R = \frac{(x + y)^2 - (x - y)^2}{x^2 - y^2}$   
 $(P + Q) \times R = \frac{x^3 + y^3}{(x - y)^2 + 3xy} \times \frac{x^3 - y^3}{(x + y)^2 - 3xy}$   
 $\times \frac{(x + y)^2 - (x - y)^2}{x^2 - y^2}$   
 $= \frac{(x + y)(x^2 + y^2 - 2xy)}{(x^2 + y^2 + xy)} \times \frac{(x - y)(x^2 + y^2 + xy)}{(x^2 + y^2 - xy)}$   
 $\times \frac{4xy}{(x - y)(x + y)} = 4xy$
20. (B)  $x^2 - 2\sqrt{5}x + 1 = 0$        $x + \frac{1}{x} = 2\sqrt{5}$   
 $\left[ x^5 + \frac{1}{x^5} = (x^3 + \frac{1}{x^3})(x^2 + \frac{1}{x^2}) - (x + \frac{1}{x}) \right]$   
 $x^3 + \frac{1}{x^3} = (2\sqrt{5})^3 - 3(2\sqrt{5})$   
 $= 40\sqrt{5} - 6\sqrt{5} = 34\sqrt{5}$   
 $x^2 + \frac{1}{x^2} = 20 - 2 = 18$   
So,  $34\sqrt{5} \times 18 - 2\sqrt{5} = 610\sqrt{5}$

21. (A)  $x^4 + x^2y^2 + y^4 = 273$   
 $x^2 - xy + y^2 = 13 \dots \text{(i)}$   
 $x^2 + xy + y^2 = \frac{273}{13} \Rightarrow 21 \dots \text{(ii)}$   
eq. (i) & (ii)  
 $2xy = 8$   
 $xy = 4$
22. (B)  $20x^2 - 30x + 1 = 0$   
 $5x + \frac{1}{4x} = \frac{15}{2}$   
 $25x^2 + \frac{1}{16x^2} + \frac{5}{2} = \frac{225}{4}$   
 $25x^2 + \frac{1}{16x^2} = \frac{215}{4} = 53\frac{3}{4}$
23. (C)  $x - \frac{1}{x} = 11$   
 $x^3 - \frac{1}{x^3} = 1331 + 33 = 1364$
24. (B)  $(a + b + c - d)^2 - (a - b - c + d)^2 = ?$   
Let,  $a = b = c = D$   
 $(a + b)^2 - 0 = 4a^2$   
go through option  
(B)  $4a(b + c - d)$   
 $= 4a(a) = 4a^2$
25. (B)  $(2x + y)^3 = 8x^3 + y^3 + 3 \times 2x \times y (2x + y)$   
 $= 8x^3 + y^3 + 6xy^2 + 12x^2y$   
coefficient of  $x^2 = 12y$
26. (C)  $3^a = 27^b = 81^c$   
 $3^a = 3^{3b} = 3^{4c}$   
 $\Rightarrow a = 3b = 4c = k$   
 $K \cdot \frac{K}{3} \cdot \frac{K}{4} = 144$   
 $K = 12$   
 $a = 12, b = 4, c = 3$
- $12 \left( \frac{1}{a} + \frac{1}{2b} + \frac{1}{5c} \right) = 12 \left( \frac{1}{12} + \frac{1}{8} + \frac{1}{15} \right)$   
 $= 1 + \frac{3}{2} + \frac{4}{5} = \frac{33}{10}$
27. (B)  $a + b + c = 9, ab + bc + ca = -22$   
 $(a + b + c)^2 = a^2 + b^2 + c^2 + 2(ab + bc + ca)$   
 $81 = a^2 + b^2 + c^2 - 44$   
 $a^2 + b^2 + c^2 = 125$   
 $a^3 + b^3 + c^3 - 3abc = (a + b + c)$   
 $[a^2 + b^2 + c^2 - ab - bc - ac] = 9 [125 + 22] = 9[147] = 1323$

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28. (C)  $(a+b-2)^2 + (b+c-5)^2 + (c+a-5)^2 = 0$

$$a+b=2 \quad \dots(i)$$

$$b+c=5 \quad \dots(ii)$$

$$c+a=5 \quad \dots(iii)$$

from equation (i), (ii) and (iii)

$$b=1, a=1$$

29. (D)  $a + \frac{1}{a} = 5 \quad a^3 + \frac{1}{a^3} = 5^3 - 3 \times 5$

$$= 125 - 15$$

$$= 110$$

30. (B)  $(x-3y)^3 = x^3 - 27y^3 - 3x \cdot 3y (x-3y)$

$$= x^3 - 27y^3 - 9x^2y + 27xy^2$$

Coefficient of x is  $27y^2$

31. (B)  $a^3 + \frac{1}{a^3} = 52$

If  $a + \frac{1}{a} = m$  then  $a^3 + \frac{1}{a^3} = m^3 - 3m$

$$m^3 - 3m = 52$$

$$m = 4$$

$$2(a + \frac{1}{a}) = 8$$

32. (D)  $x^2 - 4x + 4 = 0$

$$(x-2)^2 = 0$$

$$x = 2$$

$$16\left(x^4 - \frac{1}{x^4}\right) = 16\left(16 - \frac{1}{16}\right)$$

$$= 256 - 1 = 255$$

33. (C)  $b+c=ax, c+a=by, a+b=cz$

$$2(a+b+c) = ax+by+cz$$

$$x=2, y=2, z=2$$

$$\frac{1}{9}\left[\frac{1}{x+1} + \frac{1}{y+1} + \frac{1}{z+1}\right] = \frac{1}{9}\left[\frac{1}{3} + \frac{1}{3} + \frac{1}{3}\right] = \frac{1}{9}$$

34. (A)  $(2y-5)^3 = 8y^3 - 125 - 30y (2y-5)$

$$= 8y^3 - 125 - 60y^2 + 150y$$

coefficient of y = 150

35. (A)  $1 - 64x^3 - 12x + px^2 = (1 - 4x)^2$

$$1 - 64x^3 - 12x + px^2 = 1 - 64x^3 - 3 \times 4x (1 - 4x)$$

$$= 1 - 64x^3 - 12x + 48x^2$$

P = 48 will

36. (A)  $151^2 - 149^2 = (151 + 149)(151 - 149)$

$$= 300 \times 2 = 600$$

37. (B)  $\left(\frac{x}{3} + \frac{y}{5}\right)^3 = \frac{x^3}{27} + \frac{y^3}{125} + \frac{x^2y}{15} + \frac{xy^2}{25}$

$$\therefore (x+y)^3 = x^3 + y^3 + 3x^2y + 3xy^2$$

38. (C)  $a^2 + b^2 + c^2 = 300, ab + bc + ca = 50$

$$a+b+c = ?$$

$$(a+b+c)^2 = a^2 + b^2 + c^2 + 2(ab + bc + ca)$$

$$= 300 + 100 = 400$$

$$a+b+c = 20$$

39. (C)  $x+y+z = 10, xy+yz+zx = 15$

$$x^3 + y^3 + z^3 - 3xyz = (x+y+z)[(x+y+z)^2 - 3(xy + yz + zx)]$$

$$= 10(100 - 45) = 550$$

40. (A)  $(25a^2 - 9) \Rightarrow (5a - 3)(5a + 3)$

$$A^2 - B^2 = (A+B)(A-B)$$

41. (B)  $(a+b+2c)[a^2 + b^2 + 4c^2 - ab - 2bc - 2ca]$

$$\text{Let, } a = 1, b = 1, c = 1$$

$$(1+1+2)[1+1+4-1-2-2] \Rightarrow 4$$

Each the option

$$a^2 + b^2 + 8c^2 - 6abc \Rightarrow 1+1+8-6=4$$

So option B is true

42. (D)  $a^4 + \frac{1}{a^4} = 50, a^3 + \frac{1}{a^3} = ?$

$$a^2 + \frac{1}{a^2} = 2\sqrt{13}$$

$$a + \frac{1}{a} = \sqrt{2\sqrt{13} + 2}$$

$$\left(a^3 + \frac{1}{a^3}\right) = 2\sqrt{13} + 2 - \sqrt{2\sqrt{13} + 2}$$

$$= \sqrt{2\sqrt{13} + 2} [2\sqrt{13} + 2 - 3]$$

$$= \sqrt{2\sqrt{13} + 2} [2\sqrt{13} - 1]$$

43. (A)  $A + B = 12; AB = 17$

$$A^3 + B^3 = (A+B)^3 - 3AB(A+B)$$

$$= (12)^3 - 3 \times 17 \times 12$$

$$= 1782 - 612$$

$$= 1116$$

**Mother's एण्डवार्स • वीजगणित**

44. (A)  $(4a + 3b + 2c)^2$   
 $= 16a^2 + 9b^2 + 4c^2 + 24ab + 12bc + 16ac$

45. (B)  $(3a - 4b)^3$   
 $= 27a^3 - 64b^3 - 36ab(3a - 4b)$   
 $= 27a^3 - 64b^3 - 108a^2b + 144ab^2$

46. (A)  $x + y = 13$  ... (i)  
 $y + z = 15$  ... (ii)  
 $z + x = 16$  ... (iii)  
From eq. (i) (ii) and (iii)  
 $x + y + z = 22$   
So,  $x = 7, y = 6, z = 9$

Now,  $\frac{xy + xz}{xyz} = \frac{1}{z} + \frac{1}{y} = \frac{1}{9} + \frac{1}{6}$   
 $= \frac{2+3}{18} = \frac{5}{18}$

47. (D)  $a = 2b = 8c ; a + b + c = 13$

$a : b : c$   
So,  $8 : 4 : 1$

$\frac{\sqrt{a^2 + b^2 + c^2}}{2c}$

put values from equations

$\frac{\sqrt{64 + 16 + 1}}{2 \times 1} = \frac{\sqrt{81}}{2} = \frac{9}{2}$

48. (B)  $a^2 + b^2 - c^2 = 0$   
 $a^2 + b^2 = c^2$   
Cube both sides  $(a^2 + b^2)^3 = c^6$   
 $a^6 + b^6 + 3a^2b^2(a^2 + b^2) = c^6$   
 $(\therefore a^2 + b^2 = c^2)$   
 $c^6 = a^6 + b^6 + 3a^2b^2c^2$  .... (i)

From Question

$$\frac{2(a^6 + b^6 - c^6)}{3a^2b^2c^2}$$

Put value from eq. .... (i)

$$\frac{2(a^6 + b^6 - a^6 - b^6 - 3a^2b^2c^2)}{3a^2b^2c^2}$$
  
 $= \frac{2(-3a^2b^2c^2)}{3a^2b^2c^2} = -2$

49. (A)  $p + q = 7 ; pq = 5$   
 $p^3 + q^3 = (p+q)^3 - 3pq(p+q)$   
 $p^3 + q^3 = 7^3 - 3 \times 5 (7)$   
 $= 343 - 105 = 238$

50. (C)  $x + 3y + 2 = 0$   
 $x + 3y = -2$   
Cube both sides  
 $(x+3y)^3 = -8$   
 $x^3 + 27y^3 + 3.x.3y(x+3y) = -8$   
 $x^3 + 27y^3 + 3.x.3y (-2) = -8$   
 $x^3 + 27y^3 - 18xy + 8 = 0$

# **ALGEBRA**

(SSC CGL (PRE) - 2018)

बीजगणित

### **(Previous Year Questions)**

- 1.** If  $(5\sqrt{5}x^3 - 81\sqrt{3}y^3) \div (\sqrt{5}x - 3\sqrt{3}y) = (Ax^2 + By^2 + Cxy)$ , then the value of  $(6A + B - \sqrt{15}C)$  is :  
यदि  $(5\sqrt{5}x^3 - 81\sqrt{3}y^3) \div (\sqrt{5}x - 3\sqrt{3}y) = (Ax^2 + By^2 + Cxy)$  है, तो  $(6A + B - \sqrt{15}C)$  का मान क्या होगा ?  
(A) 10 (B) 9  
(C) 15 (D) 12

**2.** If  $x + y + z = 19$ ,  $x^2 + y^2 + z^2 = 133$  and  $xz = y^2$ , then the difference between  $z$  and  $x$  is:  
यदि  $x + y + z = 19$ ,  $x^2 + y^2 + z^2 = 133$  और  $xz = y^2$  है, तो  $z$  और  $x$  के बीच अंतर है :  
(A) 5 (B) 3  
(C) 6 (D) 4

**3.** If  $x^4 + x^{-4} = 194$ ,  $x > 0$ , then the value of  $(x - 2)^2$  is :  
यदि  $x^4 + x^{-4} = 194$ ,  $x > 0$  है, तो  $(x - 2)^2$  का मान क्या होगा ?  
(A) 1 (B) 6  
(C) 2 (D) 3

**4.** If  $16x^2 + 9y^2 + 4z^2 = 24(x - y + z) - 61$ , then the value of  $(xy + 2z)$  is:  
यदि  $16x^2 + 9y^2 + 4z^2 = 24(x - y + z) - 61$  है, तो  $(xy + 2z)$  का मान होगा :  
(A) 1 (B) 2  
(C) 3 (D) 7

**5.** If  $x + y + z = 19$ ,  $xy + yz + zx = 114$ , then the value of  $\sqrt{x^3 + y^3 + z^3 - 3xyz}$  is :  
यदि  $x + y + z = 19$ ,  $xy + yz + zx = 114$  है, तो  $\sqrt{x^3 + y^3 + z^3 - 3xyz}$  का मान होगा :  
(A) 21 (B) 17  
(C) 19 (D) 13

**6.** If  $[8(x + y)^3 - 27(x - y)^3] \div (5y - x) = Ax^2 + Bxy + Cy^2$ , then the value of  $(A + B + C)$  is:  
यदि  $[8(x + y)^3 - 27(x - y)^3] \div (5y - x) = Ax^2 + Bxy + Cy^2$  है, तो  $(A + B + C)$  का मान होगा :  
(A) 26 (B) 19  
(C) 16 (D) 13

**7.** If  $a^2 + b^2 + 64c^2 + 16c + 3 = 2(a + b)$ , then the value of  $4a^7 + b^7 + 8c^2$  is:  
यदि  $a^2 + b^2 + 64c^2 + 16c + 3 = 2(a + b)$  है, तो  $4a^7 + b^7 + 8c^2$  का मान ज्ञात कीजिये ?  
(A)  $3\frac{7}{8}$  (B)  $4\frac{7}{8}$  (C)  $4\frac{1}{8}$  (D)  $5\frac{1}{8}$

**8.** If  $x + y = 1$  and  $xy(xy - 2) = 12$ , then the value of  $x^4 + y^4$  is:  
यदि  $x + y = 1$  और  $xy(xy - 2) = 12$  है, तो  $x^4 + y^4$  का मान ज्ञात कीजिये ?  
(A) 19 (B) 25  
(C) 20 (D) 23

**9.** If  $(27x^3 - 343y^3) \div (3x - 7y) = Ax^2 + By^2 + 7Cxy$ , then the value of  $(4A - B + 5C)$  is :  
यदि  $(27x^3 - 343y^3) \div (3x - 7y) = Ax^2 + By^2 + 7Cxy$ , है, तो  $(4A - B + 5C)$  का मान ज्ञात कीजिये ?  
(A) 0 (B) 3  
(C) 2 (D) 1

**10.** If  $a^2 + b^2 + c^2 = 21$ , and  $a + b + c = 7$ , then  $(ab + bc + ca)$  is equal to:  
यदि  $a^2 + b^2 + c^2 = 21$ , और  $a + b + c = 7$  है, तो  $(ab + bc + ca)$  का मान ज्ञात कीजिये ?  
(A) 12 (B) 28  
(C) 14 (D) 8

**11.** If  $ab + bc + ca = 8$  and  $a^2 + b^2 + c^2 = 20$ , then a possible value of  $\frac{1}{2}[(a + b + c)[(a - b)^2 + (b - c)^2 + (c - a)^2]]$  is:  
यदि  $ab + bc + ca = 8$  और  $a^2 + b^2 + c^2 = 20$  है, तो  $\frac{1}{2}[(a + b + c)[(a - b)^2 + (b - c)^2 + (c - a)^2]]$  का एक संभव मान है :  
(A) 72 (B) 56  
(C) 84 (D) 80

**12.** If  $(8x^3 - 27y^3) \div (2x - 3y) = (Ax^2 + Bxy + Cy^2)$ , then the value of  $(2A + B - C)$  is:  
यदि  $(8x^3 - 27y^3) \div (2x - 3y) = (Ax^2 + Bxy + Cy^2)$  है, तो  $(2A + B - C)$  का मान है :  
(A) 4 (B) 6  
(C) 5 (D) 3

13. If  $x = a + \frac{1}{a}$  and  $y = a - \frac{1}{a}$  then  $\sqrt{x^4 + y^4 - 2x^2y^2}$

is equal to:

यदि  $x = a + \frac{1}{a}$  और  $y = a - \frac{1}{a}$  हैं तो  $\sqrt{x^4 + y^4 - 2x^2y^2}$  बराबर है:

- (A)  $16a^2$       (B) 8      (C)  $\frac{8}{a^2}$       (D) 4

14. If  $2x^2 + y^2 + 6x - 2xy + 9 = 0$ , Then the value of  $(4x^3 - y^3 + x^2y^2)$  is:

यदि  $2x^2 + y^2 + 6x - 2xy + 9 = 0$  है, तो  $(4x^3 - y^3 + x^2y^2)$  का मान है:

- (A) 0      (B) 9      (C) -3      (D) -9

15. If  $x + y = 12$  and  $xy = 27$ ,  $x > y$ , then the value of  $(x^3 - y^3)$  is:

यदि  $x + y = 12$  और  $xy = 27$ ,  $x > y$  है, तो  $(x^3 - y^3)$  का मान है:

- (A) 720      (B) 702      (C) 724      (D) 710

16. If  $x^2 + y^2 + z^2 = 133$ ,  $xy + yz + zx = 114$  and  $xyz = 216$ , then the value of  $x^3 + y^3 + z^3$  is:

यदि  $x^2 + y^2 + z^2 = 133$ ,  $xy + yz + zx = 114$  और  $xyz = 216$  है, तो  $x^3 + y^3 + z^3$  का मान ज्ञात कीजिये?

- (A) 948      (B) 999      (C) 942      (D) 1009

17. If  $3\sqrt{3}x^3 - 2\sqrt{2}y^3 = (\sqrt{3}x - \sqrt{2}y)(Ax^2 + By^2 + Cxy)$ , then the value of  $(A \times B) \div C$  is:

यदि  $3\sqrt{3}x^3 - 2\sqrt{2}y^3 = (\sqrt{3}x - \sqrt{2}y)(Ax^2 + By^2 + Cxy)$ , तो  $(A \times B) \div C$  का मान है:

- (A)  $6\sqrt{6}$       (B)  $6\sqrt{3}$       (C)  $\sqrt{3}$       (D)  $\sqrt{6}$

18. If  $a + \frac{1}{a} = 3$ , then  $\left(a^4 + \frac{1}{a^4}\right)$  is equal to:

यदि  $a + \frac{1}{a} = 3$  है, तो  $\left(a^4 + \frac{1}{a^4}\right)$  बराबर है:

- (A) 77      (B) 47      (C) 81      (D) 27

19. If  $a + b + c = 2$ ,  $a^2 + b^2 + c^2 = 26$ , then the value of  $a^3 + b^3 + c^3 - 3abc$  is:

यदि  $a + b + c = 2$ ,  $a^2 + b^2 + c^2 = 26$ , तब  $a^3 + b^3 + c^3 - 3abc$  का मान है:

- (A) 71      (B) 74      (C) 69      (D) 78

20. If  $(x^3 - 2\sqrt{2}y^3) \div (x - \sqrt{2}y) = (Ax^2 + Bxy + Cy^2)$  then,  $(2A + 4\sqrt{2}B - 4C) = ?$

यदि  $(x^3 - 2\sqrt{2}y^3) \div (x - \sqrt{2}y) = (Ax^2 + Bxy + Cy^2)$  है, तो  $(2A + 4\sqrt{2}B - 4C) = ?$

- (A) 4      (B) 2      (C) 1      (D) 0

21. If  $x^4 - 6x^2 - 1 = 0$ , then the value of  $x^6 - 5x^2$

$$+ \frac{5}{x^2} - \frac{1}{x^6} + 5$$

यदि  $x^4 - 6x^2 - 1 = 0$  है, तो  $x^6 - 5x^2 + \frac{5}{x^2} - \frac{1}{x^6} + 5$  का मान है:

- (A) 219      (B) 209      (C) 204      (D) 239

22. If  $x = 2 - p$ , then  $x^3 + 6xp + p^3$  is equal to:

यदि  $x = 2 - p$  है, तो  $x^3 + 6xp + p^3$  बराबर है:

- (A) 12      (B) 6      (C) 8      (D) 4

23. If  $9a^2 + 4b^2 + c^2 + 21 = 4(3a + b - 2c)$ , then the value of  $(9a + 4b - c)$

यदि  $9a^2 + 4b^2 + c^2 + 21 = 4(3a + b - 2c)$ , तो  $(9a + 4b - c)$  का मान है:

- (A) 2      (B) 16      (C) 6      (D) 12

24. If  $(135\sqrt{5}x^3 - 2\sqrt{2}y^3) \div (3\sqrt{5}x - \sqrt{2}y) = Ax^2 + By^2 + \sqrt{10}Cxy$ , then the value of  $(A + B - 9c)$  is:

यदि  $(135\sqrt{5}x^3 - 2\sqrt{2}y^3) \div (3\sqrt{5}x - \sqrt{2}y) = Ax^2 + By^2 + \sqrt{10}Cxy$ , तो  $(A + B - 9c)$  का मान है:

- (A) 18      (B) 12      (C) 20      (D) 10

25. If  $x^2 - 3x - 1 = 0$ , then the value of  $(x^2 + 8x - 1)(x^3 + x^{-1})$

$(x^3 + x^{-1})^{-1}$  is

यदि  $x^2 - 3x - 1 = 0$ , तो  $(x^2 + 8x - 1)(x^3 + x^{-1})$  का मान है:

- (A)  $\frac{3}{8}$       (B) 8      (C) 1      (D) 3

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26. If  $(8x^3 + 27y^3) \div (2x + 3y) = (Ax^2 + Bxy + Cy^2)$ , Then the value of  $(5A + 4B + 3C)$  is:  
 यदि  $(8x^3 + 27y^3) \div (2x + 3y) = (Ax^2 + Bxy + Cy^2)$  हो, तो  $(5A + 4B + 3C)$  का मूल्य है:  
 (A) 26 (B) 23  
 (C) 24 (D) 27
27. If  $\frac{6x}{(2x^2 + 5x - 2)} = 1$ ,  $x > 0$ , then the value of  $x^3 + \frac{1}{x^3}$  is:  
 यदि  $\frac{6x}{(2x^2 + 5x - 2)} = 1$ ,  $x > 0$  हो, तो  $x^3 + \frac{1}{x^3}$  का मूल्य है:  
 (A)  $\frac{3}{8}\sqrt{17}$  (B)  $\frac{5\sqrt{17}}{8}$   
 (C)  $\frac{5\sqrt{17}}{16}$  (D)  $\frac{3}{4}\sqrt{17}$
28. If  $4x^2 - 6x + 1 = 0$ , then the value of  $8x^3 + (8x^3)^{-1}$  is:  
 यदि  $4x^2 - 6x + 1 = 0$  है, तो  $8x^3 + (8x^3)^{-1}$  का मान है :  
 (A) 36 (B) 13  
 (C) 18 (D) 11
29. If  $x + y + z = 0$ , then the value of  $(x^2 + y^2 + z^2) \div (z^2 - xy)$  is :  
 यदि  $x + y + z = 0$  है, तो  $(x^2 + y^2 + z^2) \div (z^2 - xy)$  का मान है :  
 (A) 1 (B) 2  
 (C) -2 (D) -1
30. If  $a^2 + b^2 + c^2 + 27 = 6(a + b + c)$ , then what is the value of  $\sqrt[3]{a^3 + b^3 - c^3}$ ?  
 यदि  $a^2 + b^2 + c^2 + 27 = 6(a + b + c)$  है, तो  $\sqrt[3]{a^3 + b^3 - c^3}$  का मान है :  
 (A) 3 (B) 1  
 (C) 9 (D) 6
31. If/यदि  $x + \frac{1}{x} = 3$ , then/है, तो  $x^3 + \frac{1}{x^3}$  is equal to/  
 बराबर है:  
 (A) 27 (B) 36  
 (C) 24 (D) 18
32. If/यदि  $\sqrt{x} - \frac{1}{\sqrt{x}} = 4$ , then/है, तो  $x^2 + \frac{1}{x^2}$  is equal to/  
 बराबर है :  
 (A) 192 (B) 326  
 (C) 322 (D) 256
33. If  $a + b + c = 13$  and  $ab + bc + ca = 54$ , then  $a^3 + b^3 + c^3 - 3abc$  is equal to :  
 यदि  $a + b + c = 13$  और  $ab + bc + ca = 54$  है, तो  $a^3 + b^3 + c^3 - 3abc$  किसके बराबर होगा ?  
 (A) 793 (B) 273  
 (C) 91 (D) 182
34. If  $x + \frac{1}{x} = \sqrt{5}$ , then  $x^3 + \frac{1}{x^3}$  is equal to :  
 यदि  $x + \frac{1}{x} = \sqrt{5}$  है, तो  $x^3 + \frac{1}{x^3}$  बराबर है :  
 (A)  $3\sqrt{5}$  (B)  $4\sqrt{5}$   
 (C)  $2\sqrt{5}$  (D)  $5\sqrt{5}$
35. If  $(3x - 1)^3 + (4x - 3)^3 + (2x + 1)^3 = 3(3x - 1)(4x - 3)(2x + 1)$  and  $x \neq \frac{1}{3}$ , then  $x = ?$   
 यदि  $(3x - 1)^3 + (4x - 3)^3 + (2x + 1)^3 = 3(3x - 1)(4x - 3)(2x + 1)$  और  $x \neq \frac{1}{3}$  है तो  $x = ?$   
 (A)  $\frac{1}{2}$  (B) 2 (C)  $\frac{1}{4}$  (D) 1
36. If  $a + b + c = 11$  and  $ab + bc + ca = 38$ , then  $a^3 + b^3 + c^3 - 3abc$  is equal to :  
 यदि  $a + b + c = 11$  और  $ab + bc + ca = 38$  है, तो  $a^3 + b^3 + c^3 - 3abc$  बराबर है :  
 (A) 44 (B) 77  
 (C) 55 (D) 66
37. If/यदि  $x - 5\sqrt{x} - 1 = 0$ , then/है, तो  $x^2 + \frac{1}{x^2}$  is equal to/बराबर है :  
 (A) 625 (B) 731  
 (C) 729 (D) 727
38. If/यदि  $\sqrt{x} + \frac{1}{\sqrt{x}} = \sqrt{6}$ , then/है, तो  $x^2 + \frac{1}{x^2}$  is equal to/बराबर है:  
 (A) 62 (B) 14  
 (C) 16 (D) 36
39. If  $a + b + c = 8$  and  $ab + bc + ca = 12$ , then  $a^3 + b^3 + c^3 - 3abc$  is equal to:  
 यदि  $a + b + c = 8$  तथा  $ab + bc + ca = 12$  हो, तो  $a^3 + b^3 + c^3 - 3abc$  बराबर है:  
 (A) 192 (B) 224  
 (C) 144 (D) 400

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$$y = \frac{114}{19} = 6$$

$$x + z = 13$$

by squaring ( $xz = y^2 = (6)^2 = 36$ )

$$x^2 + z^2 = 97$$

By hit and trial  $x = 4, z = 9$

Diff. between  $z$  and  $x$  is = 5

$$3. (D) \quad x^4 + \frac{1}{x^4} = 194; \quad x^2 + \frac{1}{x^2} = 14$$

$$x + \frac{1}{x} = 4$$

$$x^2 + 1 = 4x$$

$$x^2 - 4x + 4 = 3$$

$$(x-2)^2 = 3$$

$$4. (D) \quad (4x)^2 + (3y)^2 + (2z)^2 - 24x + 24y - 24z + 61 = 0 \\ [(4x)^2 - 2 \times 4 \times 3x + 9] + [(3y)^2 + 2 \times 3 \times 4y + 16] + [(2z)^2 - 2 \times 2z \times 6 + 36] = 0 \\ (4x-3)^2 + (3y-4)^2 + (2z-6)^2 = 0$$

$$\Rightarrow x = \frac{3}{4}, y = \frac{4}{3}, z = 3$$

$$\Rightarrow xy + 2z = \frac{3}{4} \times \frac{4}{3} + 2 \times 3 = \frac{1}{1+6} = 7$$

5. (C) As we know,

$$x^3 + y^3 + z^3 - 3xyz = (x+y+z) \\ ((x+y+z)^2 - 3(xy+yz+zx)) \\ \sqrt{x^3 + y^3 + z^3} = \sqrt{19(361 - 3 \times 114)} \\ = \sqrt{19(361 - 342)} \\ = \sqrt{19 \times 19} \\ = 19$$

$$6. (C) \quad [2(x+y)]^3 - [3(x-y)]^3 \\ [2(x+y) - 3(x-y)] \times [4(x-y)^2 + 9(x-y)^2 + 6(x^2 - y^2)] \\ (5y-x)(4x^2 + 4y^2 + 8xy + 9x^2 + 9y^2 - 18xy + 6x^2 - 6y^2) \\ = (5y-x)(19x^2 + 7y^2 - 10xy)$$

Acc. to question

$$A = 19, B = 7, C = -10$$

$$A + B + C = 19 + 7 - 10 = 16$$

$$7. (D) \quad (a^2 - 2a + 1) + (b^2 - 2a + 1) + [(8c)^2 + 2(8c)(1) + 1] = 0$$

$$(a-1)^2 + (b-1)^2 + (8c+1)^2 = 0$$

$$\Rightarrow a = 1, b = 1, c = -\frac{1}{8}$$

$$4a^2 + b^2 + 8c^2$$

$$4(1) + (1) + 8 \times \frac{1}{8 \times 8} \Rightarrow 5 + \frac{1}{8} = \frac{41}{8} = 5\frac{1}{8}$$

8. (B)

$$x + y = 1$$

$$\text{given, } (xy)^2 - 2xy = 12 \\ x^4 + y^4 = (x^2 + y^2) - 2x^2y^2 \\ = [(x+y)^2 - 2xy]^2 - 2x^2y^2 \\ = (1 - 2xy)^2 - 2x^2y^2 \\ = 1 - 4xy + 2x^2y^2 \\ = 1 + 24 = 25$$

9. (C)

$$\frac{(3x)^3 - (7y)^3}{3x - 7y}$$

$$= 9x^2 + 49y^2 + 21xy = Ax^2 + By^2 + Cyx \\ A = 9, B = 49, C = 21 \\ C = 3 \\ 4A - B + 5C = 4(9) - 49 + 5(3) \\ = 36 + 15 - 49 \\ = 51 - 49 = 2$$

10. (C)

As we know,

$$(a+b+c)^2 = a^2 + b^2 + c^2 + 2(ab + bc + ca) \\ (7)^2 = 21 + 2(ab + bc + ca)$$

$$\frac{49 - 21}{2} = ab + bc + ca$$

$$\Rightarrow ab + bc + ca = \frac{28}{2} = 14$$

11. (A)

$$ab + bc + ca = 8, a^2 + b^2 + c^2 = 20$$

$$\text{Put } c = 0$$

$$ab = 8, \quad a^2 + b^2 = 20$$

$$a + b = 6$$

$$\Rightarrow \frac{1}{2}(a+b+c)[(a-b)^2 + (b-c)^2 + (c-a)^2]$$

$$\Rightarrow 6(12 - 8)$$

$$= 6(12)$$

$$= 72$$

12. (C)

$$\frac{(2x)^3 - (3y)^3}{2x - 3y} = \frac{(2x - 3y)(4x^2 + 9y^2 + 6xy)}{(2x - 3y)} \\ = 4x^2 + 9y^2 + 6xy$$

Comparing

$$A = 4, B = 6, C = 9$$

$$\Rightarrow 2A + B - C = 2(4) + 6 - 9 = 5$$

13. (D)

$$x = a + \frac{1}{a} \quad y = a - \frac{1}{a}$$

$$\text{Put } a = 1$$

$$\Rightarrow x = 2$$

$$\Rightarrow y = 0$$

$$\Rightarrow \sqrt{x^4 + y^4 - 2x^2y^2} = \sqrt{2^4} = 4$$

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- 14. (A)**  $x^2 + x^2 + y^2 + 6x - 2xy + 9 = 0$   
 $(x^2 + 6x + 9) + (x^2 + y^2 - 2xy) = 0$   
 $(x + 3)^2 + (x - y)^2 = 0$   
 $\Rightarrow x = -3, x = y$   
 $\Rightarrow 4(-3)^3 - (-3)^3 + (-3)^1$   
 $\Rightarrow -27 \times 3 + 81$   
 $\Rightarrow 0$
- 15. (B)**  $x + y = 12$        $xy = 27$   
 By hit and Trial  
 $x = 9, y = 3$   
 $x^3 - y^3 = 9^3 - 3^3$   
 $= 729 - 27$   
 $= 702$
- 16. (D)**  $x^3 + y^3 + z^3 - 3xyz$   
 $= (x^2 + y^2 + z^2 - xy - yz - zx)(x + y + z)$   
 $x^3 + y^3 + z^3 - 3 \times 216 = (133 - 114)(x + y + z)$   
 $\therefore (x + y + z)^2 = 133 + 2(114)$   
 $= 133 + 228$   
 $= 361$   
 $x + y + z = 19$   
 $x^3 + y^3 + z^3 - 648 = 19 \times 19$   
 $x^3 + y^3 + z^3 = 361 + 648$   
 $x^3 + y^3 + z^3 = 1009$
- 17. (D)**  $(\sqrt{3}x)^3 - (\sqrt{2}y)^3 = (\sqrt{3}x - \sqrt{2}y)(3x^2 + 2y^2 + \sqrt{6}xy)$   
 $= A = 3, B = 2, C =$   
 $\Rightarrow \frac{A \times B}{C} = \frac{3 \times 2}{\sqrt{6}} = \frac{6}{\sqrt{6}} = \sqrt{6}$
- 18. (B)**  $a + \frac{1}{a} = 3; a^2 + \frac{1}{a^2} = 7$   
 $a^4 + \frac{1}{a^4} = 49 - 2 = 47$
- 19. (B)** As we know,  
 $(a + b + c)^2 = (a^2 + b^2 + c^2) + 2(ab + bc + ca)$   
 $(2)^2 = a^2 + b^2 + c^2 + 2(ab + bc + ca)$   
 $4 = 26 + 2(ab + bc + ca)$   
 $ab + bc + ca = -11$   
 $a^3 + b^3 + c^3 - 3abc = (a + b + c)(a^2 + b^2 + c^2) - ab - bc - ca$   
 $\Rightarrow a^3 + b^3 + c^3 - 3abc = (2)(26 + 11)$   
 $\Rightarrow 2 \times 37 = 74$
- 20. (B)**  $a^3 - b^3 = (a - b)(a^2 + ab + b^2)$   
 by comparing the equ<sup>n</sup>  
 $Ax^2 + Bxy + Cy^2 = x^2 + \sqrt{2}xy + 2y^2$   
 $A = 1 : B = \sqrt{2}, C = 2$   
 So  $2A + 4\sqrt{2}B - 4C = 2$

- 21. (B)** Given  $x^2 - \frac{1}{x^2} = 6$  then  
 $x^6 - \frac{1}{x^6} = 234$   
 $x^6 - \frac{1}{x^6} - 5\left(x^2 - \frac{1}{x^2}\right) + 5$   
 $= 234 - 5(6) + 5$   
 $= 209$
- 22. (C)**  $x + p = 2$   
 $x^3 + p^3 + 6xp = 8$
- 23. (D)**  $9a^2 + 4b^2 + c^2 + 21 - 12a - 4b + 8c = 0$   
 $(3a - 2)^2 + (2b - 1)^2 + (c + 4)^2 = 0$   
 $a = \frac{2}{3}, b = \frac{1}{2}, c = -4$   
 $9a + 4b - c = 12$
- 24. (C)**  $\frac{(A^3 - B^3)}{(A - B)} = A^2 + AB + B^2$   
 $= \frac{135\sqrt{5}x^3 - 2\sqrt{2}y^3}{(3\sqrt{5}x - \sqrt{2}y)} = 45x^2 + 2y^2 + 3\sqrt{10}xy$   
 $A + B - 9C = 47 - 27 = 20$
- 25. (C)**  $x^2 - 3x - 1 = 0$        $x - \frac{1}{x} = 3$   
 $\Rightarrow x^2 + \frac{1}{x^2} = 11$   
 $= \frac{x^2 + 8x - 1}{x^3 + \frac{1}{x}} \Rightarrow \frac{x\left(x - \frac{1}{x} + 8\right)}{x\left(x^2 + \frac{1}{x^2}\right)}$   
 $\Rightarrow \frac{(3+8)}{11} = \frac{11}{11} = 1$
- 26. (B)**  $(8x^3 + 27y^3) = Ax^2 + Bxy + Cy^2$   
 $\Rightarrow \frac{(2x+3y)[(2x)^2 - (2x)(3y) + (3y)^2]}{(2x+3y)}$   
 $= Ax^2 + Bxy + Cy^2$   
 $\Rightarrow (4x^2 - 6xy + 9y^2) = Ax^2 + Bxy + Cy^2$   
 comparing both sides, we have  
 $A = 4, B = b, C = 9$   
 $\Rightarrow (5A + 4B + 3C) = 5 \times 4 - 4 \times 6 + 3 \times 9$   
 $= 20 - 24 + 27 = +23$

27. (B)  $\frac{6x}{(2x^2+5x-2)} \Rightarrow \frac{2x^2+5x-2}{6x} = 1$   
 $\Rightarrow \frac{(2x^2-2)}{6x} + \frac{5}{6} = 1$   
 $\Rightarrow \frac{1}{3}\left(x - \frac{1}{x}\right) = \frac{1}{6}$

$$x - \frac{1}{x} = \frac{1}{2} \Rightarrow x + \frac{1}{x} = \sqrt{\frac{1}{4} + 4} = \frac{\sqrt{17}}{2}$$

Now,  $x^3 + \frac{1}{x^3} = \left(x + \frac{1}{x}\right)^3 - 3\left(x + \frac{1}{x}\right)$   
 $= \frac{17}{8}\sqrt{17} - \frac{3}{2}\sqrt{17} = \frac{5}{8}(\sqrt{17})$

28. (C)  $4x + \frac{1}{x} = 6$   
 $2x + \frac{1}{2x} = 3$   
 $8x^3 + \frac{1}{8x^3} + 3 \times 3 = 27$   
 $8x^3 + \frac{1}{8x^3} = 27 - 9 = 18$

29. (B)  $x + y + z = 0$   
Put  $z = 0$   
 $x = 1$   
 $y = -1$

$$\frac{x^2 + y^2 + z^2}{z^2 - xy} = \frac{1+1}{+1} = 2$$

30. (A)  $a^2 + b^2 + c^2 + 27 - 6a - 6b - 6c = 0$   
 $(a-3)^2 + (b-3)^2 + (c-3)^2 = 0$   
 $\Rightarrow a = b = c = 3$   
 $\Rightarrow \sqrt{a^2 + b^2 + c^2} = a = 3$

31. (D)  $x + \frac{1}{x} = 3$   
 $x^3 + \frac{1}{x^3} = 27 - 9 = 18$

32. (C)  $\sqrt{x} - \frac{1}{\sqrt{x}} = 4$   
 $x + \frac{1}{x} = 18$   
 $x^2 + \frac{1}{x^2} = 322$

33. (C)  $a^3 + b^3 + c^3 - 3abc = (13)(169 - 3 \times 54)$   
 $= (13)(169 - 162)$   
 $= 13 \times 7 = 91$

34. (C) As we know,

$$x^3 + \frac{1}{x^3} = \left(x + \frac{1}{x}\right)^3 - 3\left(x + \frac{1}{x}\right)$$

$$x^3 + \frac{1}{x^3} = (\sqrt{5})^3 - 3\sqrt{5} = 5\sqrt{5} - 3\sqrt{5} = 2\sqrt{5}$$

35. (B)  $a^3 + b^3 + c^3 - 3abc = 0$   
 $\Rightarrow a + b + c = 0$   
 $3x - 1 + 4x - 3 + 2x + 1 = 0$   
 $9x - 3 = 0$   
 $\Rightarrow x = \frac{1}{3}$   
but  $x \neq \frac{1}{3}$   
 $\Rightarrow a = b = c$

$$3x - 1 = 4x - 3$$

x = 2

36. (B)  $a^3 + b^3 + c^3 - 3abc$   
 $= (a + b + c)((a + b + c)^2 - 3(ab + bc + ca))$   
 $a^3 + b^3 + c^3 - 3abc = (11)(121 - 3 \times 38)$   
 $= (11)(121 - 114)$   
 $= 11 \times 7 = 77$

37. (D)  $x - 5\sqrt{x} = 1$   
Divide by  $\sqrt{x}$   
 $\sqrt{x} - 5 = \frac{1}{\sqrt{x}}$   
 $\sqrt{x} - \frac{1}{\sqrt{x}} = 5$   
 $x + \frac{1}{x} = 27$   
 $x^2 + \frac{1}{x^2} = 729 - 2$   
 $= 727$

38. (B)  $x + \frac{1}{x} = 4 ; x^2 + \frac{1}{x^2} = 14$

39. (B)  $(a + b + c)^2 = a^2 + b^2 + c^2 + 2(ab + bc + ca)$   
 $(8)^2 = a^2 + b^2 + c^2 + 2(12)$   
 $\Rightarrow a^2 + b^2 + c^2 = 64 - 24 = 40$   
 $a^3 + b^3 + c^3 - 3abc$   
 $= (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca)$   
 $a^3 + b^3 + c^3 - 3abc = (8)[40 - 12]$   
 $= 8[40 - 12]$   
 $= 8 \times 28 = 224$

40. (C) As we know,  
 $a^3 + b^3 = (a + b)^3 - 3ab(a + b)$   
 $a^3 + b^3 = (5)^3 - 3 \times 3 \times 5$   
 $= 125 - 45 = 80$

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**41. (D)** As we know,

$$\begin{aligned} a^3 + b^3 + c^3 - 3abc &= (a+b+c)[(a+b+c)^2 - 3(ab+bc+ca)] \\ a^3 + b^3 + c^3 - 3abc &= (6)(36 - 3 \times 4) \\ &= 6(36 - 12) \\ &= 6 \times 24 = 144 \end{aligned}$$

**42. (D)** As we know

$$\begin{aligned} a^3 + b^3 &= (a+b)^3 - 3ab(a+b) \\ a^3 + b^3 &= (6)^3 - 3 \times \frac{16}{3} \times 6 \\ &= 216 - 96 \\ &= 120 \end{aligned}$$

**43. (A)**  $\sqrt{x} - \frac{1}{\sqrt{x}} = \sqrt{6}$

$$x + \frac{1}{x} = 8$$

$$x^2 + \frac{1}{x^2} = 62$$

**44. (A)**  $a^3 + b^3 = (a+b)^3 - 3ab(a+b)$

$$\begin{aligned} &= (8)^3 - 3 \times \frac{32}{3}(8) \\ &= 512 - 32 \times 8 \\ &= 512 - 256 = 256 \end{aligned}$$

**45. (D)**  $\sqrt{x} + \frac{1}{\sqrt{x}} = \sqrt{7}$

$$x + \frac{1}{x} = 5$$

$$x^2 + \frac{1}{x^2} = 125 - 3 \times 5 = 110$$

**46. (D)**  $a^3 + b^3 + c^3 - 3abc$

$$\begin{aligned} &= (a+b+c)[(a+b+c)^2 - 3(ab+bc+ca)] \\ a^3 + b^3 + c^3 - 3abc &= (4)(16 - 3 \times 2) \\ &= 4(10) = 40 \end{aligned}$$

**47. (D)** As we know,

$$\begin{aligned} a^3 + b^3 &= (a+b)^3 - 3ab(a+b) \\ a^3 + b^3 &= (6)^3 - 3 \times 8 \times 6 \\ &= 216 - 144 \\ &= 72 \end{aligned}$$

**48. (B)**  $a^3 + b^3 + c^3 - 3abc$

$$\begin{aligned} &= (a+b+c)[(a+b+c)^2 - 3(ab+bc+ca)] \\ a^3 + b^3 + c^3 - 3abc &= (6)(36 - 3 \times 5) \\ &= 6 \times 21 \\ &= 126 \end{aligned}$$

**49. (A)**  $x + \frac{1}{x} = 6 \Rightarrow x^2 + \frac{1}{x^2} = 34$

**50. (B)**

$$\sqrt{x} - \frac{1}{\sqrt{x}} = 2\sqrt{2}$$

$$x + \frac{1}{x} = 8 + 2 = 10$$

$$x^2 + \frac{1}{x^2} = 98$$

**51. (A)** As we know,

$$\begin{aligned} a^3 + b^3 + c^3 - 3abc &= (a+b+c)[(a+b+c)^2 - 3(ab+bc+ca)] \\ 126 &= (6)[36 - 3(ab+bc+ca)] \\ 21 &= 36 - 3(ab+bc+ca) \\ \Rightarrow ab+bc+ca &= \frac{15}{3} = 5 \end{aligned}$$

**52. (B)** As we know,

$$\begin{aligned} a^3 + b^3 &= (a+b)^3 - 3ab(a+b) \\ a^3 + b^3 &= (5)^3 - 3 \times 3 \times 5 \\ &= 125 - 45 \\ &= 80 \end{aligned}$$

**53. (A)** As we know,

$$\begin{aligned} a^3 + b^3 + c^3 - 3abc &= (a+b+c)[(a+b+c)^2 - 3(ab+bc+ca)] \\ a^3 + b^3 + c^3 - 3abc &= (7)(49 - 3 \times 1) \\ &= 7 \times 46 = 322 \end{aligned}$$

**54. (B)** As we know,

$$\begin{aligned} a^3 - b^3 &= (a-b)^3 + 3ab(a-b) \\ a^3 - b^3 &= (5)^3 + 3 \times 2 \times 5 \\ &= 125 + 30 = 155 \end{aligned}$$

**55. (D)** Given

$$\sqrt{x} - \frac{1}{\sqrt{x}} = 3\sqrt{2}$$

Squaring both side

$$x + \frac{1}{x} - 2 = 18$$

$$\Rightarrow x + \frac{1}{x} = 20$$

Squaring both side

$$\Rightarrow x^2 + \frac{1}{x^2} + 2 = 400$$

$$\Rightarrow x^2 + \frac{1}{x^2} = 398$$

**56. (B)**

$$\begin{aligned} a^3 - b^3 &= (a-b)^3 + 3ab(a-b) \\ &= 64 + 3(2)(4) \\ &= 64 + 24 \rightarrow 88 \end{aligned}$$

57. (C)  $\sqrt{x} - \frac{1}{\sqrt{x}} = \sqrt{5}$

Squaring both sides

$$x + \frac{1}{x} = 7$$

Again squaring both sides

$$x^2 + \frac{1}{x^2} = 49$$

58. (C)  $a + b + c = 8$   
 $ab + bc + ca = 20$

$$\begin{aligned} a^3 + b^3 + c^3 - 3abc &= (a+b+c)[(a+b+c)^2 - 3(ab+bc+ca)] \\ a^3 + b^3 + c^3 - 3abc &= (8)(64 - 3(20)) \\ &= 8 + 4 = 32 \end{aligned}$$

59. (B)  $\sqrt{x} + \frac{1}{\sqrt{x}} = \sqrt{6}$

$$x + \frac{1}{x} = 4$$

$$x^2 + \frac{1}{x^2} = 14$$

60. (B) As we know,

$$\begin{aligned} a^3 + b^3 + c^3 - 3abc &= (a + b + c)((a^2 + b^2 + c^2) - 3(ab + bc + ca)) \\ a^3 + b^3 + c^3 - 3abc &= 10(10^2 - 3 \times 32) \\ &= 10(100 - 96) \\ &= 40 \end{aligned}$$

61. (D) Put  $a = 6, b = 1$

$$\begin{aligned} 6^3 - 1^3 &= 216 - 1 \\ &= 215 \end{aligned}$$

62. (A) As we know,

$$x^3 + \frac{1}{x^3} = \left(x + \frac{1}{x}\right)^3 - 3\left(x + \frac{1}{x}\right)$$

$$x + \frac{1}{x} = 5$$

$$x^3 + \frac{1}{x^3} = (5)^3 - 3(5)$$

$$= 125 - 15 = 110$$

63. (B) Here  $a^3 + b^3 + c^3 - 3abc = 0$

$$\Rightarrow a + b + c = 0$$

$$\text{here, } a = x - 5$$

$$b = x - 6$$

$$c = x - 7$$

$$\Rightarrow x - 5 + x - 6 + x - 7 = 0$$

$$\Rightarrow 3x - 18 = 0$$

$$\Rightarrow x = 6$$

64. (C) Put  $a = 6, b = 2$

$$\Rightarrow (8)^2 - 6 \times 2 \rightarrow 64 - 12$$

$$\Rightarrow 52$$

# **ALGEBRA**

(SSC CGL (PRE) - 2018)

## बीजगणित

### **(Previous Year Questions)**

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- 10.** If  $(x - 2)^2 + (y + 3)^2 + (z - 15)^2 = 0$ , then what is the value of  $x + y + z - 5$ ?  
यदि  $(x - 2)^2 + (y + 3)^2 + (z - 15)^2 = 0$  है, तो  $x + y + z - 5$  का मान क्या है?  
(A) 5 (B) 9  
(C) 15 (D) 20

**11.** If  $a^3 + b^3 = 28$  and  $a + b = 4$ , then what is the value of  $ab$ ?  
यदि  $a^3 + b^3 = 28$  और  $a + b = 4$  है, तो  $ab$  का मान क्या है?  
(A) -3 (B) 2  
(C) 8 (D) 3

**12.** If  $x + \left(\frac{1}{x}\right) = 2$ , then what is the value of  $x^{64} + \frac{1}{x^{121}}$ ?  
यदि  $x + \left(\frac{1}{x}\right) = 2$ , तो  $x^{64} + \frac{1}{x^{121}}$  का मान क्या होगा?  
(A) 0 (B) 1  
(C) 2 (D) -2

**13.** If  $x = 6 + 2\sqrt{6}$ , then what is the value of  $\sqrt{x-1} + \frac{1}{\sqrt{x-1}}$ ?  
यदि  $x = 6 + 2\sqrt{6}$ , तो  $\sqrt{x-1} + \frac{1}{\sqrt{x-1}}$  का मान क्या है?  
(A)  $2\sqrt{3}$  (B)  $3\sqrt{2}$   
(C)  $2\sqrt{2}$  (D)  $3\sqrt{3}$

**14.** If  $a + b + c = 27$ , then what is the value of  $(a - 7)^3 + (b - 9)^3 + (c - 11)^3 - 3(a - 7)(b - 9)(c - 11)$ ?  
यदि  $a + b + c = 27$ ,  $(a - 7)^3 + (b - 9)^3 + (c - 11)^3 - 3(a - 7)(b - 9)(c - 11)$  का मान क्या है?  
(A) 0 (B) 9  
(C) 27 (D) 81

**15.** If  $(x^2/yz) + (y^2/zx) + (z^2/xy) = 3$ , then what is the value of  $(x + y + z)^3$ ?  
यदि  $(x^2/yz) + (y^2/zx) + (z^2/xy) = 3$  है, तो  $(x + y + z)^3$  का मान क्या होगा?  
(A) 0 (B) 1  
(C) 2 (D) 3

**16.** If  $x^{1/4} + x^{-1/4} = 2$ , then what is the value of  $x^{81} + \frac{1}{x^{81}}$ ?  
यदि  $x^{1/4} + x^{-1/4} = 2$  है, तो  $x^{81} + \frac{1}{x^{81}}$  का मान क्या होगा?  
(A) -2 (B) 0  
(C) 1 (D) 2

**17.** If  $a(a + b + c) = 45$ ,  $b(a + b + c) = 75$  and  $c(a + b + c) = 105$ , then what is the value of  $(a^2 + b^2 + c^2)$ ?  
यदि  $a(a + b + c) = 45$ ,  $b(a + b + c) = 75$  तथा  $c(a + b + c) = 105$  है, तो  $(a^2 + b^2 + c^2)$  का मान क्या होगा?  
(A) 75 (B) 83  
(C) 217 (D) 225

**18.** If  $x^2 + \frac{1}{x^2} = 1$ , then what is the value of  $x^{18} + x^{12} + x^{36} + x^{24} + x^{18} + x^{12} + x^6 + 1$ ?  
यदि  $x^2 + \frac{1}{x^2} = 1$  है, तो  $x^{48} + x^{42} + x^{36} + x^{30} + x^{24} + x^{18} + x^{12} + x^6 + 1$  का मान क्या होगा?  
(A) -9 (B) 0  
(C) 1 (D) 9

**19.** If  $\frac{11-13x}{x} + \frac{11-13y}{y} + \frac{11-13z}{z} = 5$ , then what is the value of  $\frac{1}{x} + \frac{1}{y} + \frac{1}{z}$ ?  
यदि  $\frac{11-13x}{x} + \frac{11-13y}{y} + \frac{11-13z}{z} = 5$  है, तो  $\frac{1}{x} + \frac{1}{y} + \frac{1}{z}$  का मान क्या है?  
(A) 1 (B)  $13/11$   
(C)  $13/5$  (D) 4

**20.** If  $2x + (9/x) = 9$ , then what is the minimum value of  $x^2 + (1/x^2)$ ?  
यदि  $2x + (9/x) = 9$ , तो  $x^2 + (1/x^2)$  का न्यूनतम मान क्या होगा?  
(A)  $95/36$  (B)  $97/36$   
(C)  $86/25$  (D)  $623/27$

**21.** If  $(5x - y)/(5x + y) = 3/7$ , then what is the value of  $(4x^2 + y^2 - 4xy)/(9x^2 + 16y^2 + 24xy)$ ?  
यदि  $(5x - y)/(5x + y) = 3/7$ , तो  $(4x^2 + y^2 - 4xy)/(9x^2 + 16y^2 + 24xy)$  का मान क्या होगा?  
(A) 0 (B)  $3/7$   
(C)  $18/49$  (D)  $1/6$

**22.** If  $(x + y)^2 = xy + 1$  and  $x^3 - y^3 = 1$ , then what is the value of  $x - y$ ?  
यदि  $(x + y)^2 = xy + 1$  तथा  $x^3 - y^3 = 1$ , तो  $x - y$  का मान क्या होगा?  
(A) 1 (B) 0  
(C) -1 (D) 2

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23. If  $(x - 2)$  and  $(x + 3)$  are the factors of the equation  $x^2 + k_1x + k_2 = 0$ , then what are the values of  $k_1$  and  $k_2$ ?  
यदि समीकरण  $x^2 + k_1x + k_2 = 0$  के गुणनखण्ड  $(x - 2)$  तथा  $(x + 3)$  हैं, तो  $k_1$  तथा  $k_2$  का मान क्या है ?  
(A)  $k_1 = 6, k_2 = -1$       (B)  $k_1 = 1, k_2 = -6$   
(C)  $k_1 = 1, k_2 = 6$       (D)  $k_1 = -6, k_2 = 1$
24. If  $(x - y) = 7$ , then what is the value of  $(x - 15)^3 - (y - 8)^3$ ?  
यदि  $(x - y) = 7$  हो, तो  $(x - 15)^3 - (y - 8)^3$  का मान क्या है ?  
(A) 0      (B) 343  
(C) 392      (D) 2863
25. The value of  $\sqrt{-\sqrt{3} + \sqrt{3 + 8\sqrt{7 + 4\sqrt{3}}}}$ .  
 $\sqrt{-\sqrt{3} + \sqrt{3 + 8\sqrt{7 + 4\sqrt{3}}}}$  का मान क्या होगा ?  
(A) 2      (B) 3  
(C)  $\sqrt{2}$       (D)  $2\sqrt{3}$
26. If  $p/q = r/s = t/u = \sqrt{5}$ , then what is the value of  $[(3p^2 + 4r^2 + 5t^2)/(3q^2 + 4s^2 + 5u^2)]$ ?  
यदि  $p/q = r/s = t/u = \sqrt{5}$  हो, तो  $[(3p^2 + 4r^2 + 5t^2)/(3q^2 + 4s^2 + 5u^2)]$  का मान क्या है ?  
(A)  $1/5$       (B) 5  
(C) 25      (D) 60
27. If  $(1/x) + (1/y) + (1/z) = 0$  and  $x + y + z = 9$ , then what is the value of  $x^3 + y^3 + z^3 - 3xyz$ ?  
यदि  $(1/x) + (1/y) + (1/z) = 0$  तथा  $x + y + z = 9$  है, तो  $x^3 + y^3 + z^3 - 3xyz$  का मान क्या होगा ?  
(A) 81      (B) 361  
(C) 729      (D) 6561
28. If  $x^4 + (1/x^4) = 34$ , then what is the value of  $x^3 - (1/x^3)$ ?  
यदि  $x^4 + (1/x^4) = 34$ , तो  $x^3 - (1/x^3)$  का मान क्या होगा ?  
(A) 0      (B) 6  
(C) 8      (D) 14
29. If  $x = 1 - y$  and  $x^2 = 2 - y^2$ , then what is the value of  $xy$ ?  
यदि  $x = 1 - y$  तथा  $x^2 = 2 - y^2$ , तो  $xy$  का मान क्या होगा ?  
(A) 1      (B) 2  
(C)  $-1/2$       (D)  $-1$
30. If  $x + [1/(x + 7)] = 0$ , then what is the value of  $x - [1/(x + 7)]$ ?  
यदि  $x + [1/(x + 7)] = 0$  है, तो  $x - [1/(x + 7)]$  का मान क्या होगा ?  
(A)  $3\sqrt{5}$       (B)  $3\sqrt{5} - 7$   
(C)  $3\sqrt{5} + 7$       (D) 8
31. If  $4^{(x+y)} = 256$  and  $(256)^{(x-y)} = 4$ , then what is the value of  $x$  and  $y$ ?  
यदि  $4^{(x+y)} = 256$  तथा  $(256)^{(x-y)} = 4$  है, तो,  $x$  तथा  $y$  का मान क्या होगा ?  
(A)  $17/8, 15/8$       (B)  $17/4, 15/4$   
(C)  $9/17, 15/17$       (D)  $8/17, 8/15$
32. If the expression  $px^3 - qx^2 - 7x - 6$  is completely divisible by  $x^2 - x - 6$ , then what is the value of  $p$  and  $q$  respectively?  
यदि व्यंजक  $px^3 - qx^2 - 7x - 6$ ,  $x^2 - x - 6$  से पूर्णतः विभाजित होता है, तो क्रमशः  $p$  तथा  $q$  का मान क्या है ?  
(A) 0, 1      (B) 1, 0      (C) 2, 1      (D) 1, 2
33. If the expression  $px^3 - 2x^2 - qx + 18$  is completely divisible by  $(x^2 - 9)$ , then what is the ratio between  $p$  and  $q$  respectively?  
यदि व्यंजक  $px^3 - 2x^2 - qx + 18$ ,  $(x^2 - 9)$  से पूर्णतः विभाजित है, तो क्रमशः  $p$  तथा  $q$  के बीच का अनुपात क्या होगा ?  
(A) 1:9      (B) 1:3      (C) 3:1      (D) 9:1
34. If  $x + \frac{1}{x} = 5$ , then what is the value of  $x^5 + \frac{1}{x^5}$ ?  
यदि  $x + \frac{1}{x} = 5$ , तो  $x^5 + \frac{1}{x^5}$  का मान क्या है ?  
(A) 1875      (B) 2525  
(C) 2530      (D) 3120
35. If  $(x/y)^{a+4} = (y/x)^{2a-5}$ , then what is the relation between  $x$  and  $y$ ?  
यदि  $(x/y)^{a+4} = (y/x)^{2a-5}$  है, तो  $x$  तथा  $y$  के बीच क्या संबंध होगा ?  
(A)  $x > y$   
(B) Cannot be determined/ज्ञात नहीं किया जा सकता  
(C)  $x < y$   
(D)  $x = y$
36. If  $3a - (3/a) - 3 = 0$ , then what is the value of  $a^3 - (1/a^3) + 2$ ?  
यदि  $3a - (3/a) - 3 = 0$  है, तो  $a^3 - (1/a^3) + 2$  का मान क्या है ?  
(A) 0      (B) 2  
(C) 4      (D) 6

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37.  $5(x^2 + y^2 + z^2) = 4(xy + yz + zx)$  then  $x + y + z = ?$   
 $5(x^2 + y^2 + z^2) = 4(xy + yz + zx)$  है, तो  $x + y + z = ?$   
 (A) 1 (B) 0  
 (C) 5 (D) 4
38. If  $x^3 + 2x^2 - 5x + k$  is divisible by  $x + 1$ , then what is the value of  $k$ ?  
 यदि  $x^3 + 2x^2 - 5x + k$ ,  $x + 1$  से विभाजित होता है, तो  $K$  का मान क्या है?  
 (A) -6 (B) -1  
 (C) 0 (D) 6
39. If  $3x + [1/(5x)] = 7$ , then what is the value of  $5x/(15x^2 + 15x + 1)$ ?  
 यदि  $3x + [1/(5x)] = 7$  तो  $5x/(15x^2 + 15x + 1)$  का मान क्या होगा?  
 (A)  $1/5$  (B)  $1/10$   
 (C)  $2/5$  (D) 10
40. If  $x + [1/(4x)] = 5/2$ , then what is the value of  $(64x^6 + 1)/8x^3$ ?  
 यदि  $x + [1/(4x)] = 5/2$  तो  $(64x^6 + 1)/8x^3$  का मान क्या होगा?  
 (A) 110 (B) 115  
 (C) 125 (D) 140
41. If  $x^2 + x = 19$ , then what is the value of  $(x + 5) + [1/(x + 5)]$ ?  
 यदि  $x^2 + x = 19$  है, तो  $(x + 5) + [1/(x + 5)]$  का मान क्या होगा?  
 (A) 7 (B) 9  
 (C) 8 (D) 3
42. If  $\frac{a}{1-a} + \frac{b}{1-b} + \frac{c}{1-c} = 2$  than what is the value of  $\frac{1}{1-a} + \frac{1}{1-b} + \frac{1}{1-c} = ?$   
 यदि  $\frac{a}{1-a} + \frac{b}{1-b} + \frac{c}{1-c}$  तो  $\frac{1}{1-a} + \frac{1}{1-b} + \frac{1}{1-c}$  का मान क्या होगा?  
 (A) 0 (B) 5  
 (C) -5 (D) 1
43. If  $\alpha$  and  $\beta$  are roots of the equation  $3x^2 - 13x + 14 = 0$ , then what is the value of  $(\alpha/\beta) + (\beta/\alpha)$ ?  
 यदि  $\alpha$  तथा  $\beta$  हैं, तो व्यंजक  $3x^2 - 13x + 14 = 0$ , तो  $(\alpha/\beta) + (\beta/\alpha)$  का मान क्या है?  
 (A)  $65/28$  (B)  $53/14$   
 (C) 9 (D)  $85/42$
44. If  $a + b + c = 9$  and  $ab + bc + ca = 18$ , then what is the value of  $a^3 + b^3 + c^3 - 3abc$ ?  
 यदि  $a + b + c = 9$  तथा  $ab + bc + ca = 18$ , तो  $a^3 + b^3 + c^3 - 3abc$  का मान क्या है?  
 (A) 189 (B) 243  
 (C) 361 (D) 486
45. If  $(x/y) + (y/x) = 1$ , then what is the value of  $x^3 + y^3$ ?  
 यदि  $(x/y) + (y/x) = 1$  है, तो  $x^3 + y^3$  का मान क्या है?  
 (A) -1 (B) 0  
 (C) 1 (D) 3
46. If  $5^x = 30^y = 6^z$ , then what is the value of  $(xy + yz + zx)/xyz$ ?  
 यदि  $5^x = 30^y = 6^z$  तो  $(xy + yz + zx)/xyz$  का मान क्या है?  
 (A) 0 (B) 1 (C) 2 (D) 3
47. What is the value of  $\frac{1}{x^{(p-q)}+1} + \frac{1}{x^{(q-p)}+1}$ ?  
 $\frac{1}{x^{(p-q)}+1} + \frac{1}{x^{(q-p)}+1}$  का मान क्या है?  
 (A) 0 (B) 1  
 (C)  $x^{(p-q)}$  (D)  $x^{(q-p)}$
48. If  $x = 8 + 2\sqrt{15}$ , then what is the value of  $\sqrt{x} + \frac{1}{\sqrt{x}}$ ?  
 यदि  $x = 8 + 2\sqrt{15}$  तो  $\sqrt{x} + \frac{1}{\sqrt{x}}$  का मान क्या है?  
 (A)  $2\sqrt{5}$  (B)  $2\sqrt{3}$   
 (C)  $(3\sqrt{5} + \sqrt{3})/2$  (D)  $(3\sqrt{3} - \sqrt{5})/2$
49. What is the value of  $\frac{1+a}{a^{1/2}+a^{-1/2}} - \frac{a^{1/2}+a^{-1/2}}{1+a} + a^{-1/2}$ ?  
 $\frac{1+a}{a^{1/2}+a^{-1/2}} - \frac{a^{1/2}+a^{-1/2}}{1+a} + a^{-1/2}$  का मान क्या है?  
 (A)  $\sqrt{a}$  (B)  $1/\sqrt{a}$   
 (C)  $\sqrt{a} + 1$  (D)  $\sqrt{a} - 1$
50. If  $\frac{p}{q} = \frac{x+3}{x-3}$ , then what is the value of  $\frac{p^2+q^2}{p^2-q^2}$ ?  
 यदि  $\frac{p}{q} = \frac{x+3}{x-3}$  तो  $\frac{p^2+q^2}{p^2-q^2}$  का मान क्या है?  
 (A)  $\frac{x^2+9}{3x}$  (B)  $\frac{x^2+18}{6x}$  (C)  $\frac{x^2+18}{3x}$  (D)  $\frac{x^2+9}{6x}$

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## Solution

1. (A)  $\frac{2+\sqrt{3}}{2-\sqrt{3}} \times \frac{2+\sqrt{3}}{2+\sqrt{3}} \Rightarrow 7 + 4\sqrt{3}$

$$\frac{1}{x} = 7 - 4\sqrt{3}$$

A. T. Q.  $x + \frac{1}{x} = 7 + 4\sqrt{3} + 7 - 4\sqrt{3} = 14$

2. (C)  $x = 2 + \sqrt{3} \Rightarrow \sqrt{2x} + \frac{1}{\sqrt{2x}}$

$$\sqrt{4+2\sqrt{3}} + \frac{1}{\sqrt{4+2\sqrt{3}}} \Rightarrow \sqrt{(\sqrt{3}+1)^2} + \frac{1}{\sqrt{(\sqrt{3}+1)^2}}$$

$$= (\sqrt{3}+1) + \frac{1}{(\sqrt{3}+1)} = \frac{3\sqrt{3}+1}{2}$$

3. (D)  $x + \frac{1}{x} = 4$

$$x^3 + \frac{1}{x^3} = \left(x + \frac{1}{x}\right)^3 - 3\left(x + \frac{1}{x}\right)$$

$$x^3 + \frac{1}{x^3} = 4^3 - 3 \times 4$$

$$x^3 + \frac{1}{x^3} = 64 - 12$$

$$x^3 + \frac{1}{x^3} = 52$$

A.T.Q.  $\left(x^3 + \frac{1}{x^3}\right)^2 = x^6 + \frac{1}{x^6} + 2$

$$52 \times 52 = x^6 + \frac{1}{x^6} + 2$$

$$2704 = x^6 + \frac{1}{x^6} + 2$$

$$x^6 + \frac{1}{x^6} = 2702$$

4. (C)  $\frac{1}{1+y} + \frac{2y+1}{y^2-1} \Rightarrow$

$$\frac{y-1}{(y+1)(y-1)} + \frac{2y+1}{(y+1)(y-1)}$$

$$\frac{3y}{(y+1)(y-1)} \Rightarrow \frac{3\left[\frac{2-x}{1+x}\right]}{\left(\frac{2-x}{1+x}+1\right)\left(\frac{2-x}{1+x}-1\right)} \\ = \frac{(2-x)(1+x)}{(1-2x)}$$

5. (B)  $x^2 - 8x + 15 = 0 : y^2 + 2y - 35 = 0$   
 $x^2 - 5x - 3x + 15 = 0 : y^2 + 7y - 5y - 35 = 0$   
 $x(x-5) - 3(x-5) = 0 : y(y+7) - 5(y+7) = 0$   
 $(x-3)(x-5) = 0 : (y+7)(y-5) = 0$   
 $x = 3, 5 : y = 5, -7$   
 Common root is 5 so difference of its cube and square will be  
 $5^3 - 5^2 = 125 - 25 = 100$

6. (B)  $\left(x - \frac{1}{3}\right)^2 + (y-4)^2 = 0$  then  $\frac{y+x}{y-x}$   
 Since  $x = \frac{1}{3}$ ,  $y = 4$   
 then,  $\frac{y+x}{y-x} = \frac{4+\frac{1}{3}}{4-\frac{1}{3}} = \frac{13}{11}$

7. (D) Expression is  $x^2 + \frac{1}{x^2} - 6$

then its later  $\left(x^2 + \frac{1}{x^2} - 2\right) - 4$

$$= \left(x + \frac{1}{x}\right)^2 - 4 = \left(x + \frac{1}{x}\right)^2 - (2)^2$$

$$= \left(x + \frac{1}{x} + 2\right) \left(x + \frac{1}{x} - 2\right)$$

Difference between factors

$$\left(x + \frac{1}{x} + 2\right) - \left(x + \frac{1}{x} - 2\right) = 4 \text{ Ans}$$

8. (C)  $x + \frac{1}{x} = \sqrt{13}$  so  $x - \frac{1}{x} = 3$

$$x^5 + \frac{1}{x^5} = \left[x^3 + \frac{1}{x^3}\right] \times \left[x^2 - \frac{1}{x^2}\right] - \left[x - \frac{1}{x}\right]$$

$$x - \frac{1}{x} = 3 \text{ then } x^3 - \frac{1}{x^3} = 36$$

$$x^2 - \frac{1}{x^2} = 11$$

$$x^5 - \frac{1}{x^5} = 36 \times 11 - 3 = 396 - 3 \\ = x^5 - \frac{1}{5} = 393$$

9. (A)  $a^3 + b^3 = 35$ ,  $ab = 6$ ,  $(a+b) = ?$   
 $(a+b)^3 = a^3 + b^3 + 3ab(a+b)$   
 $(a+b)^3 = 35 + 3(6)(a+b)$   
 $(a+b) = 5$

10. (B)  $(x-2)^2 + (y+3)^2 + (z-15)^2 = 0$   
 $x = 2, y = -3, z = 15$   
 $\Rightarrow 2-3+15-5=9$

11. (D)  $(a+b)^3 = a^3 + b^3 + 3ab(a+b)$   
 $(4)^3 = 28 + 3ab \times 4$   
 $64 = 28 + 12ab$   
 $36 = 12ab$   
 $ab = 3$

12. (C)  $x + \frac{1}{x} = 2$   
 $x^2 - 2x + 1 = 0$   
 $x = 1$

then  $x^{64} + \frac{1}{x^{121}} = 1 + 1 = 2$

13. (A)  $x-1 = 6 + 2\sqrt{6} - 1$   
 $= 5 + 2\sqrt{6}$   
 $= (\sqrt{3} + \sqrt{2})^2$   
 $\sqrt{x-1} = \sqrt{3} + \sqrt{2}$   
 $\frac{1}{\sqrt{x-1}} = \sqrt{3} - \sqrt{2}$   
 $\sqrt{x-1} + \frac{1}{\sqrt{x-1}} = 2\sqrt{3}$

14. (A) If  $a + b + c = 0$   
then  $a^3 + b^3 + c^3 - 3abc = 0$   
 $a^3 + b^3 + c^3 - 3abc = 0$

15. (A)  $\frac{x^2}{yz} + \frac{y^2}{zx} + \frac{z^2}{xy} = 3$

$$\Rightarrow \frac{x^3 + y^3 + z^3}{xyz} = 3$$

$$\Rightarrow x^3 + y^3 + z^3 = 3xyz$$
 $ie. (x+y+z) = 0$ 
 $\therefore (x+y+z)^3 = 0$

16. (D)  $x^{\frac{1}{4}} + \frac{1}{x^{\frac{1}{4}}} = 2$   $x = 1$

$$x^{81} + \frac{1}{x^{81}} = 2$$

17. (B)  $a(a+b+c) = 45$   
 $b(a+b+c) = 75$   
 $c(a+b+c) = 105$   
 $(a^2 + b^2 + c^2) = ?$   
Let  $a+b+c = K$

$$a = \frac{45}{k}, b = \frac{75}{k}, c = \frac{105}{k}$$

$$(a+b+c) = \frac{45}{k} + \frac{75}{k} + \frac{105}{k}$$

$$\Rightarrow k^2 = 225$$

$$\Rightarrow k = 15$$

$$a = 3, b = 5, c = 7$$

$$\Rightarrow (a^2 + b^2 + c^2) = (9 + 25 + 49) = 83$$

18. (C)  $x^2 + \frac{1}{x^2} = 1 \Rightarrow x + \frac{1}{x} = \sqrt{3}$

$$\Rightarrow x^6 = -1$$

$$x^{48} + x^{42} + x^{36} + x^{30} + x^{24} + x^{18} + x^{12} + x^6 + 1 = ?$$

$$\Rightarrow 1 + x^6 + 0 + 0 + 0 + 1$$

$$= 2 - 1$$

$$= 1$$

19. (D)  $\frac{11}{x} + \frac{11}{y} + \frac{11}{z} = 44$

$$11 \left( \frac{1}{x} + \frac{1}{y} + \frac{1}{z} \right) = 44$$

$$\frac{1}{x} + \frac{1}{y} + \frac{1}{z} = \frac{44}{11} \Rightarrow \frac{1}{x} + \frac{1}{y} + \frac{1}{z} = 4$$

20. (B)  $2x^2 - 9x + 9 = 0$   
 $2x^2 - 6x - 3x + 9 = 0$   
 $2x(x-3) - 3(x-3) = 0$

$$x = \frac{3}{2}, 3$$

Minimum value of  $x^2 + \frac{1}{x^2}$

$$= \left(\frac{3}{2}\right)^2 + \left(\frac{2}{3}\right)^2 = \frac{97}{36}$$

21. (A)  $\frac{5x-y}{5x+y} = \frac{3}{7}$

Let, Hit & Trial  $x = 1$ ;  $y = 2$

$$\frac{4x^2 + y^2 - 4xy}{9x^2 + 16y^2 + 24xy} \Rightarrow \frac{4(1)^2 + (2)^2 - 4 \times 1 \times 2}{9(1)^2 + 16(2)^2 + 24 \times 1 \times 2}$$

$$= \frac{8 - 8}{9 + 64 + 48} = \frac{0}{121} = 0$$

22. (A)  $\Rightarrow (x+y)^2 = xy + 1$

$$\Rightarrow x^2 + y^2 + xy = 1$$

$$x^3 - y^3 = 1 \quad (\because x^3 - y^3 = (x-y)(x^2 + y^2 + xy))$$

$$(x-y)(x^2 + y^2 + xy) = 1$$

$$(x-y) = 1$$

23. (B)  $x^2 + k_1 x + k_2$

factors  $(x-2)$  &  $(x+3)$

$$\Rightarrow x = 2$$

$$4 + 2k_1 + k_2 = 0 \quad \dots \text{(i)} \times 3$$

$$x = -3$$

$$9 - 3k_1 + k_2 = 0 \quad \dots \text{(ii)} \times 2$$

$$12 + 6k_1 + 3k_2 = 0$$

$$18 - 6k_1 + 2k_2 = 0$$

$$5k_2 = -30$$

$$k_2 = -6$$

$$k_1 = 1$$

24. (A)  $(x-y) = 7 \quad \dots \text{(1)}$

$$(x-15)^3 - (y-8)^3 = ?$$

First value for  $(x-15) - (y-8)$

$$x - 15 - y + 8$$

$$= x - y = 7$$

$$= 0$$

$$\text{i.e. } (x-15) - (y-8) = 0$$

25. (A)  $\sqrt{-\sqrt{3} + \sqrt{3 + 8\sqrt{7 + 4\sqrt{3}}}}$

$$= \sqrt{-\sqrt{3} + \sqrt{3 + 8\sqrt{4 + 3\sqrt{12}}}}$$

$$= \sqrt{-\sqrt{3} + \sqrt{3 + 8(2 + \sqrt{3})}}$$

$$= \sqrt{-\sqrt{3} + \sqrt{3 + 16 + 2\sqrt{48}}} = \sqrt{-\sqrt{3} + \sqrt{16 + \sqrt{3}}}$$

$$= \sqrt{\sqrt{16}} = \sqrt{4} = 2$$

26. (B)  $\frac{p}{q} = \frac{r}{s} = \frac{t}{u} = \sqrt{5}$

$$p = \sqrt{5}q$$

$$r = \sqrt{5}s$$

$$t = \sqrt{5}u$$

$$= \frac{3p^2 + 4r^2 + 5t^2}{3q^2 + 4s^2 + 5u^2}$$

using above relations

$$= \frac{3.5.q^2 + 4.5.s^2 + 5.5.u^2}{3q^2 + 4s^2 + 5u^2}$$

$$= 5 \frac{(3q^2 + 4s^2 + 5u^2)}{(3q^2 + 4s^2 + 5u^2)} = 5$$

27. (C)  $\frac{1}{x} + \frac{1}{y} + \frac{1}{z} = 0$

$$xy + yz + xz = 0$$

$$x + y + z = 9$$

$$(x + y + z)^2 = 81$$

$$\Rightarrow x^2 + y^2 + z^2 + 2(xy + yz + zx) = 81$$

$$\Rightarrow x^2 + y^2 + z^2 = 81$$

$$\Rightarrow x^3 + y^3 + z^3 - 3xyz$$

$$= (x + y + z)[x^2 + y^2 + z^2 - xy - yz - zx]$$

$$= 9 \times (81 - 0)$$

$$= 729$$

28. (D)  $x^4 + \frac{1}{x^4} = 34$

$$(x^2)^2 + \left(\frac{1}{x^2}\right)^2 + 2 = 36$$

$$= \left(x^2 + \frac{1}{x^2}\right)^2 = (6)^2$$

$$= x^2 + \frac{1}{x^2} = 6$$

Again

$$\Rightarrow x^2 + \frac{1}{x^2} - 2 = 6 - 2$$

$$\Rightarrow \left(x - \frac{1}{x}\right)^2 = 4 \Rightarrow x - \frac{1}{x} = 2$$

$$\Rightarrow x^3 - \frac{1}{x^3} = 2^3 + 3.2$$

$$= 8 + 6 = 14$$

29. (C)  $x = 1 - y$

$$\Rightarrow x + y = 1$$

$$\Rightarrow x^2 + y^2 + 2xy = 1 \quad \dots \text{(ii)}$$

$$\Rightarrow x^2 + y^2 = 2 \quad \dots \text{(i)}$$

$$\text{(ii)} - \text{(i)}$$

$$2xy = -1$$

$$xy = -\frac{1}{2}$$

30. (B)  $x + \frac{1}{x+7} = 0$

$$\begin{aligned} x &= -\frac{1}{x+7} \\ x^2 + 7x + 1 &= 0 \\ x &= \frac{-7 \pm \sqrt{49-4}}{2} \\ x &= \frac{-7 \pm 3\sqrt{5}}{2} \end{aligned}$$

.... (1)

$$\begin{aligned} x &= \frac{1}{x+7} \\ &= \frac{-2}{x+7} \\ &= \frac{-2}{-7 \pm 3\sqrt{5} + 7} = \frac{-2}{-7 \pm 3\sqrt{5} + 14} = \frac{-2 \times 2}{3\sqrt{5} + 7} \end{aligned}$$

Expression  $\pm 3\sqrt{5}$  की +ve Value लेकर

$$\begin{aligned} &= \frac{-4}{(3\sqrt{5} + 7)} \times \frac{(3\sqrt{5} - 7)}{(3\sqrt{5} - 7)} = \frac{-4(3\sqrt{5} - 7)}{-4} \\ &= 3\sqrt{5} - 7 \end{aligned}$$

31. (A)  $(4)^{x+y} = 256$

$(4)^{x+y} = 4^4$

$x + y = 4$

.... (i)

$4^{4(x-y)} = 4$

$4^{(x-y)} = 1$

$x - y = \frac{1}{4}$  .... (ii)

(i) + (ii)

$2x = \frac{17}{4}$

$x = \frac{17}{8}; y = \frac{15}{8}$

32. (B)  $px^3 - qx^2 - 7x - 6$  .... (i)

$x^2 - x - 6$  ये पूर्णतः विभाजित है।

$\Rightarrow x^2 - 3x + 2x - 6$

$\Rightarrow (x-3)(x+2)$

$\Rightarrow x = 3, -2$

Use it in eqn (i)

$27p - 9q - 21 - 6 = 0$

$27p - 9q = 27$

$9p - 3q = 9$  .... (ii)

$-8p - 4q + 14 - 6 = 0$

$-8p - 4q = -8$

$2p + q = 2$  .... (iii)  $\times 3$

$6p + 3q = 6$  .... (ii) + (iii)

$15p = 15$

$p = 1$

$q = 0$

33. (A)  $px^3 - 2x^2 - qx + 18$

$x^2 - 9 = 0$

$x = \pm 3$

$\Rightarrow 27p - 18 - 3q + 18 = 0$

$\Rightarrow 27p = 3q$

$\Rightarrow \frac{p}{q} = \frac{3}{27} = \frac{1}{9}$

$\Rightarrow p : q = 1 : 9$

34. (B)  $x + \frac{1}{x} = 5 ; x^5 + \frac{1}{x^5} = ?$

$\left(x^2 + \frac{1}{x^2}\right) = 23$

$\left(x^3 + \frac{1}{x^3}\right) = 110$

$$\begin{aligned} x^5 + \frac{1}{x^5} &= \left(x^2 + \frac{1}{x^2}\right)\left(x^3 + \frac{1}{x^3}\right) - \left(x + \frac{1}{x}\right) \\ &= 110 \times 23 - 5 \\ &= 2525 \end{aligned}$$

35. (D)  $\left(\frac{x}{y}\right)^{a-4} = \left(\frac{y}{x}\right)^{2a-5}$

$= x^{a-4} \cdot x^{2a-5} = y^{2a-5} \cdot y^{a-4}$

$= x^{3a-9} = y^{3a-9}$

$x = y$

36. (D)  $3a - \frac{3}{a} - 3 = 0$

$3a - \frac{3}{a} = 3; a - \frac{1}{a} = 1$

$a^3 - \frac{1}{a^3} = 1 + 3 \times 1 = 4$

so  $a^3 - \frac{1}{a^3} + 2 = 4 + 2 = 6$

37. (B)  $5(x^2 + y^2 + z^2) = 4(xy + yz + zx)$

$4x^2 - 4xy + y^2 + 4y^2 - 4yz + z^2 + 4z^2 - 4zx + x^2 = 0$

$(2x-y)^2 + (2y-z)^2 + (2z-x)^2 = 0$

$2x - y = 0, 2y - z = 0, 2z - x = 0$

On adding  $x + y + z = 0$

38. (A)  $x^3 + 2x^2 - 5x + k, x + 1$  से विभाजित है।

$\therefore x = -1$  रखने पर  $= -1 + 2 + 5 + k = 0$

$k + 6 = 0$

$k = -6$

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39.(B)  $3x + \frac{1}{5x} = 7$   
 $15x^2 + 1 = 35x$  ..... (1)

then  $\frac{5x}{15x^2 + 15x + 1}$  from (1)

$$\frac{5x}{35x + 15x}$$

$$\frac{5x}{50x} = \frac{1}{10}$$

40.(A)  $x + \frac{1}{4x} = \frac{5}{2}$

$$\Rightarrow 2x + \frac{1}{2x} = 5$$

$$\Rightarrow 8x^3 + \frac{1}{8x^3} = (5)^3 - 3 \times 5$$

$$= 125 - 15 = 110$$

$$\left( \frac{64x^6 + 1}{8x^3} \right) = 110$$

41. (B)  $x^2 + x = 19$  then  $(x + 5) + \frac{1}{x+5} = ?$

from (1)  $(y - 5)^2 + y - 5 = 19$  Let  $x + 5 = y$   
 $y^2 + 25 - 10y + y - 5 = 19$

then  $x = y - 5$ .... (1)

$$y^2 - 9y = -1$$

$$y + \frac{1}{y} = 9$$

Put the value of  $y = (x + 5) + \frac{1}{(x+5)} = 9$

42. (B)  $\frac{a}{1-a} + \frac{b}{1-b} + \frac{c}{1-c} = 2$

$$\frac{a}{1-a} + 1 + \frac{b}{1-b} + \frac{c}{1-c} + 1 = 2 + 3$$

$$\frac{1}{1-a} + \frac{1}{1-b} + \frac{1}{1-c} = 5$$

43. (D)  $3x^2 - 13x + 14 = 0$

$\alpha$  and  $\beta$  are the roots of this eq.  
 then

$$\alpha + \beta = \frac{13}{3}; \quad \alpha \times \beta = \frac{14}{3}$$

$$\frac{\alpha}{\beta} + \frac{\beta}{\alpha} = \frac{\alpha^2 + \beta^2}{\alpha\beta}$$

$$= \frac{(\alpha + \beta)^2 - 2\alpha\beta}{\alpha\beta} = \frac{\left(\frac{13}{3}\right)^2 - 2 \times \frac{14}{3}}{\frac{14}{3}} = \frac{85}{42}$$

44. (B)  $a + b + c = 9$   
 $ab + bc + ca = 18$   
 $a^3 + b^3 + c^3 - 3abc = ?$   
 $\Rightarrow (a + b + c)^2 = 81$   
 $\Rightarrow a^2 + b^2 + c^2 + 2(ab + bc + ca) = 81$   
 $\Rightarrow a^2 + b^2 + c^2 = 81 - 2 \times 18$   
 $= 81 - 36 = 45$

Now,

$$a^3 + b^3 + c^3 - 3abc = (a + b + c)[a^2 + b^2 + c^2 - ab - bc - ca] = 9.[45 - 18] = 9 \times 27 = 243$$

45. (B)  $\frac{x}{y} + \frac{y}{x} = 1$

$$\frac{x^2 + y^2}{xy} = 1$$

then  $x^3 + y^3 = ?$

$$\Rightarrow x^2 + y^2 - xy = 0$$

Now,  $x^3 + y^3 = (x + y)(x^2 + y^2 - xy) = 0$

46. (A)  $5^x = 30^y = 6^z$   
 $30^{-y} = 5^y \times 6^y$

Let  $5^x = k \Rightarrow 5 = k^{\frac{1}{x}}$

$30^{-y} = k \Rightarrow 30 = k^{\frac{1}{y}}$

$$6^z = k \Rightarrow 6 = k^{\frac{1}{z}}$$

$$\Rightarrow k^{\frac{1}{x}} \cdot k^{\frac{1}{y}} = k^{\frac{1}{z}} \Rightarrow \frac{1}{x} + \frac{1}{y} = -\frac{1}{z}$$

$$\Rightarrow \frac{1}{x} + \frac{1}{y} + \frac{1}{z} = 0 \Rightarrow \frac{xy + yz + zx}{xyz} = 0$$

47. (B)  $\frac{1}{x^{p-q} + 1} + \frac{1}{x^{q-p} + 1}$

$$= \frac{1}{x^{p-q} + 1} + \frac{1}{\frac{1}{x^{p-q}} + 1} = \frac{1}{x^{p-q} + 1} + \frac{x^{p-q}}{x^{p-q} + 1}$$

$$= \frac{1 + x^{p-q}}{1 + x^{p-q}} = 1$$

48. (C)  $x = 8 + 2\sqrt{15}$

$$x = (\sqrt{5})^2 + (\sqrt{3})^2 + 2\sqrt{5} \cdot \sqrt{3}$$

$$x = (\sqrt{5} + \sqrt{3})^2$$

$$\sqrt{x} = \sqrt{5} + \sqrt{3}$$

$$\text{or } \frac{1}{\sqrt{x}} = \frac{1}{(\sqrt{5} + \sqrt{3})} = \frac{(\sqrt{5} - \sqrt{3})}{2}$$

$$\left( \sqrt{x} + \frac{1}{\sqrt{x}} \right) = \sqrt{5} + \sqrt{3} + \frac{\sqrt{5}}{2} - \frac{\sqrt{3}}{2}$$

$$= \frac{3\sqrt{5}}{2} + \frac{\sqrt{3}}{2}$$

49. (A)  $\frac{\frac{1+a}{1} - \frac{a^{\frac{1}{2}} + a^{-\frac{1}{2}}}{1+a} + a^{-2}}{a^2 + a^2} = ?$

$$= \frac{1+a}{\sqrt{a} + \frac{1}{\sqrt{a}}} - \frac{\sqrt{a} + \frac{1}{\sqrt{a}}}{1+a} + \frac{1}{\sqrt{a}}$$

$$= \frac{(1+a)\sqrt{a}}{(a+1)} - \frac{(a+1)}{\sqrt{a}(a+1)} + \frac{1}{\sqrt{a}}$$

$$= \sqrt{a} - \frac{1}{\sqrt{a}} + \frac{1}{\sqrt{a}}$$

$$= \sqrt{a}$$

50. (D)  $\frac{p}{q} = \frac{x+3}{x-3} \quad \frac{p^2 + q^2}{p^2 - q^2} = ?$

$$\frac{p^2}{q^2} = \frac{(x+3)^2}{(x-3)^2}$$

$$= \frac{p^2 + q^2}{p^2 - q^2} = \frac{(x+3)^2 + (x-3)^2}{(x+3)^2 - (x-3)^2}$$

$$= \frac{2(x^2 + 9)}{2(6x)}$$

$$= \frac{x^2 + 9}{6x}$$

51. (D)  $x^6 - 18x^3 + k$

Value of 'k' to be a perfect square

use  $x = -1$

$$\text{We'll get } = 1 + 18 + k$$

$$k + 19$$

for this to be square

We'll take from options  $k = 81$

That since  $100 = (10)^2$

52. (D)  $\frac{\sqrt{5+x} + \sqrt{5-x}}{\sqrt{5+x} - \sqrt{5-x}} = 3$

C & D

$$\frac{\sqrt{5+x}}{\sqrt{5-x}} = \frac{3+1}{3-1} = \frac{4}{2} = 2$$

Squaring

$$\Rightarrow \frac{5+x}{5-x} = 4$$

$$\Rightarrow 5+x = 20-4x$$

$$\Rightarrow x = \frac{15}{5} = 3$$

53. (D)  $x+y+z = 12$

$$xy + yz + xz = 44$$

$$xyz = 48$$

$$x^3 + y^3 + z^3 = ?$$

$$(x+y+z)^2 = 144$$

$$x^2 + y^2 + z^2 + 2(xy + yz + zx) = 144$$

$$\Rightarrow x^2 + y^2 + z^2 = 144 - 88$$

$$\Rightarrow x^2 + y^2 + z^2 = 56$$

$$x^3 + y^3 + z^3 - 3xyz$$

$$= (x+y+z)[x^2 + y^2 + z^2 - (xy + yz + zx)]$$

$$\Rightarrow x^3 + y^3 + z^3 - 144 = 12[56 - 44]$$

$$\Rightarrow x^3 + y^3 + z^3 = 144 + 144$$

$$\Rightarrow x^3 + y^3 + z^3 = 288$$

54. (B)  $x = \frac{4\sqrt{ab}}{\sqrt{a} + \sqrt{b}} \quad a \neq b$

$$\text{find } \frac{x+2\sqrt{a}}{x-2\sqrt{a}} + \frac{x+2\sqrt{b}}{x-2\sqrt{b}} = ?$$

$$= \frac{(x+2\sqrt{a})(x-2\sqrt{b}) + (x+2\sqrt{b})(x+2\sqrt{a})}{(x-2\sqrt{a})(x-2\sqrt{b})}$$

$$= \frac{2x^2 - 8\sqrt{ab}}{x^2 - 4\sqrt{ab}} = 2 \cdot \frac{(x^2 - 4\sqrt{ab})}{(x^2 - 4\sqrt{ab})} = 2$$

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**55.(C)**  $x(2x + 3) = 90$

$$\frac{7}{\sqrt{y}} + \frac{2}{\sqrt{y}} = \sqrt{y}$$

$$= y = 9 \quad \text{---(i)}$$

$$x = 6 \quad \text{---(ii)}$$

$$x^2 + y^2 = 36 + 81 \\ = 117$$

**56.(C)**  $\frac{x}{y} = \frac{4}{9}$

$$x = 4K$$

$$y = 9K$$

$$\frac{7x^2 - 19xy + 11y^2}{y^2} = ?$$

$$\frac{(112 - 19 \times 36 + 11 \times 81)K^2}{81K^2} = \frac{319}{81}$$

**57.(C)**  $(x - 3) + \frac{1}{(x - 3)} = 4$

$$(x - 3)^3 + \frac{1}{(x - 3)^3} = ? \\ = 4^3 - 3 \times 4 = 52$$

**58.(B)**  $x^2 + y^2 + z^2 = xy + yz + zx$

$$x = y = z$$

$$\Rightarrow \frac{7x + 3y - 5z}{5x} = \frac{10x - 5x}{5x} = 1$$

**59. (D)**  $ab + bc + ca = 17$

$$a + b + c = 11$$

Squaring both sides, we get

$$(a + b + c)^2 = 11^2$$

$$a^2 + b^2 + c^2 + 2(ab + bc + ac) = 121$$

$$a^2 + b^2 + c^2 + 2 \times 17 = 121$$

$$a^2 + b^2 + c^2 = 121 - 34 = 87$$

$$a^3 + b^3 + c^3 - 3abc = (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca)$$

$$= 11(87 - 17)$$

$$= 11 \times 70 = 770$$

**60. (D)**  $x^4 + \frac{1}{x^4} = 62$

$$x^4 + \frac{1}{x^4} + 2x^2 \cdot \frac{1}{x^2} = 62 + 2$$

$$\left(x^2 + \frac{1}{x^2}\right)^2 = 64$$

$$x^2 + \frac{1}{x^2} = 8$$

cubing both sides, we get

$$\left(x^2 + \frac{1}{x^2}\right)^3 = (8)^3$$

$$x^6 + \frac{1}{x^6} + 3x^2 \cdot \frac{1}{x^2} \left(x^2 + \frac{1}{x^2}\right) = 512$$

$$x^6 + \frac{1}{x^6} + 3 \times 8 = 512$$

$$x^6 + \frac{1}{x^6} = 512 - 24 = 488$$

**61. (B)**  $x + y = 4$

$$\frac{2}{x-2} + \frac{2}{y-2} = \frac{2(y-2) + 2(x-2)}{(x-2)(y-2)}$$

$$= \frac{(2y-4) + (2x-4)}{(x-2)(y-2)} = \frac{2(x+y)-8}{(x-2)(y-2)}$$

$$\frac{x^2 + 25}{5x} = -2$$

$$x^2 + 10x + 25 = 0$$

$$(x + 5)^2 = 0$$

$$x = -5$$

$$\therefore x^3 = -125$$

$$= \frac{2 \times 4 - 8}{(x-2)(y-2)} = 0$$

**62. (A)**  $\frac{x}{5} + \frac{5}{x} = -2$

$$\frac{x^2 + 25}{5x} = -2$$

$$x^2 + 10x + 25 = 0$$

$$(x + 5)^2 = 0$$

$$x = -5$$

$$\therefore x^3 = -125$$

**63. (C)**  $x + \frac{1}{x} = 2 \quad x = 1, \frac{1}{x} = 1$

$$x^{21} + \frac{1}{x^{1331}} = 2$$

**64. (B)**  $x^3 - y^3 = 81$

$$x - y = 3 \quad \dots\dots (1)$$

$$x^2 + y^2 = ?$$

$$(x^2 + y^2 + xy)(x - y) = 81$$

$$x^2 + y^2 + xy = \frac{81}{3} = 27$$

$$\frac{x^2 + y^2 - 2xy}{3xy} = 18$$

$$xy = 6$$

$$x^2 + y^2 = 27 - 6 = 21$$

65. (C)  $\sqrt{5x-6} + \sqrt{5x-6} = 6$

$$(\sqrt{5x-6} + \sqrt{5x-6})^2 = 36$$

$$10x + 2\sqrt{25x^2 - 36} = 36$$

$$2\sqrt{25x^2 - 36} = 36 - 10x$$

Square

$$25x^2 - 36 = 324 + 25x^2 - 180x$$

$$\Rightarrow 180x = 360$$

$$x = 2$$

or from options we can satisfy the ans.

66. (D)  $2x + \frac{1}{2x} = 2; \quad \sqrt{2\left[\frac{1}{x}\right]^4 + \left[\frac{1}{x}\right]^5} = ?$

$$\Rightarrow 4x^2 + 1 = 4x$$

$$4x^2 + 1 = 4x$$

$$4x^2 - 4x + 1 = 0$$

$$(2x - 1)^2 = 0$$

$$2x = 1$$

$$x = \frac{1}{2}$$

$$\frac{1}{x} = 2$$

Using the given eq.

$$\sqrt{2 \cdot 2^4 + 2^5}$$

$$\sqrt{2^5 + 2^5} = \sqrt{2^6} = 2^3 = 8$$

67. (D)  $x + \frac{1}{x} = 5$

$$x - \frac{1}{x} = \pm \sqrt{21}$$

68. (A)  $x = (\sqrt{2} + 1) / (\sqrt{2} - 1)$

$$x = \frac{(\sqrt{2} + 1)}{(\sqrt{2} - 1)} = \frac{1}{x} = \left(\frac{\sqrt{2} - 1}{\sqrt{2} + 1}\right)$$

Then

$$\frac{x^5 + x^4 + x^2 + x}{x^3}$$

$$\Rightarrow x^2 + x + \frac{1}{x} + \frac{1}{x^2}$$

$$= x^2 + \frac{1}{x^2} + x + \frac{1}{x} \quad \dots\dots (1)$$

$$x^2 = \left(\frac{\sqrt{2} + 1}{\sqrt{2} - 1}\right)^2 = \left(\frac{3 + 2\sqrt{2}}{3 - 2\sqrt{2}}\right) = (3 + 2\sqrt{2})^2$$

$$\frac{1}{x} = \left(\frac{3 - 2\sqrt{2}}{3 + 2\sqrt{2}}\right) = (3 - 2\sqrt{2})^2$$

eq. (1)

$$= (3 + 2\sqrt{2})^2 + (3 - 2\sqrt{2})^2 + (\sqrt{2} + 1)^2 + (\sqrt{2} - 1)^2$$

$$= 17 + 17 + 3 + 3 = 40$$

69. (C)  $x = 5 - 2\sqrt{6}$

$$\sqrt{x} + \frac{1}{\sqrt{x}} = ?$$

$$(\sqrt{x})^2 = (\sqrt{3} - \sqrt{2})^2$$

$$\sqrt{x} = \sqrt{3} - \sqrt{2}$$

$$\frac{1}{\sqrt{x}} = \sqrt{3} + \sqrt{2} \Rightarrow \sqrt{x} + \frac{1}{\sqrt{x}} = 2\sqrt{3}$$

70. (A)  $27^x + 27^{\left(\frac{x-1}{3}\right)} = 972$

$$x = ?$$

$$27^x + \frac{27^x}{27^{4/3}}$$

$$27^x \left[ 1 + \frac{1}{3} \right] = 972$$

$$27^x = \frac{972 \times 3}{4} = 243 \times 3$$

$$27^x = 729 = (27)^2$$

$$x = 2$$

71. (C)  $a = 73$

$b = 74 \quad c = 75$

$$a^3 + b^3 + c^3 - 3abc$$

$$= \frac{1}{2} (a + b + c) [(a - b)^2 + (b - c)^2 + (c - a)^2]$$

$$= \frac{1}{2} (222) [1+1+4]$$

$$= 666$$

72. (B)  $x^2 + \frac{1}{x^2} = \frac{31}{9}$

$$x + \frac{1}{x} = \frac{7}{3}$$

$$x^3 + \frac{1}{x^3} = \frac{343}{27} - 3 \times \frac{7}{3} = \frac{154}{27}$$

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73.(A)  $\frac{(x^2 - 5x + 6)}{(x^2 - 3x + 2)} \div \frac{(x^2 - 7x + 12)}{(x^2 - 5x + 4)}$

$$= \frac{(x^2 - 3x - 2x + 6)}{(x^2 - 2x - x + 2)} \times \frac{(x^2 - 4x - x + 4)}{(x^2 - 4x - 3x + 12)}$$

$$= \frac{(x-3)(x-2)}{(x-2)(x-1)} \times \frac{(x-4)(x-1)}{(x-4)(x-3)} = 1$$

74. (C)  $x - \frac{1}{x} = 3$

$$= \frac{(2x^4 + 3x^3 + 13x^2 - 3x + 2)}{(3x^4 + 3)}$$

$$= \frac{x^2 \left( 2x^2 + 3x + 13 - \frac{3}{x} + \frac{2}{x^2} \right)}{x^2 3 \left( x^2 + \frac{1}{x^2} \right)}$$

$$= \frac{2 \left( x^2 + \frac{1}{x^2} \right) + 3 \left( x - \frac{1}{x} \right) + 13}{3 \left( x^2 + \frac{1}{x^2} \right)}$$

$$= x^2 + \frac{1}{x^2} = 11$$

$$= \frac{2 \times 11 + 3 \times 3 + 13}{3 \times 11} = \frac{44}{33} = \frac{4}{3}$$

75.(B)  $x + y = 5$   
 $x^3 + y^3 = 35$   
 $x = 2, y = 3$   
Diff. = 1

76.(D)  $x = \sqrt{\frac{2+\sqrt{3}}{2-\sqrt{3}}}$   
 $x^2 + x - 9 = ?$

$$\Rightarrow \frac{2+\sqrt{3}}{2-\sqrt{3}} + \sqrt{\frac{2+\sqrt{3}}{2-\sqrt{3}} \times \frac{(2+\sqrt{3})}{(2+\sqrt{3})} - 9}$$

$$= \frac{2+\sqrt{3}}{2-\sqrt{3}} + (2+\sqrt{3}) - 9$$

$$= \frac{2+\sqrt{3} + 1 - 9(2-\sqrt{3})}{2-\sqrt{3}}$$

$$= \frac{3 + \sqrt{3} - 18 + 9\sqrt{3}}{2-\sqrt{3}} = 10\sqrt{3} - 15$$

$$= 5\sqrt{3} \frac{(2-\sqrt{3})}{(2-\sqrt{3})} = 5\sqrt{3}$$

77.(C) If  $x + y + z = 0$

$$= \frac{x^3}{3z} + \frac{y^3}{3xz} + \frac{z^2}{3x}$$

$$= \frac{x^3 + y^3 + z^2}{3xz} = \frac{3xyz}{3xz} = y$$

78.(C)  $x - \frac{1}{x} = 1$

$$x + \frac{1}{x} = \pm\sqrt{5}$$

$$\left[ \frac{1}{x-1} - \frac{1}{x+1} + \frac{1}{x^2+1} - \frac{1}{x^2-1} \right]$$

$$= \left[ \frac{2}{x^2-1} + \frac{1}{x^2+1} + \frac{1}{x^2-1} \right]$$

$$= \left[ \frac{1}{x^2-1} + \frac{1}{x^2+1} \right]$$

$$= \frac{2x^2}{(x^4-1)} = \frac{2}{\left(x^2 - \frac{1}{x^2}\right)} = \frac{2}{\left(x + \frac{1}{x}\right)\left(x - \frac{1}{x}\right)}$$

$$= \frac{\pm 2}{1/\sqrt{5}} = \frac{\pm 2}{\sqrt{5}}$$

79. (A)  $7x - \frac{3}{2}(2x-3) = \frac{1}{2}$

$$\Rightarrow 14x - 6x + 9 = 1$$

$$\Rightarrow 8x = -8$$

$$\Rightarrow x = -1$$

80. (C)  $a = 3, b = 1$

$$a + b = 4$$

$$ab = 3$$

$$a^3 + b^3 = ?$$

$$27 + 1 = 28$$

81. (A) Let the fraction be  $\frac{p}{q}$

$$\text{then } \frac{p}{q} + 7 \cdot \frac{q}{p} = \frac{11}{2}$$

$$\Rightarrow p^2 + 7q^2 = \frac{11pq}{2}$$

$$\Rightarrow 2p^2 + 14q^2 - 11pq = 0$$

$$\Rightarrow 2p^2 - 17pq + 4pq + 14q^2 = 0$$

$$\Rightarrow p(2p - 7q) - 2q(2p - 7q) = 0$$

$$\Rightarrow (p - 2q)(2p - 7q) = 0$$

$$\frac{p}{q} = 2 \quad \frac{p}{q} = \frac{7}{2}$$

**82. (B)**  $5x - \frac{1}{2}(2x - 7) = 5.5$   
 $= 5x - x + \frac{7}{2} = 5.5$   
 $= 4x = 5.5 - 3.5 = 2$   
 $= x = \frac{1}{2}$

**83. (C)**  $a + b = 4$   
 $ab = -5$

Here  $a = 5$

$b = -1$

$a^3 + b^3$

$= 5^3 + (-1)^3$

$= 125 - 1 = 124$

**84. (A)** Let No. be 'p'  
 A.T.Q.

$P + \frac{4}{P} = 5$

Here  $P = 4$

**85. (A)**  $\frac{x}{3} - \left[ 5\left(\frac{7x}{5} - \frac{4}{3}\right) \right] \times \frac{1}{2} = \frac{-x}{6}$   
 $\Rightarrow \frac{x}{3} - \left[ 7x - \frac{20}{3} \right] \times \frac{1}{2} = \frac{-x}{6}$   
 $\Rightarrow \frac{x}{3} + \frac{x}{6} = \frac{7x}{2} + \frac{10}{3}$   
 $\Rightarrow \frac{x}{2} - \frac{7x}{2} = -\frac{10}{3}$   
 $\Rightarrow 3x = \frac{10}{3} \Rightarrow n = \frac{10}{9}$

**86. (B)**  $a^3 + b^3 = +19$   
 $a + b = 1$   
 $ab = ?$   
 $a^3 + b^3 = (a + b)^3 - 3ab(a + b)$   
 $\Rightarrow +19 = 1 - 3(1).ab$   
 $\Rightarrow +19 - 1 = -3ab$   
 $\Rightarrow .18 = -3ab$   
 $\Rightarrow ab = -6$

**87. (B)** Let the fraction be  $\frac{p}{q}$   
 $\frac{p}{q} = \frac{q}{p} + \frac{72}{77}$   
 $\frac{p}{q} - \frac{q}{p} = \frac{72}{77}$   
 $77p^2 - 77q^2 = 77pq$   
 $\Rightarrow 77p^2 - 121pq + 49pq - 77q^2 = 0$   
 $\Rightarrow 17(7p - 11q) + 7q(7p - 11q) = 0$   
 $\Rightarrow 7p = 11q = \frac{p}{q} = \frac{11}{7}$

**88. (B)**  $\frac{7\left(\frac{5x}{3} - \frac{3}{2}\right)}{2} + \frac{3}{2} = \frac{1}{4}$   
 $\Rightarrow 7\left(\frac{5x}{3} - \frac{3}{2}\right) = \frac{1}{2} - 3 \Rightarrow \frac{35x}{3} - \frac{21}{2} = \frac{-5}{2}$   
 $\Rightarrow \frac{35x}{3} = \frac{16}{2} \Rightarrow x = \frac{24}{35}$

**89. (C)**  $a^3 + b^3 = 19$   
 $ab = -6$   
 $a + b = ?$   
 from (1)  
 $(a + b)^3 = a^3 + b^3 + 3ab(a + b)$   
 $= 19 + 3(-6)(a + b)$   
 $(a + b)^3 + 18(a + b) = 19$   
 From options  
 $(a + b) = 1$

**90. (A)** Let fraction =  $\frac{a}{b}$   
 A.T.Q.  $\frac{4a}{b} + \frac{6b}{a} = 11$   
 $\Rightarrow 4a^2 + 6b^2 = 11ab$   
 $\Rightarrow 4a^2 - 8ab - 3ab + 6b^2 = 0$   
 $\Rightarrow 4a(a - 2b) - 3b(a - 2b) = 0$   
 $\Rightarrow 4a = 3b \quad a = 2b$   
 $\Rightarrow \frac{a}{b} = \frac{3}{4} \quad \frac{a}{b} = 2$

**91. (D)**  $\frac{17}{3} + 3x\left[2x - \frac{5}{3}\right] \times \frac{1}{2} = \frac{1}{6}$   
 $\Rightarrow \frac{17}{3} + [6x - 5] \times \frac{1}{2} = \frac{1}{6}$   
 $\Rightarrow \frac{17}{3} + 3x - \frac{5}{2} = \frac{1}{6}$   
 $\Rightarrow 3x = \frac{5}{2} + \frac{1}{6} - \frac{17}{3} \Rightarrow 3x = \frac{15 + 1 - 34}{6}$

$\Rightarrow 3x = \frac{-18}{6} \Rightarrow x = -1$

**92. (C)**  $a + b = 5$   
 $ab = 6$   
 $a = 3, b = 2$   
 $a^3 + b^3 = 27 + 8 = 35$

**93. (A)** Let the fraction be  $\frac{a}{b}$   
 $\frac{a}{b} + \frac{3b}{a} = \frac{37}{10}$

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$$\Rightarrow \frac{a^2 + 3b^2}{ab} = \frac{37}{10}$$

$$\Rightarrow a = 5, b = 2$$

$$= \frac{5}{2}$$

94.(A)  $\frac{5x}{2} - \left[ 7\left(6x - \frac{3}{2}\right)\right] \frac{1}{4}$

$$\frac{5x}{2} - \frac{21x}{2} + \frac{21}{8} = \frac{5}{8}$$

$$\frac{16x}{2} = \frac{16}{8} \Rightarrow x = \frac{1}{4}$$

95.(D)  $a^3 - b^3 = 91$

$$a - b = 1$$

$$a^3 - b^3 = (a - b)(a^2 + ab + b^2) \dots (i)$$

$$\therefore a - b = 1$$

$$a^2 + b^2 - 2ab = 1$$

$$a^2 + b^2 = 1 + 2ab \dots (ii)$$

From (i) and (ii)

$$91 = 1(1 + 2ab + ab)$$

$$91 = 1 + 3ab$$

$$3ab = 90$$

$$\boxed{ab = 30}$$

96. (B) Let the fraction is  $\underline{x}$

$$\text{the } x - \frac{2}{x} = \frac{7}{15}$$

$$15x^2 - 7x - 30 = 0$$

$$15x^2 - 25x + 18x - 30 = 0$$

$$5x(3x - 5) + 6(3x - 5) = 0$$

$$3x - 5 = 0$$

$$\boxed{x = \frac{5}{3}}$$

97. (C)  $\left[ 4\left(\frac{2x}{5} - \frac{3}{2}\right)\right] \times \frac{1}{3} + \frac{7}{5} = \frac{37}{5}$

$$\left(\frac{8x}{5} - 6\right) \frac{1}{3} = 6$$

$$\frac{8x}{5} = 24$$

$$x = \frac{24 \times 5}{8} = x = 15$$

98. (B)  $a - b = 4 \dots (1)$

$$ab = -3 \dots (2)$$

from (1)

$$(a - b)^2 = 16$$

$$a^2 + b^2 - 2ab = 16$$

$$a^2 + b^2 = 16 + 2 \times (-3) \text{ from 2}$$

$$a^2 + b^2 = 10 \dots (3)$$

Now,

$$a^3 - b^3 = (a - b)(a^2 + ab + b^2)$$

$$= 4(10 + (-3))$$

$$a^3 - b^3 = 28$$

99. (D) Let fraction =  $x$

$$\text{then, } 2x + \frac{3}{x} = \frac{29}{3}$$

$$\Rightarrow 6x^2 - 29x + 9 = 0$$

$$6x^2 - 27x - 2x + 9 = 0$$

$$3x(2x - 9) - 1(2x - 9) = 0$$

$$x = \frac{1}{3}, \frac{9}{2}$$

According to option  $x = \frac{9}{2}$

100.(C)  $\frac{8x}{3} + 7\left(5 - \frac{2x}{3}\right) \times \frac{1}{2} = \frac{1}{2}$

$$\Rightarrow \frac{8x}{3} + \frac{35}{2} - \frac{7x}{3} = \frac{1}{2}$$

$$\Rightarrow \frac{x}{3} = \frac{-34}{2}$$

$$x = -51$$

101.(B)  $a - b = 1 \dots (1)$

$$ab = 6 \dots (2)$$

from (1)

$$a^2 + b^2 - 2ab = 1$$

$$a^2 + b^2 = 1 + 2 \times 6$$

$$a^2 + b^2 = 13$$

$$\therefore a^3 - b^3 = (a - b)(a^2 + ab + b^2)$$

$$= -1(13 + 6)$$

$$= -19$$

102.(B) Do by option

If we take  $= \frac{9}{2}$

$$\text{then, } \frac{9}{2} + \frac{2}{9} \times 3$$

$$= \frac{9}{2} + \frac{2}{3} = \frac{31}{6}$$

So,  $\frac{9}{2}$  is the fraction

**103.** (C)  $\frac{x}{2} - \left[ 4\left(\frac{15}{2} - \frac{x}{3}\right) \right] \times \frac{1}{3} = -\frac{x}{18}$

$$\frac{x}{2} - \left( 30 - \frac{4x}{3} \right) \times \frac{1}{3} = \frac{-x}{18}$$

$$\frac{x}{2} + \frac{4x}{9} - 10 = \frac{-x}{18}$$

$$\frac{x}{2} + \frac{4x}{9} + \frac{x}{18} = 10 \Rightarrow \frac{9x + 8x + x}{18} = 10$$

$$x = 10$$

**104.** (D)  $a^3 + b^3 = 152 \quad \dots \dots (1)$

$$a + b = 8 \quad \dots \dots (2)$$

By (2)

$$(a + b)^2 = 64$$

$$a^2 + b^2 + 2ab = 64$$

$$a^2 + b^2 + 2ab = 64$$

$$a^2 + b^2 - 2ab = 64 - 3ab$$

Now from (1)

$$a^3 + b^3 = 152$$

$$(a + b)(a^2 + b^2 - ab) = 152$$

$$8(64 - 3ab) = 152$$

$$64 - 3ab = 19$$

$$3ab = 45$$

$$ab = 15$$

**105.** (A) Do by options

If we take option (A)

$$\text{the } \frac{5}{4} - \frac{4}{5} = \frac{9}{20}$$

So option (A) is correct

**106.** (C)  $5x + 6(3 - 2x) = 4$

$$5x + 18 - 12x = 4$$

$$7x = 14$$

$$x = 2$$

**107.** (C)  $a + b = 1 \quad \dots \dots (1)$

$$ab = -6 \quad \dots \dots (2)$$

From (1)

$$a^2 + b^2 + 2ab = 1$$

$$a^2 + b^2 = 1 - 2ab$$

(from 2)

$$a^2 + b^2 = 13$$

Now,

$$a^3 + b^3 = (a + b)(a^2 + b^2 - ab)$$

$$a^3 + b^3 = 1(13 - (-6))$$

$$a^3 + b^3 = 19$$

**108.** (D)  $x + \frac{20}{x} = 9$

$$x^2 - 9x + 20 = 0$$

$$x^2 - 5x - 4x + 20 = 0$$

$$x(x - 8) - 4(x - 5) = 0$$

$$x = 4, 5$$

By option x = 5

**109.** (A)  $9x - \left[ \frac{5(2x+1)}{2} \right] = \frac{9}{2}$

$$\Rightarrow 9x - 5x - \frac{5}{2} = \frac{9}{2}$$

$$\Rightarrow 4x = \frac{14}{2} \Rightarrow x = \frac{7}{4}$$

**110.** (D)  $a + b = 4 \quad \dots \dots (1)$

$$ab = -21 \quad \dots \dots (2)$$

From (1)

$$a^2 + b^2 + 2ab = 16$$

$$a^2 + b^2 = 16 + 42 \quad (\text{from 2})$$

$$a^2 + b^2 = 58$$

Now,

$$a^3 + b^3 = (a + b)(a^2 + b^2 - ab)$$

$$a^3 + b^3 = 4(58 - (-21))$$

$$a^3 + b^3 = 4 \times 79$$

$$a^3 + b^3 = 316$$

**111.** (A)  $x + \frac{10}{x} = \frac{37}{4}$

$$4x - 37x + 40 = 0$$

$$4x^2 - 32x - 5x + 40 = 0$$

$$4x(x - 8) - 5(x - 8) = 0$$

$$x = 8, \frac{5}{4}$$

According to option x =  $\frac{5}{4}$

**112.** (A)  $\frac{-1}{2} \times (x - 5) + 3 = \frac{-5}{2}$

$$\Rightarrow \frac{-x}{2} + \frac{5}{2} + 3 = \frac{-5}{2}$$

$$\Rightarrow \frac{-x}{2} = -5 - 3$$

$$x = 16$$

**113.** (C)  $a - b = 1 \quad \dots \dots (1)$

$$ab = 6 \quad \dots \dots (2)$$

$$a^2 + b^2 = 13 \quad \dots \dots (3)$$

Now

$$a^3 - b^3 = (a - b)(a^2 + b^2 + ab)$$

$$a^3 - b^3 = 1(13 + 6)$$

$$a^3 - b^3 = 19$$

**114.** (D)  $x - \frac{58}{x} = \frac{3}{4}$

$$4x^2 - 3x - 232 = 0$$

$$4x^2 - 32x + 29x - 232 = 0$$

$$4x(x - 8) + 29(x - 8) = 0$$

$$x = 8$$

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**115. (D)**  $\frac{5}{2} \left( \frac{8x}{3} - \frac{1}{2} \right) + \frac{13}{2} = \frac{2x}{3}$

$$\Rightarrow \frac{20x}{3} - \frac{5}{4} + \frac{13}{2} = \frac{2x}{3}$$

$$\Rightarrow \frac{20x}{3} - \frac{2x}{3} = \frac{5}{4} - \frac{13}{2}$$

$$\Rightarrow \frac{18x}{3} = \frac{5 - 26}{4}$$

$$\Rightarrow 6x = \frac{-21}{4}$$

$$x = \frac{-21}{6 \times 4} = \frac{-7}{8}$$

**116. (C)**  $a^3 + b^3 = 72$

$$ab = 8$$

$$\text{let } a = 4$$

$$b = 2$$

$$\text{then } a + b = 6$$

**117. (B)** let fraction is  $x$

A.T.Q.

$$4x + \frac{7}{x} = 16$$

$$\Rightarrow 4x^2 + 7 = 16x$$

$$\Rightarrow 4x^2 - 16x + 7 = 0$$

$$\Rightarrow 4x^2 - 14x - 2x + 7 = 0$$

$$\Rightarrow 2x(2x-1) - 7(2x-1) = 0$$

$$(2x-7)(2x-1) = 0$$

$$x = \frac{7}{2}, \frac{1}{2}$$

$$x = \frac{7}{2}$$

**118.(A)**  $\frac{14}{3} + \frac{1}{2} \left( x - \frac{7}{3} \right) = \frac{-2x}{3}$

$$\Rightarrow \frac{14}{3} + \frac{x}{2} - \frac{7}{6} = \frac{-2x}{3}$$

$$\Rightarrow \frac{x}{2} + \frac{2x}{3} = \frac{7}{6} - \frac{14}{3}$$

$$\Rightarrow \frac{7x}{6} = \frac{-21}{6}$$

$$\Rightarrow x = -3$$

**119.(A)**  $a + b = 10 \quad \dots\dots (1)$

$$ab = 24 \quad \dots\dots (2)$$

From (1)

$$a^2 + b^2 + 2ab = 100$$

$$a^2 + b^2 = 100 - 48$$

$$a^2 + b^2 = 52 \quad \dots\dots (3)$$

$$\text{Now } a^3 + b^3 = (a + b)(a^2 + b^2 - ab)$$

$$10(52 - 24)$$

$$a^3 + b^3 = 280$$

**120.(A)**  $x + \frac{3}{x} = \frac{19}{4}$

$$4x^2 - 19x + 12 = 0$$

$$4x^2 - 16x - 3x + 12 = 0$$

$$4x(x-4) - 3(x-4) = 0$$

$$x = \frac{3}{4}, 4$$

According to the option  $x = \frac{3}{4}$

**121. (D)**  $\frac{5}{2} - \frac{6}{5} \left( x - \frac{15}{2} \right) = \frac{-x}{5}$

$$\frac{5}{2} - \frac{6x}{5} + 9 = \frac{-x}{5}$$

$$x = \frac{23}{2}$$

**122.(D)**  $a - b = 2 \quad \dots\dots (1)$

$$ab = 24 \quad \dots\dots (2)$$

From (1)

$$(a - b)^2 = 4$$

$$a^2 + b^2 - 2ab = 4$$

$$a^2 + b^2 = 52 \quad \dots\dots (3)$$

$$\text{Now } a^3 - b^3 = (a - b)(a^2 + b^2 + ab)$$

$$a^3 - b^3 = 2(52 + 24)$$

$$a^3 - b^3 = 152$$

**123.(C)**  $2x + \frac{1}{x} = \frac{17}{6}$

$$12x^2 - 17x + 6 = 0$$

$$12x^2 - 8x - 9x + 6 = 0$$

$$4x(3x-2) - 3(3x-2) = 0$$

$$x = \frac{2}{3}, \frac{3}{4}$$

According to the option  $x = \frac{3}{4}$

**124.** (D)  $\frac{-3}{2} + \frac{2}{3}(3x+9) = \frac{x}{2}$

$$\frac{-3}{2} + 2x + 6 = \frac{x}{2}$$

$$\frac{3}{2}x = \frac{-9}{2}$$

$$x = -3$$

**125.** (D)  $a - b = 2$

$$ab = 8$$

$$a^3 - b^3 = ?$$

So,

$$\text{Let } a = 4$$

$$b = 2$$

$$\begin{aligned} a - b &= 2 \\ ab &= 4 \times 2 = 8 \end{aligned}$$

$$\begin{aligned} \text{So, } a^3 - b^3 &= 4^3 - 2^3 \\ &= 64 - 8 = 56 \end{aligned}$$

or

$$(a - b)^3 = a^3 - b^3 - 3ab(a - b)$$

$$2^3 = a^3 - b^3 - 3 \times 8 \times 2$$

$$a^3 - b^3 = 56$$

**126.** (A) So, let number is  $x$

$$x - \frac{7}{x} = 9.3$$

Best to solve this type we can put the options easily

$$\text{let } x = 10$$

$$10 - \frac{7}{10} = 9.3$$

$$\text{So } x = 10$$

**127.** (C)  $-3\left(1 - \frac{x}{2}\right) + \frac{5x}{3} = \frac{1}{6} \Rightarrow \frac{19x}{16} = 3 + \frac{1}{6}$

$$\Rightarrow \frac{19x}{6} = \frac{19}{6}$$

$$x = 1$$

**128.** (B)  $(a+b)^3 = a^3 + b^3 + 3ab(a+b)$

$$3^3 = a^3 + b^3 + 3 \times 4 \times 3 \Rightarrow a^3 + b^3 = 63$$

**129.** (C) Let number =  $x$

$$x + \frac{9}{x} = x^2 + 9 = 10x \Rightarrow x^2 - 10x + 9 = 0$$

$$x = 9$$

**130.** (D)  $\frac{10x}{3} + \frac{5}{2}\left(2 - \frac{x}{3}\right) = \frac{7}{2}$

$$\frac{10x}{3} + 5 - \frac{5x}{6} = \frac{7}{2}$$

$$\frac{15x}{6} = \frac{-3}{2}$$

$$x = \frac{-3}{5}$$

**131.** (D)  $a - b = 2 \quad \dots (1)$

$$ab = 15 \quad \dots (2)$$

$$(a - b)^2 = 4$$

$$a^2 + b^2 - 2ab = 4$$

$$a^2 + b^2 = 34 \quad \dots (3)$$

$$\text{Now } a^3 - b^3 = (a - b)(a^2 + b^2 + ab)$$

$$a^3 - b^3 = 2(34 + 15)$$

$$a^3 - b^3 = 98$$

**132.** (A)  $x + \frac{4}{x} = \frac{13}{3}$

$$3x^2 - 13x + 12 = 0$$

$$3x^2 - 9x - 4x + 12 = 0$$

$$3x(x - 3) - 4(x - 3) = 0$$

$$x = \frac{4}{3}, 3$$

According to option  $x = \frac{4}{3}$

**133.** (C)  $7x - \frac{3}{2} \times (4x - 9) = \frac{13}{2} \Rightarrow 14x - 12x + 27 = 13$

$$2x = -14 \Rightarrow x = -7$$

**134.** (B)  $(a+b)^3 = a^3 + b^3 + 3ab(a+b)$

$$8^3 = a^3 + b^3 + 3 \times 15 \times 8 \Rightarrow a^3 + b^3 = 152$$

**135.** (A) Let number =  $x$

$$x + \frac{4}{x} = \frac{17}{2} \Rightarrow \frac{x^2 + 4}{x} = \frac{17}{2}$$

$$\Rightarrow 2x^2 - 17x + 8 = 0$$

$$x = \frac{1}{2}, 8$$

**136.** (A)  $\frac{1}{3}\left(\frac{12x}{5} - \frac{1}{2}\right) + \frac{6}{5} = \frac{7}{6}$

$$\frac{4x}{5} - \frac{1}{6} + \frac{6}{5} = \frac{7}{6}$$

$$\frac{4x}{5} = \frac{4}{30} \Rightarrow x = \frac{1}{6}$$

**137.** (B)  $a - b = 10 \quad \dots (1)$

$$ab = -21 \quad \dots (2)$$

from (1)

$$a^2 + b^2 - 2ab = 100$$

$$a^2 + b^2 = 58 \quad \dots (3)$$

$$\text{Now } a^3 - b^3 = (a - b)(a^2 + b^2 + ab)$$

$$= 10(58 - 21)$$

$$a^3 - b^3 = 370$$

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**138.(C)**  $2x + \frac{5}{x} = 7$

$$2x^2 - 7x + 5 = 0$$

$$2x^2 - 5x - 2x + 5 = 0$$

$$x(2x - 5) - 1(2x - 5) = 0$$

$$x = 1, \frac{5}{2}$$

According to option  $x = \frac{5}{2}$

**139. (B)**  $\frac{2}{3}\left(\frac{6x}{5} - \frac{1}{4}\right) + \frac{1}{3} = \frac{9x}{5}$

$$\frac{12x}{15} - \frac{1}{6} + \frac{1}{3} = \frac{9x}{5}$$

$$\frac{12x}{15} - \frac{9x}{5} = -\frac{1}{6}$$

$$\frac{12x - 27x}{15} = -\frac{1}{6}$$

$$\frac{-15x}{15} = -\frac{1}{6}$$

$$x = \frac{1}{6}$$

**140. (D)**  $a^3 + b^3 = 341$

$$ab = 30$$

$$\text{Here } a = 6, b = 5$$

$$\text{So, } a + b = 11$$

**141. (C)** Assume that Fraction is  $x$   
according to question

$$x + \frac{1}{x} \times 3 = \frac{31}{6}$$

$$\frac{x^2 + 3}{x} = \frac{31}{6}$$

$$6x^2 + 18 = 31x$$

$$6x^2 - 31x + 18 = 0$$

$$6x^2 - 27x - 4x + 18 = 0$$

$$3x(2x - 9) - 2(2x - 9) = 0$$

$$x = \frac{9}{2}$$



### Mother's Advance Maths • Algebra [Previous Year Questions]

9. Consider a question and two statements:

**Question :** Is  $3x + 2y$  positive?

**Statement-I :**  $x^3 = -29.8$

**Statement-II :**  $y^3 = 3x$

Which one of the following is correct in respect of the question and the statements?

एक प्रश्न और दो कथनों पर विचार कीजिए:

प्रश्न : क्या  $3x + 2y$  धनात्मक है?

**कथन-I :**  $x^3 = -29.8$

**कथन-II :**  $y^3 = 3x$

प्रश्न और कथनों के बारे में निप्रलिखित में से कौन-सा एक सही है?

(A) प्रश्न का उत्तर देने के लिए केवल कथन-I ही पर्याप्त है

Statement-I alone is sufficient to answer the question

(B) प्रश्न का उत्तर देने के लिए केवल कथन-II ही पर्याप्त है

Statement-II alone is sufficient to answer the question

(C) प्रश्न का उत्तर देने के लिए कथन-I और कथन-II दोनों मिलकर ही पर्याप्त है

Both Statement-I and Statement-II are together sufficient to answer the question

(D) प्रश्न का उत्तर देने के लिए कथन-I और कथन-II दोनों मिलकर ही पर्याप्त नहीं है

Both statement-I and Statement-II are not sufficient to answer the question

10. Consider a question and two statements:

**Question :** Does the equation  $ax^2 + bx + c = 0$  have real roots of opposite sign?

**Statement-I :** The discriminant  $D > 0$

**Statement-II :**  $c / a > 0$

Which one of the following is correct in respect of the question and the statements?

एक प्रश्न और दो कथनों पर विचार कीजिए:

प्रश्न : क्या समीकरण  $ax^2 + bx + c = 0$  विपरीत चिन्ह वाले वास्तविक मूल हैं?

**कथन-I :** विविक्तकर  $D > 0$

**कथन-II :**  $c / a > 0$

प्रश्न और कथनों के बारे में निप्रलिखित में से कौन-सा एक सही है?

(A) प्रश्न का उत्तर देने के लिए केवल कथन-I ही पर्याप्त है

Statement-I alone is sufficient to answer the question

(B) प्रश्न का उत्तर देने के लिए केवल कथन-II ही पर्याप्त है

Statement-II alone a sufficient to answer the question

(C) प्रश्न का उत्तर देने के लिए कथन-I और कथन-II दोनों मिलकर ही पर्याप्त है

Both Statement-I and Statement-II are together sufficient to answer the question

(D) प्रश्न का उत्तर देने के लिए कथन-I और कथन-II दोनों मिलकर ही पर्याप्त नहीं है

Both statement-I and Statement-II are not sufficient to answer the question

11. Consider a question and two statements:

**Question :** Is  $a^2 + b^2 + c^2 - ab - bc - ca$  ( $a, b, c$  are distinct real numbers) always positive?

**Statement-I :**  $a > b > c$

**Statement-II :**  $a + b + c = 0$

Which one of the following is correct in respect of the question and the statements?

एक प्रश्न और दो कथनों पर विचार कीजिए:

प्रश्न : क्या  $a^2 + b^2 + c^2 - ab - bc - ca$  ( $a, b, c$  भिन्न वास्तविक संख्याएँ हैं) सर्वदा धनात्मक है?

**कथन-I :**  $a > b > c$

**कथन-II :**  $a + b + c = 0$

प्रश्न और कथनों के बारे में निप्रलिखित में से कौन-सा एक सही है?

(A) प्रश्न का उत्तर देने के लिए केवल कथन-I ही अपेक्षित है

Statement-I alone is required to answer the question

(B) प्रश्न का उत्तर देने के लिए केवल कथन-II ही अपेक्षित है

Statement-II alone is required to answer the question

(C) प्रश्न का उत्तर देने के लिए कथन-I और कथन-II दोनों अपेक्षित हैं

Both Statement-I and Statement-II are required to answer the question

(D) प्रश्न का उत्तर देने के लिए न तो कथन-I और न ही कथन-II अपेक्षित हैं

Neither Statement-I nor Statement-II required to answer the question

12. Consider a question and two statements:

**Question :** Is  $\frac{x^5 + y^5}{x^4 + y^4}$  always greater than

$$\frac{x^4 + y^4}{x^2 + y^2} \quad (x \neq y \neq 0)?$$

**Statement-I :**  $x > y$

**Statement-II :**  $x^2 + y^2 > 2xy$

Which one of the following is correct in respect of the question and the statements?

एक प्रश्न और दो कथनों पर विचार कीजिए:

प्रश्न : क्या  $\frac{x^6 + y^6}{x^4 + y^4}$  हमेशा  $\frac{x^4 + y^4}{x^2 + y^2}$  ( $x \neq y \neq 0$ ) से बड़ा है?

**कथन-I :**  $x > y$

**कथन-II :**  $x^2 + y^2 > 2xy$

- (A) प्रश्न का उत्तर देने के लिए केवल कथन-I ही अपेक्षित है। Statement-I alone is required to answer the question.
- (B) प्रश्न का उत्तर देने के लिए केवल कथन-II ही अपेक्षित है। Statement-II alone is required to answer the question.

(C) प्रश्न का उत्तर देने के लिए कथन-I और कथन-II दोनों अपेक्षित हैं।

Both Statement-I and Statement-II are required to answer the question

(D) प्रश्न का उत्तर देने के लिए न तो कथन-I और न ही कथन-II अपेक्षित हैं।

Neither Statement-I nor Statement-II required to answer the question

13. How many quadratic equations have the sum of their roots equal to the product of their roots?

कितने द्विघात समीकरणों में उनके मूलों के योग, उनके मूलों के गुणनफल के बराबर होते हैं?

(A) Zero / शून्य

(B) One / एक

(C) Two / दो

(D) Infinitely many / अनंततः अनेक

## Solution

$$1. (D) x = 7 + 4\sqrt{3}$$

$$x = (\sqrt{3})^2 + (2)^2 + 4\sqrt{3} \text{ Square root}$$

$$\sqrt{x} = (\sqrt{3} + 2) = 2 + \sqrt{3}$$

$$\frac{1}{\sqrt{x}} = 2 - \sqrt{3}$$

$$\sqrt{x} + \frac{1}{\sqrt{x}} = 4$$

$$2. (C) \frac{(5.4)^3 - (.4)^3}{(5.4)^2 + 5.4 \times .4 + (.4)^2}$$

$$a^3 - b^3 = (a-b)(a^2 + b^2 + ab)$$

$$\Rightarrow a - b = \frac{a^3 - b^3}{a^2 + b^2 + ab}$$

$$5.4 - 0.4 = 5$$

$$3. (C) x = 9999$$

$$\Rightarrow \frac{4x^3 - x}{(2x-1)(6x-3)}$$

$$\Rightarrow \frac{x(4x^2 - 1)}{(2x+1)3(2x-1)}$$

$$\Rightarrow \frac{x(2x-1)(2x+1)}{3(2x+1)(2x-1)}$$

$$\Rightarrow \frac{x}{3} = \frac{9999}{3} = 3333$$

4. (A) x and y are real numbers

So  $x = 0$  and  $y = 0$

$$(0 + \sqrt{1 + 0^2})(0 + \sqrt{1 + 0^2}) = 1$$

$$1 = 1$$

$$(0 + 0)^2 = 0$$

$$5. (A) 43^x \times 47^y = (2021)^2$$

$$43^x \times 47^y = 43^2 \times 47^2$$

$$x = 2$$

$$y = 2$$

$$\Rightarrow \frac{16 + 2 + 2}{8 - 2 - 2} = \frac{20}{4} = 5$$

$$6. (A) x^2 = 17x + y \quad \dots(i)$$

$$y^2 = x + 17y \dots(ii) \quad x \neq y$$

$$\text{eq. (i)} + \text{(ii)}$$

$$x^2 + y^2 = 18(x + y)$$

$$\text{eq. (i)} - \text{(ii)}$$

$$x^2 - y^2 = 16(x - y)$$

$$(x - y)(x + y) = 16(x - y)$$

$$x + y = 16$$

**Mother's Advance Maths • Algebra [Previous Year Questions]**

$$x^2 + y^2 = 18 \times 16$$

eq.(i) add 1 bothside

$$x^2 + y^2 + 1 = 288 + 1$$

$$\sqrt{x^2 + y^2 + 1} = \sqrt{289} \text{ square root}$$

$$\sqrt{x^2 + y^2 + 1} = 17$$

7. (A)  $194480 + n = m^4 \quad n = 1, m = 21$   
 $194480 + 1 = (21)^4$   
 $194481 = 194481$

8. (C)  $\frac{x-y}{x\sqrt{y} + y\sqrt{x}} = \frac{1}{\sqrt{x}}$

$$\frac{x-y}{\sqrt{x}\sqrt{y}(\sqrt{x} + \sqrt{y})} = \frac{1}{\sqrt{x}}$$

$$\therefore (a-b) = (\sqrt{a} + \sqrt{b})(\sqrt{a} - \sqrt{b})$$

$$\frac{(\sqrt{x} - \sqrt{y})(\sqrt{x} + \sqrt{y})}{\sqrt{x}\sqrt{y}(\sqrt{x} + \sqrt{y})} = \frac{1}{\sqrt{x}}$$

$$\sqrt{x} - \sqrt{y} = \sqrt{y}$$

$$\sqrt{x} = 2\sqrt{y}$$

$$x = 4y$$

$$\Rightarrow \frac{x}{y} = 4$$

9. (C) Equation -  $3x + 2y$   
Statement - I =  $x^3 = -29.8$

Statement - II =  $y^3 = 3x$

Both statements are required to solving the equation.

10. (D) Equation -  $ax^2 + bx + c = 0$   
Roots are same and opposite sign

$$\alpha + \beta = 0 \quad \alpha = -\beta$$

$$\frac{-b}{a} = 0$$

$$-\alpha\beta < 0$$

$$\frac{c}{a} < 0$$

Statement (ii) is wrong.

$$\sqrt{D} = \sqrt{b^2 - 4ac}$$

Real roots then  $D > 0$

Because  $b^2 - 4ac > 0$

Statement (i) right.

11. (D)  $a^2 + b^2 + c^2 - ab - bc - ca$   
equation is multiple by 2 and divided 2

$$\frac{1}{2}(a-b)^2 + (b-c)^2 + (c-a)^2$$

neither statements required because result of square is always positive.

12.(D) Statement (i)  $x > y$   
 $x = 1, y = -1$

$$\frac{1+1}{1+1} = \frac{1+1}{1+1}$$

$$1 = 1$$

Statement I wrong

Statement (ii)

$$x^2 + y^2 - 2xy > 0$$

$$(x-y)^2 > 0$$

$(x-y)^2$  is always greater than zero

$$x = 1, y = -1$$

$$(2)^2 > 0$$

$$x = -1, y = 1$$

$$(-2)^2 > 0$$

Statement II is right.

13. (D)  $x^2 + 4x + 4 = 0$   
 $(x+2)(x+2) = 0$   
 $x^2 - x + 1 = 0$   
 $x = -2, -2$   
 $4x^2 - 4x + 4 = 0$

$$-\frac{b}{a} = \frac{4}{4}$$

$$\frac{c}{a} = \frac{4}{4}$$

$$-\frac{b}{a} = \frac{1}{1} = \alpha + \beta$$

$$\frac{c}{a} = \frac{1}{1} = \alpha \beta$$

$$\alpha + \beta = 1, \alpha\beta = 1$$

Infinitely many.

CDS - [2021-II]

### Mother's Advance Maths • Algebra [Previous Year Questions]

1.  $\frac{a^2 - b^2}{a^2 + b^2} > \frac{a - b}{a + b}$  जहाँ  $a > b > 0$
2.  $\frac{a^3 + b^3}{a^2 + b^2} > \frac{a^2 + b^2}{a + b}$  केवल तब, जब  $a > b > 0$   
उपर्युक्त में से कौन-सा/कौन-से सही है/हैं ?  
 (A) Only 1/केवल 1  
 (B) Only 2/केवल 2  
 (C) Both 1 and 2/ 1 और 2 दोनों  
 (D) Neither 1 nor 2/ न तो 1, न ही 2
11. If  $\frac{ay - bx}{c} = \frac{cx - ax}{b} = \frac{bz - cy}{a}$ , then which of

the following is/are correct ?

यदि  $\frac{ay - bx}{c} = \frac{cx - ax}{b} = \frac{bz - cy}{a}$  है, तो निम्नलिखित में कौन-सा/कौन-से सही है/हैं ?

$$1. \frac{x}{a} = \frac{y}{b}$$

$$2. \frac{x + y + z}{a + b + c} = \frac{z}{c}$$

Select the correct answer using the code given below :

- नीचे दिए कूट का प्रयोग कर सही उत्तर चुनिए :  
 (A) Only 1/केवल 1  
 (B) Only 2/केवल 2  
 (C) Both 1 and 2/ 1 और 2 दोनों  
 (D) Neither 1 nor 2/ न तो 1 न ही 2

### Solution

1. (D) Put  $x = 7$   
 $6 \times 5 \times 3 = 90$   
 $= 90 - 90$   
 $= 0$   
 It satisfies ... (D)
2. (C)  $2x^2 + xy - 3y^2$   
 $(x - y)(2x + 3y)$   
 factors  $\rightarrow x - y$  &  $2x + 3y$   
 sum of factors  $\rightarrow x - y + 2x + 3y$   
 $= 3x + 2y$
3. (D) If an equation has no real roots,  $D = b^2 - 4ac < 0$   
 $4x^2 + 9x + 6 = 0$   
 $D = 81 - 4 \times 4 \times 6$   
 $= 81 - 96$   
 $= -15 < 0$   
 $\therefore$  it satisfies our condition.
4. (B)  $\alpha + \beta = 7$   
 $\alpha\beta = 12$   
 $\Rightarrow \alpha = 4, \beta = 3$   
 $\Rightarrow \alpha_1 = 2, \beta_1 = 6$   
 equation  $\rightarrow x^2 - (\alpha + \beta)x + \alpha\beta = x^2 - 8x + 12 = 0$
5. (D)  $x^2 - kx + 2 = 0$   
 Roots are real and distinct.  
 So,  
 $b^2 - 4ac > 0$   
 $\Rightarrow k^2 - 4(1)(2) > 0$   
 $K^2 > 8$   
 $K > 2\sqrt{2}$  or  $k < -2\sqrt{2}$
6. (A) If  $\alpha + \beta + \gamma = \alpha\beta + \beta\gamma + \gamma\alpha$  ..... (i)  
 then,

$$\begin{aligned} & (1 - \alpha)(1 - \beta)(1 - \gamma) \\ &= (1 - \alpha - \beta + \alpha\beta)(1 - \gamma) \\ &= (1 - \alpha - \beta + \alpha\beta - \gamma + \alpha\gamma + \gamma\beta - \alpha\beta\gamma) \\ &= (1 - \alpha\beta\gamma + (\alpha\beta + \gamma\beta + \alpha\gamma) - (\alpha + \beta + \gamma)) \end{aligned}$$

from equation ..... (i)

$$1 - \alpha\beta\gamma$$

7. (B)  $ax^2 - 4ax + 15 = 0$   
 let roots are  $\alpha + \beta$   
 one root is  $\frac{3}{2}$

$$a \times \left(\frac{3}{2}\right)^2 - 4a\left(\frac{3}{2}\right) + 15 = 0$$

$$a \times \frac{9}{4} - 6a + 15 = 0$$

$$\frac{15a}{4} = 15$$

$$a = 4$$

$$\text{equation} = 4x^2 - 16x + 15 = 0$$

$$\alpha + \beta = \frac{+16}{4} = 4$$

$$\Rightarrow \beta = 4 - \frac{3}{2} = \frac{5}{2}$$

$$\Rightarrow \alpha^2 + \beta^2 = \frac{9}{4} + \frac{25}{4} = \frac{34}{4} = \frac{17}{2}$$

8. (D)  $2x - 3y - 7 = 0$  Then,

$$2x - 3y = 7$$

Cubing both side

$$8x^3 - 27y^3 - 36x^2y + 54xy^2 = 343$$

$$8x^3 - 36x^2y + 54xy^2 - 27y^3 - 340 = 3$$

9. (C)  $\frac{x}{b+c-a} = \frac{y}{b-c-a} = \frac{z}{a-b-c} = K$

Put C = 0

$$x = k(b-a) \quad x = y$$

$$y = k(b-a)$$

$$z = K(a+b)$$

Now put the value of x, y, z in question

$$\Rightarrow x^2 + x^2 + z^2 - 2/x^2 - 2x/z + 2z/x$$

$$\Rightarrow z^2$$

$$\Rightarrow k^2(a+b)^2$$

or

$$k^2(a+b+c)^2$$

Method-2

Put,

$$a = b = c = 1$$

10. (A)  $\frac{a^2 - b^2}{a^2 + b^2} > \frac{a-b}{a+b}$

Where (a > b > 0)

By putting value of a & b it holds.

11. (C) We know,

If  $\frac{a}{b} = \frac{c}{d} = \frac{e}{f} = K$

then,  $\frac{a+c+e}{b+d+f} = k$

(i)  $\frac{x}{a} = \frac{y}{b} = \frac{z}{c} = k$

(ii)  $\frac{x+y+z}{a+b+c} = k = \frac{z}{c}$

Both are correct.

# ALGEBRA

CDS - [2021-2016]

## बीजगणित

(Previous Year Questions)

### CDS [2021-I]

1. If  $a + b + c = 0$ , then which of the following are correct?

यदि  $a + b + c = 0$ , है, तो निम्नलिखित में से कौन-से सही हैं ?  
(CDS-2021)

- i)  $a^3 + b^3 + c^3 = 3abc$
- ii)  $a^2 + b^2 + c^2 = -2(ab + bc + ca)$
- iii)  $a^3 + b^3 + c^3 = -3ab(a + b)$

Select the correct answer using the code given below

नीचे दिए गए कूट का प्रयोग कर सही उत्तर चुनिए :

- |                  |                  |
|------------------|------------------|
| (A) 1 and 2 only | (B) 2 and 3 only |
| (C) 1 and 3 only | (D) 1, 2 and 3   |

2. If  $\frac{x}{a} + \frac{y}{b} = a + b$  and  $\frac{x}{a^2} + \frac{y}{b^2} = 2$  then what is

$\frac{x}{a^2} - \frac{y}{b^2}$  equal to ?

यदि  $\frac{x}{a} + \frac{y}{b} = a + b$  और  $\frac{x}{a^2} + \frac{y}{b^2} = 2$  है, तो  $\frac{x}{a^2} - \frac{y}{b^2}$  किसके बराबर है ?  
(CDS-2021)

- |        |        |
|--------|--------|
| (A) -2 | (B) -1 |
| (C) 0  | (D) 1  |

3. If  $(x - k)$  is the HCF of  $x^2 + ax + b$  and  $x^2 + cx + d$ , then what is the value of  $k$  ?

यदि  $x^2 + ax + b$  और  $x^2 + cx + d$  का म.स. (एच.सी.एफ.)  $(x - k)$  है, तो  $k$  का मान क्या है ?  
(CDS-2021)

- |                           |                           |
|---------------------------|---------------------------|
| (A) $\frac{d - b}{c - a}$ | (B) $\frac{d - b}{a - c}$ |
| (C) $\frac{d + b}{c + a}$ | (D) $\frac{d - b}{c + a}$ |

4. Consider the following statements :

- i) If  $x$  is directly proportional to  $z$  and  $y$  is directly proportional to  $z$ , then  $(x^2 - y^2)$  is directly proportional to  $z^2$ .
- ii) If  $x$  is inversely proportional to  $z$  and  $y$  is inversely proportional to  $z$ , then  $(xy)$  is inversely proportional to  $z^2$ .

Which of the above statements is/are correct?

निम्नलिखित कथनों पर विचार कीजिए : (CDS-2021)

i) यदि  $x, z$  के अनुक्रमानुपाती हैं और  $y, z$  के अनुक्रमानुपाती हैं, तो  $(x^2 - y^2)$ ,  $z^2$  के अनुक्रमानुपाती हैं।

ii) यदि  $x, z$  के व्युक्तमानुपाती हैं और  $y, z$  के व्युक्तमानुपाती हैं, तो  $(xy)$ ,  $z^2$  के व्युक्तमानुपाती हैं।

उपरोक्त कथनों में से कौन-सा/से सही है/हैं ?

- |                   |                      |
|-------------------|----------------------|
| (A) i only        | (B) ii only          |
| (C) Both i and ii | (D) Neither i nor ii |

5. What is  $\frac{8x}{1-x^4} - \frac{4x}{x^2+1} + \frac{x+1}{x-1} + \frac{x-1}{x+1}$  equal to ?

$\frac{8x}{1-x^4} - \frac{4x}{x^2+1} + \frac{x+1}{x-1} + \frac{x-1}{x+1}$  किसके बराबर है ?

(CDS-2021)

- |       |       |
|-------|-------|
| (A) 0 | (B) 1 |
| (C) 2 | (D) 4 |

6. If  $x(x-1)(x-2)(x-3) + 1 = k^2$ , then which one of the following is a possible expression for  $k$  ?

यदि  $x(x-1)(x-2)(x-3) + 1 = k^2$  है, तो निम्नलिखित में से कौन-सा एक व्यंजक (एक्सप्रेशन)  $k$  के लिए संभव है ?

(CDS-2021)

- |                    |                    |
|--------------------|--------------------|
| (A) $x^2 - 3x + 1$ | (B) $x^2 - 3x - 1$ |
| (C) $x^2 + 3x - 1$ | (D) $x^2 - 2x - 1$ |

7. What is  $\frac{1}{bc(a-b)(a-c)} +$

$\frac{1}{ca(b-c)(b-a)} + \frac{1}{ab(c-a)(c-b)}$  equal to.

$\frac{1}{bc(a-b)(a-c)} + \frac{1}{ca(b-c)(b-a)} +$

$\frac{1}{ab(c-a)(c-b)}$  किसके बराबर है ? (CDS-2021)

- |                    |       |
|--------------------|-------|
| (A) $a + b + c$    | (B) 3 |
| (C) $ab + bc + ca$ | (D) 0 |

**Mother's एण्डवार्स • वीजगणित**

8. For how many real values of  $k$  is  $6kx^2 + 12kx - 24x + 16$  a perfect square for every integer  $x$ ?  
 के कितने वास्तविक मानों के लिए  $6kx^2 + 12kx - 24x + 16$  प्रत्येक पूर्णक  $x$  के लिए एक पूर्ण बर्ग है? (CDS-2021)
- (A) 0 (B) 1  
 (C) 2 (D) 4
9. If  $x + \frac{1}{x} = \frac{5}{2}$ , then what is  $x^4 - \frac{1}{x^4}$  equal to?  
 यदि  $x + \frac{1}{x} = \frac{5}{2}$  है, तो  $x^4 - \frac{1}{x^4}$  किसके बराबर है? (CDS-2021)
- (A)  $\frac{195}{16}$  (B)  $\frac{255}{16}$  (C)  $\frac{625}{16}$  (D) 0
10. If the equation  $4x^2 - 2kx + 3k = 0$  has equal roots, then what are the value of  $k$ ?  
 यदि समीकरण  $4x^2 - 2kx + 3k = 0$  के मूल एक समान हैं, तो  $k$  के मान क्या हैं? (CDS-2021)
- (A) 4,12 (B) 4,8  
 (C) 0,12 (D) 0,8
11. If the sum as well as the product of the roots of the equation  $px^2 - 6x + q = 0$  is 6, then what is  $(p + q)$  to?  
 यदि समीकरण  $px^2 - 6x + q = 0$  के मूलों का युग्मफल और योगफल दोनों ही 6 है, तो  $(p + q)$  किसके बराबर है? (CDS-2021)
- (A) 8 (B) 7  
 (C) 6 (D) 5
12. If  $\frac{1}{1 \times 2} + \frac{1}{2 \times 3} + \frac{1}{3 \times 4} + \dots + \frac{1}{n(n+1)} = \frac{99}{100}$  then what is the value of  $n$ ?  
 यदि  $\frac{1}{1 \times 2} + \frac{1}{2 \times 3} + \frac{1}{3 \times 4} + \dots + \frac{1}{n(n+1)} = \frac{99}{100}$  है, तो  $n$  का मान क्या है? (CDS-2021)
- (A) 98 (B) 99  
 (C) 100 (D) 101

**Solution**

1. (A)  $\because a + b + c = 0$

then,

$$a^3 + b^3 + c^3 - 3abc = 0$$

$$\text{and } a^2 + b^2 + c^2 + 2(ab + bc + ca) = 0$$

$\therefore$  option (A) is correct

2. (C) ATQ,

$$\frac{x}{a} + \frac{y}{b} = a + b \quad \dots\dots\dots(1)$$

$$\frac{x}{a^2} + \frac{y}{b^2} = 2 \quad \dots\dots\dots(2)$$

multiplying by  $b$  in (2) and subtracting from (1) then

$$\Rightarrow \frac{x}{a} + \frac{y}{b} - \left( \frac{xb}{a^2} + \frac{yb}{b^2} \right) = a + b - 2b$$

$$\Rightarrow \left( \frac{x}{a} - \frac{xb}{a^2} \right) + \left( \frac{y}{b} - \frac{yb}{b^2} \right) = a - b$$

$$\Rightarrow x \left[ \frac{a-b}{a^2} \right] = a - b \Rightarrow \frac{x}{a^2} = 1$$

$$\Rightarrow x = a^2$$

Putting  $x = a^2$  in (1)

$$\Rightarrow \frac{a^2}{a} + \frac{y}{b} = a + b$$

$$\Rightarrow \frac{y}{b} = a + b - a = b$$

$$\Rightarrow y = b^2$$

hence,

$$\begin{aligned} \Rightarrow \frac{x}{a^2} - \frac{y}{b^2} &= \frac{a^2}{a^2} - \frac{b^2}{b^2} \\ \Rightarrow 1 - 1 &= 0 \end{aligned}$$

3. (B) HCF =  $x - k$

and  $x^2 + ax + b \quad \dots\dots\dots(i)$

$x^2 + cx + d \quad \dots\dots\dots(ii)$

Put  $x = k$  in eq. (i) and (ii)

$$\therefore k^2 + ka + b = 0$$

$$k^2 + kc + d = 0$$

$$\Rightarrow k^2 + ka + b = k^2 + kc + d$$

$$\Rightarrow k = \frac{d - b}{a - c}$$

4. (C)  $x \propto z \Rightarrow x = kz$

$$y \propto z \Rightarrow y = cz$$

$$\therefore x^2 - y^2 = (k^2 - c^2)z^2$$

$$\Rightarrow x^2 - y^2 \propto z^2$$

$$\text{and } x \propto \frac{1}{z} \qquad \qquad x = \frac{k}{z}$$

$$y \propto \frac{1}{z} \qquad \qquad y = \frac{c}{z}$$

$$\Rightarrow xy = \frac{1}{z}(kc)$$

$$\Rightarrow xy \propto \frac{1}{z}$$

**Mother's Advance Maths • Algebra [Previous Year Questions]**

5. (A)  $\frac{8x}{1-x^4} - \frac{4x}{x^2+1} + \frac{x+1}{x-1} - \frac{x-1}{x+1}$

Put  $x = 0$

$$0 - 0 - 1 - (-1) = 0$$

6. (A)  $x(x-1)(x-2)(x-3) + 1 = k^2$

Put  $x = 4$

$$4 \times 3 \times 2 \times 1 + 1 = k^2$$

$$\therefore k = \pm 5$$

(a)  $x^2 - 3x + 1$

put  $x = 4$

$$16 - 12 + 1 = 5$$

7. (D)  $\frac{1}{bc(a-b)(a-c)} + \frac{1}{ca(b-c)(b-a)} +$

$$\frac{1}{ab(c-a)(c-b)}$$

$$\Rightarrow \frac{-a(b-c) - b(c-a) - c(a-b)}{abc(a-b)(b-c)(c-a)}$$

$$\Rightarrow -ab - ac - bc + ab - ac + bc = 0$$

8. (C)  $6kx^2 + 12kx - 24x + 16$

for perfect square  $b^2 = 4ac$

$$\Rightarrow (12k-24)^2 = 4 \times 6k \times 16$$

$$\Rightarrow 12 \times 12(k-2)^2 = 4 \times 16 \times 6k$$

$$\Rightarrow 3k^2 - 12k + 12 = 8k$$

$$\Rightarrow 3k^2 - 20k + 12 = 0$$

$$\Rightarrow b^2 - 4ac = 400 - 144 = 256$$

$$\Rightarrow \sqrt{b^2 - 4ac} = 16$$

$$\Rightarrow k = \frac{20 \pm 16}{6} = 6, \frac{2}{3}$$

9. (B)  $x + \frac{1}{x} = \frac{5}{2}$

$$x^2 + \frac{1}{x^2} = \frac{17}{4}$$

$$x^4 + \frac{1}{x^4} = \frac{257}{16}$$

$$x^4 - \frac{1}{x^4} = \sqrt{\left(\frac{257}{16}\right)^2 - 4} = \frac{255}{16}$$

10. (C)  $4x^2 - 2kx + 3k = 0$

for equal roots  $b^2 = 4ac$

$$\Rightarrow 4k^2 = 48k$$

$$\Rightarrow k = 0, 12$$

11. (B)  $px^2 - 6x + q = 0$

$$\text{sum of roots } \frac{6}{p} = 6 \Rightarrow p = 1$$

$$\text{product } \frac{q}{p} = 6 \Rightarrow q = 6$$

$$\therefore p + q = 7$$

12. (B)  $\frac{1}{1 \times 2} + \frac{1}{2 \times 3} + \frac{1}{3 \times 4} + \dots + \frac{1}{n(n+1)} = \frac{99}{100}$

$$= 1 - \frac{1}{2} + \frac{1}{2} - \frac{1}{3} + \dots - \frac{1}{n+1} = \frac{99}{100}$$

$$= \frac{n+1-1}{n+1} = \frac{99}{100} \Rightarrow n = 99$$

CDS [2020-I]

- 1.** If  $\alpha$  and  $\beta$  are the roots of the quadratic equation  $x^2 + kx - 15 = 0$  such that  $\alpha - \beta = 8$ , then what is the positive value of  $k$ ?  
यदि  $\alpha$  और  $\beta$  द्विघात समीकरण  $x^2 + kx - 15 = 0$  के मूल इस प्रकार हैं कि  $\alpha - \beta = 8$  हैं, तो का धनात्मक मान क्या है ?  
(A) 2 (B) 3  
(C) 4 (D) 5

**2.** If  $(x + k)$  is the HCF of  $x^2 + 5x + 6$  and  $x^2 + 8x + 15$ , then what is the value of  $k$ ?  
यदि  $x^2 + 5x + 6$  और  $x^2 + 8x + 15$  का म.स.  $(x + k)$  है तो  $k$  का मान क्या है ?  
(A) 5 (B) 3  
(C) 2 (D) 1

**3.** If  $x^2 + 9y^2 = 6xy$  then what is  $y : x$  equal to?  
यदि  $x^2 + 9y^2 = 6xy$  है तो  $y : x$  किसके बराबर है ?  
(A) 1 : 3 (B) 1 : 2  
(C) 2 : 1 (D) 3 : 1

**4.** What is  $\frac{1}{a^{m-n}-1} + \frac{1}{a^{n-m}-1}$  equal to?  
 $\frac{1}{a^{m-n}-1} + \frac{1}{a^{n-m}-1}$  किसके बराबर है ?  
(A) 1 (B) -1  
(C) 0 (D)  $2a^{m-n}$

**5.** If  $\frac{c}{a} = \sqrt[3]{6}$  and  $z = \sqrt[3]{6}$  then which one of the following is correct?  
यदि  $x = \sqrt{2}$ ,  $y = 3\sqrt{3}$  और  $z = \sqrt[3]{6}$  हैं तो निम्नलिखित में से कौन-सा एक सही है ?  
(A)  $y < x < z$  (B)  $z < x < y$   
(C)  $z < y < x$  (D)  $x < y < z$

**6.** What is the point on the  $xy$ -plane satisfying  $5x + 2y = 7xy$  and  $10x + 3y = 8xy$ ?  
 $xy$ -समतल पर  $5x + 2y = 7xy$  और  $10x + 3y = 8xy$  को संतुष्ट करने वाला बिन्दु कौन-सा है ?  
(A)  $\left(-1, \frac{1}{6}\right)$  (B)  $\left(\frac{1}{6}, -1\right)$   
(C)  $\left(1, \frac{1}{6}\right)$  (D)  $\left(-\frac{1}{6}, 1\right)$

7. If  $\left( x^{\frac{8}{x^8}} \right) = 47$ , what is the value of  $\left( x^{\frac{6}{x^6}} \right) = ?$   
यदि  $\left( x^{\frac{8+1}{x^8}} \right)$  हैं, तो  $\left( x^{\frac{6-1}{x^6}} \right)$  का मान क्या हैं?  
(A) 36 (B) 27  
(C) 18 (D) 9

8. What are the values of p and q respectively, if  $(x - 1)$  and  $(x + 2)$  divide the polynomial  $x^3 + 4x^2 + px + q$ ?  
प और q के मान क्रमशः क्या हैं, यदि  $(x - 1)$  और  $(x + 2)$  बहुपद  $x^3 + 4x^2 + px + q$  को विभाजित करते हैं?  
(A) 1, -6 (B) 2, -6  
(C) 1, 6 (D) 2, 6

9. If  $5^{x+1} - 5^{x-1} = 600$ , then what is the value of  $10^{2x}$ ?  
यदि  $5^{x+1} - 5^{x-1} = 600$  है, तो  $10^{2x}$  का मान क्या है?  
(A) 1 (B) 1000  
(C) 100000 (D) 1000000

10. If  $f(x)$  is divided by  $(x - \alpha)(x - \beta)$  where  $\alpha \neq \beta$ , then what is the remainder?  
यदि  $f(x)$  को  $(x - \alpha)(x - \beta)$  से विभाजित किया जाए, जहाँ  $\alpha \neq \beta$  हैं, तो शेषफल क्या है?  
(A)  $\frac{(x - \alpha)f(\alpha) - (x - \beta)f(\beta)}{\alpha - \beta}$   
(B)  $\frac{(x - \alpha)f(\beta) - (x - \beta)f(\alpha)}{\alpha - \beta}$   
(C)  $\frac{(x - \beta)f(\alpha) - (x - \alpha)f(\beta)}{\alpha - \beta}$   
(D)  $\frac{(x - \beta)f(\beta) - (x - \alpha)f(\alpha)}{\alpha - \beta}$

11. What is the area of the triangle having side lengths  $\frac{y}{z}, \frac{z}{x}, \frac{x}{y}, \frac{x}{y}, \frac{y}{z}$ ?  
उस त्रिभुज का क्षेत्रफल क्या है जिसकी भुजाओं की लम्बाई  $\frac{y}{z}, \frac{z}{x}, \frac{x}{y}, \frac{x}{y}, \frac{y}{z}$  है?  
(A)  $\frac{(x+y+z)2}{xyz}$  (B)  $\frac{\sqrt{xyz}}{x+y+z}$   
(C)  $\frac{x}{y} + \frac{y}{z} + \frac{z}{x}$  (D)  $\sqrt{\frac{xy+yz+zx}{xyz}}$

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8. (A) If  $(x-1)$  and  $(x+2)$  divide the polynomial  $x^3 + 4x^2 + px + q$

Then  $x = 1$  and  $x = -2$  both will satisfy equation  $x^3 + 4x^2 + px + q$

Put  $x = 1$  in equation  $x^3 + 4x^2 + px + q$

$$\Rightarrow 1 + 4 + p + q = 0$$

$$\Rightarrow p + q = -5 \quad \dots \dots \dots \text{(i)}$$

Put  $x = -2$  in equation  $x^3 + 4x^2 + px + q$

$$\Rightarrow -8 + 16 - 2p + q = 0$$

$$\Rightarrow -2p + q = -8 \quad \dots \dots \dots \text{(ii)}$$

Subtract (ii) from (i)

$$\Rightarrow 3p = 3$$

$$\Rightarrow p = 1$$

Put the value of  $p$  in equation (i)

$$q = -6$$

9. (D) Given  $5^{x+1} - 5^{x-1} = 600 \dots \dots \dots \text{(i)}$

$$\text{Also, } 5^4 - 5^2 = 625 - 25 = 600 \quad \dots \dots \dots \text{(ii)}$$

From (i) and (ii)

$$\Rightarrow x + 1 = 4$$

$$\Rightarrow x = 3$$

$$\text{Hence, } 10^{2x} = (10)^5 = 1000000$$

10. (C)  $f(x)$  is divided by  $(x - \alpha)(x - \beta)$  where  $\alpha \neq \beta$

Then  $f(x) = (x - \alpha)(x - \beta)g(x) + (ax + b) \dots \dots \text{(i)}$

where  $g(x)$  is quotient and  $(ax + b)$  is linear remainder

Put  $x = \alpha$  in ..... (i)

$$f(\alpha) = a + b \quad \dots \dots \dots \text{(ii)}$$

Put  $x = \beta$  in ..... (i)

$$f(\beta) = \alpha\beta + b \quad \dots \dots \dots \text{(iii)}$$

Subtract (iii) from (ii)

$$f(\alpha) - f(\beta) = aa + b - (\alpha\beta + b) \quad \dots \dots \dots \text{(iii)}$$

$$\alpha = \frac{f(\alpha) - f(\beta)}{\alpha - \beta} \quad \dots \dots \dots \text{(iv)}$$

Put the value of 'a' in equation (ii)

$$f\alpha = \left[ \frac{f(\alpha) - f(\beta)}{\alpha - \beta} \right] a + b$$

$$\alpha f(\alpha) - \beta f(\alpha) = \alpha f(\alpha) - \alpha f(\beta) + b(\alpha - \beta)$$

$$b = \frac{\alpha f(\beta) - \beta f(\alpha)}{\alpha - \beta} \quad \dots \dots \dots \text{(v)}$$

Remainder =  $(ax + b)$

$$= \frac{f(\alpha)x - f(\beta)x}{\alpha - \beta} + \frac{\alpha f(\beta) - \beta f(\alpha)x}{\alpha - \beta}$$

$$= \frac{(x - \beta)f(\alpha) - (x - \alpha)f(\beta)}{\alpha - \beta}$$

11. (C) Triangle having side lengths

$$\frac{y}{z} + \frac{z}{x}, \frac{z}{x} + \frac{x}{y}, \frac{x}{y} + \frac{y}{z}$$

As we can see from here all sides are of different length, then the triangle will be a scalene triangle,

$$a = \cot\theta \cdot \tan\theta \cdot \cot2\theta \cdot \tan2\theta \cdot \cot3\theta \cdot \tan3\theta \dots \dots$$

Then the area of triangle = where  $a, b, c$  are the sides of the triangle

$$a = \frac{y}{z} + \frac{z}{x}, b = \frac{z}{x} + \frac{x}{y}, c = \frac{x}{y} + \frac{y}{z}$$

$$\text{Here, } s = \frac{\frac{x}{y} + \frac{y}{z} + \frac{z}{x} + \frac{z}{x} + \frac{x}{y} + \frac{y}{z}}{2} = \frac{x}{y} + \frac{y}{z} + \frac{z}{x}$$

$$s = \frac{x}{y} + \frac{y}{z} + \frac{z}{x}$$

Put the value of each term then you will get

$$\text{Area} = \sqrt{s(s-a)(s-b)(s-c)} = \sqrt{\frac{x}{y} + \frac{y}{z} + \frac{z}{x}}$$

Hence option C is correct

12. (B) Here, the given equation is  $5x + 9y = 7$   
Under the condition:  $x$  &  $y$  should be integer b/w  $-500$  to  $500$ .

Now, we have to check the value by hit and trial method and try to observe the relation  
Here, 1<sup>st</sup> convert the given equation as

$$y = \frac{7 - 5x}{9}$$

Try to put some value of  $x$  (integer) to get  $y$  as integer

x	y
-1	12/9
-4	3
-13	8
-22	13
-31	18

Here, we can see that when we put  $x = -4, -13, -22, -31 \dots \dots \dots$  (common difference b/w each term = 9). Then  $y = \text{integer value}$ . As  $x \in [-500, 500]$

X may be  $-495, -486, \dots \dots \dots -4, -13, -22, \dots \dots \dots, 495$  (common difference = 9)

It is nothing but an A.P having 1<sup>st</sup> term = -495 & last term = 495 and d (common difference) = 9

Then, no. of possible value (n) = no. of terms of the A.P





**Mother's Advance Maths • Algebra [Previous Year Questions]**

**CDS [2019-I]**

1. If  $\frac{a}{b+c} = \frac{b}{c+a} = \frac{c}{a+b}$  then which one of the following statements is correct?

यदि  $\frac{a}{b+c} = \frac{b}{c+a} = \frac{c}{a+b}$  है, तो निम्नलिखित में से कौन-सा कथन सही हैं ?

- (A) Each fraction is equal to 1 or -1  
प्रत्येक भिन्न 1 या -1 के बराबर हैं।  
(B) Each fraction is equal to  $\frac{1}{2}$  or 1  
प्रत्येक भिन्न  $\frac{1}{2}$  या 1 के बराबर हैं।  
(C) Each fraction is equal to  $\frac{1}{2}$  or -1  
प्रत्येक भिन्न  $\frac{1}{2}$  या -1 के बराबर हैं।  
(D) Each fraction is equal to 1.2 only  
प्रत्येक भिन्न केवल  $\frac{1}{2}$  के बराबर हैं।

2. If  $3^x = 4^y = 12^z$ , then z is equal to.

यदि  $3^x = 4^y = 12^z$  है, तो z किसके बराबर हैं ?

- (A) xy (B) x + y  
(C)  $\frac{xy}{x+y}$  (D)  $4x + 3y$

3. If  $(4a + 7b)(4c - 7d) = (4a - 7b)(4c + 7d)$ , then which one of the following is correct ?

यदि  $(4a + 7b)(4c - 7d) = (4a - 7b)(4c + 7d)$  है, तो निम्नलिखित में से कौन-सा एक सही हैं ?

- (A)  $\frac{a}{b} = \frac{c}{d}$  (B)  $\frac{a}{d} = \frac{c}{b}$  (C)  $\frac{a}{b} = \frac{d}{c}$  (D)  $\frac{4a}{7b} = \frac{c}{d}$

4. Given that the polynomial  $(x^2 + ax + b)$  leaves the same remainder when by  $(x - 1)$  or  $(x + 1)$ . What are the values of a and b respectively ?

दिया गया है कि बहुपद  $(x^2 + ax + b)$  को  $(x - 1)$  अथवा  $(x + 1)$  से विभाजित करने पर शेषफल समान रहता है। a और b के मान क्रमशः क्या हैं ?

- (A) 4 and 0 (B) 0 and 3  
(C) 3 and 0 (D) 0 and any integer

5. What is  $\frac{(x-y)^3 + (y-z)^3 + (z-x)^3}{3(x-y)(y-z)(z-x)}$  equal to / किसके बराबर हैं ?

- (A) 1 (B) 0  
(C)  $\frac{1}{3}$  (D) 3

6. If  $a^x = b^y = c^z$  and  $b^2 = ac$ , then what is

$$\frac{1}{x} + \frac{1}{z}$$

यदि  $a^x = b^y = c^z$  और  $b^2 = ac$  है, तो  $\frac{1}{x} + \frac{1}{z}$  किसके बराबर हैं ?

- (A)  $\frac{1}{y}$  (B)  $-\frac{1}{y}$  (C)  $\frac{2}{y}$  (D)  $-\frac{2}{y}$

7. If p and q are the roots of the equation  $x^2 - 15x + r = 0$  and  $p - q = 1$ , then what is the value of r ?

यदि p और q समीकरण  $x^2 - 15x + r = 0$  के मूल हैं और  $p - q = 1$  हैं तो r का मान क्या है ?

- (A) 55 (B) 56  
(C) 60 (D) 64

8. For the inequation  $x^2 - 7x + 12 > 0$ , which one of the following is correct ?

असमिका  $x^2 - 7x + 12 > 0$  के लिए, निम्नलिखित में से कौन-सा एक सही है ?

- (A)  $3 < x < 4$  (B)  $-\infty < x < 3$  only  
(C)  $4 < x < \infty$  only  
(D)  $-\infty < x < 3$  or  $4 < x < \infty$

9. The expression  $5^{2n} - 2^{3n}$  has a factor ?

व्यंजक  $5^{2n} - 2^{3n}$  का गुणनखंड है ?

- (A) 3 (B) 7  
(C) 17 (D) None of these

10. For  $x = \frac{4\sqrt{6}}{\sqrt{2} + \sqrt{3}}$ , what is the value of  $\frac{x+2\sqrt{2}}{x-2\sqrt{2}} + \frac{x+2\sqrt{3}}{x-2\sqrt{3}}$  ?

$x = \frac{4\sqrt{6}}{\sqrt{2} + \sqrt{3}}$  के लिए  $\frac{x+2\sqrt{2}}{x-2\sqrt{2}} + \frac{x+2\sqrt{3}}{x-2\sqrt{3}}$  का मान क्या है ?

- (A) 1 (B)  $\sqrt{2}$  (C)  $\sqrt{3}$  (D) 2

11. For any two real numbers a and b.

$$\sqrt{(a-b)^2} + \sqrt{(b-a)^2}$$

किन्हीं दो वास्तविक संख्याओं a और b के लिए

$$\sqrt{(a-b)^2} + \sqrt{(b-a)^2}$$

होगा।

- (A) always zero/हमेशा शून्य  
(B) never zero/कभी भी शून्य नहीं  
(C) positive only if  $a \neq b$ /धनात्मक केवल यदि  $a \neq b$   
(D) positive if an only if  $a > b$

धनात्मक यदि और केवल यदि  $a > b$

12. If  $a : b = c : d = 1 : 6$ , then what is the value of

$$\frac{a^2 + c^2}{b^2 + d^2} ?$$

यदि  $a : b = c : d = 1 : 6$  हैं, तो  $\frac{a^2 + c^2}{b^2 + d^2}$  का मान क्या हैं?

- (A)  $\frac{1}{600}$       (B)  $\frac{1}{60}$       (C)  $\frac{1}{36}$       (D)  $\frac{1}{6}$

13. For  $x > 0$ , what is the minimum value of  $x +$

$$\frac{x+2}{2x} ?$$

$x > 0$  के लिये  $x + \frac{x+2}{2x}$  का न्यूनतम मान क्या हैं?

- (A) 1      (B) 2      (C)  $2\frac{1}{2}$

(D) Cannot be determined/निर्धारित नहीं किया जा सकता

14. If  $\frac{1+px}{1-px} \sqrt{\frac{1-qx}{1+qx}} = 1$  then what are the non-zero solutions of  $x$ ?

यदि  $\frac{1+px}{1-px} \sqrt{\frac{1-qx}{1+qx}} = 1$  हैं, तब  $x$  के शून्येतर हल क्या हैं?

- (A)  $\pm \frac{1}{p} \sqrt{\frac{2p-q}{q}}$ ,  $2p \neq q$       (B)  $\pm \frac{1}{p} \sqrt{p-q}$ ,  $p \neq q$

- (C)  $\pm \frac{p}{q} \sqrt{\frac{2p-q}{q}}$ ,  $2p \neq q$       (D)  $\pm \frac{p}{q} \sqrt{2p-q}$ ,  $2p \neq q$

15. Which of the following pair of numbers is the solution of the equation  $3^{x+2} + 3^x = 10$ ?

संख्याओं की निम्नलिखित में से कौन-सा युग्म, समीकरण  $3^{x+2} + 3^x = 10$  का हल हैं?

- (A) 0, 2      (B) 0, -2  
(C) 1, -1      (D) 1, 2

16. If  $a$ ,  $b$  and  $c$  are positive integers such that

$$\frac{1}{a+} \frac{1}{b+} \frac{1}{c+} = \frac{16}{23} \text{ then what is the mean of } a,$$

b and c?

यदि  $a$ ,  $b$  और  $c$  धनात्मक पूर्ण संख्याएँ इस प्रकार हैं कि

$$\frac{1}{a+} \frac{1}{b+} \frac{1}{c+} = \frac{16}{23} \text{ हैं, तब } a, b \text{ और } c \text{ का माध्य क्या हैं?}$$

- (A) 1      (B) 2  
(C) 1.33      (D) 2.33

**CDS [2019-II]**

17. What is  $(x-a)(x-b)(x-c)$  equal to?

$(x-a)(x-b)(x-c)$  किसके बराबर हैं?

- (A)  $x^3 - (a+b+c)x^2 + (bc+ca+ab)x - abc$   
(B)  $x^3 - (a+b+c)x^2 + (bc+ca+ab)x - abc$   
(C)  $x^3 - (a+b+c)x^2 + (a+b+c)x - abc$   
(D)  $x^3 + (a+b+c)x^2 + (a+b+c)x + abc$

18. The quotient when  $x^4 - x^2 + 7x + 5$  is divided by  $(x+2)$  is  $ax^3 + bx^2 + cx + d$ . What are the values of  $a$ ,  $b$ ,  $c$  and  $d$  respectively?

जब  $x^4 - x^2 + 7x + 5$  को  $(x+2)$  से विभाजित किया जाता हैं, तो भागफल  $ax^3 + bx^2 + cx + d$  आता हैं।  $a$ ,  $b$ ,  $c$  और  $d$  के मान क्रमशः क्या हैं?

- (A) 1, -2, 3, 1      (B) -1, 2, 3, 1  
(C) 1, -2, -3, -1      (D) -1, 2, -3, -1

19. Two numbers  $p$  and  $q$  are such that the quadratic equation  $px^2 + 3x + 2q = 0$  has -6 as the sum and the product of the roots. What is the value of  $(p-q)$ ?

दो संख्याएँ  $p$  और  $q$  इस प्रकार हैं कि द्विघात समीकरण  $px^2 + 3x + 2q = 0$  के मूलों का योगफल और गुणनफल -6 हैं।  $(p-q)$  का मान क्या हैं?

- (A) -1      (B) 1      (C) 2      (D) 3

20. What is the value of.

$$\frac{(x-y)^3 + (y-z)^3 + (z-x)^3}{9(x-y)(y-z)(z-x)} ?$$

का मान क्या हैं?

- (A) 0      (B)  $\frac{1}{3}$       (C)  $\frac{1}{9}$       (D) 1

21. What is the LCM of the polynomials  $x^3 + 3x^2 + 3x + 1$ ,  $x^3 + 5x^2 + 5x + 4$  and  $x^2 + 5x + 4$ ?

बहुपदों  $x^3 + 3x^2 + 3x + 1$ ,  $x^3 + 5x^2 + 5x + 4$  और  $x^2 + 5x + 4$  का अनुत्तम समापवर्ती ल.स क्या हैं?

- (A)  $(x+1)^3(x+4)(x^2+x+1)$   
(B)  $(x+4)(x^2+x+1)$       (C)  $(x+1)(x^2+x+1)$   
(D)  $(x+1)^2(x+4)(x^2+x+1)$

Mother's Advance Maths • Algebra [Previous Year Questions]



### Solution

1. (C)  $\frac{a}{(b+c)} = \frac{b}{(c+a)} = \frac{c}{(a+b)}$

Taking reciprocal and adding 1 to each ratio we get

$$\frac{(b+c)}{a+1} = \frac{b}{(c+a)+1} = \frac{c}{(a+b)+1}$$

Or

$$\frac{(a+b+c)}{a} = \frac{(a+b+c)}{b} = \frac{(a+b+c)}{c}$$

So this can only be equal when  $a = b = c$  or  $a + b + c = 0$

When  $a=b=c$  we get  $\frac{a}{(b+c)} = \frac{1}{2}$

When  $a + b + c = 0$  we get  $b + c = -a$

So  $\frac{a}{(b+c)} = -1$

the ratios are  $\frac{1}{2}$  or  $-1$

2. (C)  $3^x = 4^y = 12^z$

Taking log of all 3 we get

$$x \ln 3 = y \ln 4 = z \ln 12 = k$$

$$z = \frac{k}{\ln 12} = \frac{k}{\ln(3 \times 4)} = \frac{k}{\ln 3 + \ln 4} = \frac{k}{\frac{k}{x} + \frac{k}{y}}$$

$$= \frac{xy}{(x+y)}$$

3. (C)  $(4a + 7b)(4c - 7d) = (4a - 7b)(4c+7d)$

$$\frac{(4a + 7b)}{(4a - 7b)} = \frac{(4a + 7b)}{(4a - 7b)}$$

### Using componendo and dividendo

$$\frac{(4a+7b)}{(4a-7b)} = \frac{(4a+7b)}{(4a-7b)} =$$

$$\frac{(4c + 7d) + (4c - 7d)}{(4c + 7d) - (4c - 7d)}$$

$$\text{Or } \frac{8a}{14b} = \frac{8c}{14d}$$

$$\text{Or } \frac{a}{b} = \frac{c}{d}$$

4. (D) Since  $x^2 + ax + b$  when divided by  $x - 1$  or  $x + 1$  leaves the same remainder

So on putting  $x = 1$  and  $x = -1$  we get the same value  $1 + a + b = 1 - a + b$

$$2a = 0$$

$$a = 0$$

here  $b$  can take any value as it will always get cancelled out

5. (A) We know that when  $a + b + c = 0$ , then  $a^3 + b^3 + c^3 = 3abc$

in the above question,

$$(x - y) + (y - z) + (z - x) = 0$$

Therefore,

$$(x - y)^3 + (y - z)^3 + (z - x)^3 = 3(x - y)(y - z)(z - x)$$

$$\frac{(x - y)^3 + (y - z)^3 + (z - x)^3}{3(x - y)(y - z)(z - x)} = 1$$

6. (C)  $a^x = b^y = c^z = k$

$$a = k^{\frac{1}{x}}$$

$$b = k^{\frac{1}{y}}$$

$$c = k^{\frac{1}{z}}$$

given  $b^2 = ac$ , putting the above values of  $a, b, c$  in the equation we get

$$k^{\frac{2}{y}} = k^{\frac{1}{x}} \cdot k^{\frac{1}{z}}$$

$$\frac{2}{y} = \frac{1}{x} + \frac{1}{z}$$

7. (B) In the below equation

$$x^2 - 15x + r = 0$$

$$\text{sum of roots} = p + q = \frac{-(-15)}{1} = 15$$

(sum of roots for equation  $ax^2 + bx + c$  is  $\frac{-b}{a}$ )

$$\text{product of roots} = pq = \frac{r}{1} = r$$

(product of roots for equation  $ax^2 + bx + c$  is  $\frac{c}{a}$ )

given  $p - q = 1$

also we know that  $p + q = 15$

subtracting the squares of both

$$(p + q)^2 + (p - q)^2 = 15^2 - 1$$

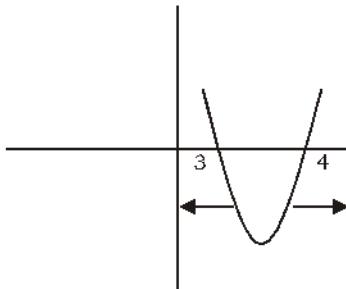
$$p^2 + q^2 + 2pq - p^2 - q^2 + 2pq = 225 - 1$$

$$4pq = 224$$

$$4r = 224$$

$$r = 56$$

8. (D)



As we can see from the graph of the quadratic equation, that the value of the equation is greater than zero for the values of  $x < 3$  and  $x > 4$

9. (C)  $5^{2n} - 2^{3n} = (5^2)^n - (2^3)^n = (25)^n - (8)^n$

We know that  $a^n - b^n$  always have a common factor  $(a - b)$

Therefore one of the factors is  $25 - 8 = 17$

10. (D)  $x = \frac{4\sqrt{6}}{\sqrt{2} + \sqrt{3}}$

on rationalizing

$$x = \frac{4\sqrt{6}}{\sqrt{2} + \sqrt{3}} \times \frac{\sqrt{3} + \sqrt{2}}{\sqrt{3} + \sqrt{2}}$$

$$x = 12\sqrt{2} - 8\sqrt{3}$$

putting the value of  $x$  in the equation

$$\frac{14\sqrt{2} - 8\sqrt{3}}{10\sqrt{2} - 8\sqrt{3}} + \frac{12\sqrt{2} - 6\sqrt{3}}{12\sqrt{2} - 10\sqrt{3}}$$

$$= \frac{7\sqrt{2} - 4\sqrt{3}}{5\sqrt{2} - 4\sqrt{3}} + \frac{6\sqrt{2} - 3\sqrt{3}}{6\sqrt{2} - 5\sqrt{3}}$$

$$\frac{2\sqrt{2}}{5\sqrt{2} - 4\sqrt{3}} + 1 + 1 + \frac{2\sqrt{3}}{6\sqrt{2} - 5\sqrt{3}}$$

$$2 + \frac{2\sqrt{2}(6\sqrt{2} - 5\sqrt{3}) - 2\sqrt{3}(5\sqrt{2} - 4\sqrt{3})}{(5\sqrt{2} - 4\sqrt{3})(6\sqrt{2} - 5\sqrt{3})}$$

$$2 + \frac{24 - 10\sqrt{6} + 10\sqrt{6} - 24}{(5\sqrt{2} - 4\sqrt{3})(6\sqrt{2} - 5\sqrt{3})} = 2 + 0 = 2$$

11. (C) For the equation

$$\sqrt{(a - b)^2} + \sqrt{(b - a)^2}$$

The roots of number is always positive and hence it can be zero only at  $a = b$

So the above equation is positive only when  $a = b$

**Mother's Advance Maths • Algebra [Previous Year Questions]**

12. (C) Let  $a = x$  then  $b = 6x$   
Also let  $c = y$  then  $d = 6y$

$$\frac{a^2 + c^2}{b^2 + d^2} = \frac{x^2 + y^2}{(6x)^2 + (6y)^2} = \frac{1}{36}$$

13. (C) For  $x > 0$  Min of  $\frac{x + (x+2)}{2x} = ?$

$$\frac{x + (x+2)}{2x} = x + \frac{1}{2} + \frac{1}{x}$$

So we have to find the minimum of  $\frac{x+1}{x}$

and add  $\frac{1}{2}$  to it

As AM > GM

So

$$\frac{\left(\frac{x+1}{x}\right)}{2} > \sqrt{\left(\frac{x \times 1}{x}\right)}$$

$$\text{Or } \frac{x+1}{x} > 2$$

$$\text{So min of } x + \frac{x+2}{2x} = \frac{2+1}{2} = \frac{5}{2}$$

14. (A)  $\frac{1+px}{1-px} \sqrt{\frac{1-qx}{1+qx}} = 1$

On squaring and cross multiplying, we get

$$\left(\frac{1+px}{1-px}\right)^2 = \left(\sqrt{\frac{1+qx}{1-qx}}\right)^2$$

$$\frac{1+p^2+x^2+2px}{1+p^2x^2-2px} = \frac{1+qx}{1-qx}$$

On applying componendo and dividend

$$\frac{2(1+p^2x^2)}{-4px} = \frac{2}{-2qx}$$

On solving the above equation, we get

$$x = \pm \frac{1}{p} \sqrt{\frac{2p-q}{q}}$$

15. (B)  $3^{x+2} + 3^x = 10$   
Only powers of 3 that add upto 10 is

$$3^4 + 3^0 = 10$$

$$X + 2 = 0$$

X = -2 solution is consistent

$$\text{Or } x + 2 = 2$$

X= 0 solution is consistent

Thus x = 0, -2 are the solutions

Alternatively, we can put values from the options and check.

$$16. (B) \frac{16}{23} = \frac{1}{23} = \frac{1}{1 + \frac{7}{16}}$$

$$= \frac{1}{1 + \left(\frac{1}{16}\right)} = \frac{1}{1 + \frac{1}{2 + \left(\frac{2}{7}\right)}}$$

$$= \frac{1}{1 + \left(\frac{1}{2 + \left(\frac{1}{2 + \left(\frac{1}{3 + \frac{1}{2}}\right)}\right)}\right)} = \frac{1}{1 + \left(\frac{1}{2 + \left(\frac{1}{3 + \frac{1}{2}}\right)}\right)}$$

On comparing equations we get a= 1 , b = 2 and c = 3

$$\text{Mean} = \frac{a+b+c}{3} = \frac{6}{3} = 2$$

17. (A) We have,  
 $(x-a)(x-b)(x-c)$   
 $\Rightarrow (x^2 - bx - ax + ab)(x - c)$   
 $\Rightarrow x^3 - cx^2 - bx^2 + cbx - ax^2 + acx + abx - abc$   
 $\Rightarrow x^3 - (a+b+c)x^2 + (bc+ca+ab)x - abc$

18. (A) We have

$$\begin{array}{r} x+2) x^4 - x^2 + 7x + 5 (x^3 - 2x^2 + 3x + 1 \\ \quad \quad \quad x^4 + 2x^3 \\ \quad \quad \quad - \quad - \\ \hline \end{array}$$

$$\begin{array}{r} -2x^3 - x^2 \\ -2x^3 - 4x^2 \\ \hline \end{array}$$

$$\begin{array}{r} + \quad + \\ \hline 3x^2 + 7x \end{array}$$

$$\begin{array}{r} 3x^2 + 6x \\ \hline \end{array}$$

$$\begin{array}{r} - \quad - \\ \hline x + 5 \end{array}$$

$$\begin{array}{r} x + 2 \\ \hline \end{array}$$

$$\begin{array}{r} - \quad - \\ \hline 3 \end{array}$$

So, here quotient  $x^3 - 2x^2 + 3x + 1$  is compare with  $ax^3 + bx^2 + cx + d$ . Then  $a = 1$ ,  $b = -2$ ,  $c = 3$ ,  $d = 1$

19. (C) Consider  $px^2 + 3x + 2q = 0$

$$= \text{Sum of roots} = -\frac{3}{p}$$

According to the question

$$\Rightarrow -\frac{3}{p} = -6$$

$$\Rightarrow -6p = -3$$

$$\Rightarrow p = \frac{3}{6} = \frac{1}{2}$$

$$\Rightarrow \text{Product of roots} = \frac{2q}{p}$$

According to the question

$$\Rightarrow \frac{2q}{p} = -6$$

$$\Rightarrow \frac{4q}{1} = -6$$

$$\Rightarrow 4q = -6$$

$$\Rightarrow q = -\frac{6}{4} = -\frac{3}{2}$$

$$p - q = \left(\frac{1}{2}\right) - \left(-\frac{3}{2}\right) = 2$$

20. (B) Consider  $\frac{(x-y)^3 + (y-z)^3 + (z-x)^3}{9(x-y)(y-z)(z-x)}$

We know that when  $A + B + C = 0$  then  $A^3 + B^3 + C^3 = 3ABC$

$$\text{Clearly, } (x-y) + (y-z) + (z-x) = 0$$

$$\text{Hence, } (x-y)^3 + (y-z)^3 + (z-x)^3 = 3(x-y)(y-z)(z-x)$$

$$\Rightarrow \frac{(x-y)^3 + (y-z)^3 + (z-x)^3}{9(x-y)(y-z)(z-x)}$$

$$= \frac{3(x-y)(y-z)(z-x)}{9(x-y)(y-z)(z-x)} = \frac{1}{3}$$

21. (A) We are interested in finding LCM of the polynomials

$$x^3 + 3x^2 + 3x + 1, x^3 + 5x^2 + 5x + 4 \text{ and } x^2 + 5x + 4$$

$$\Rightarrow x^3 + 3x^2 + 3x + 1 = (x+1)^3$$

$$\Rightarrow x^3 + 5x^2 + 5x + 4 = (x+4)(x^2 + x + 1)$$

$$\Rightarrow x^2 + 5x + 4 = (x+4)(x+1)$$

$$\text{Hence, LCM of the polynomials } x^3 + 3x^2 + 3x + 1, x^3 + 5x^2 + 5x + 4 \text{ and } x^2 + 5x + 4 = (x+1)^3(x+4)(x^2+x+1)$$

22. (D) If  $n^2 + 19n + 92$  is a perfect square.

$$\text{Then let } n^2 + 19n + 92 = k^2$$

$$\Rightarrow n^2 + 19n + 92 - k^2 = 0$$

$$\Rightarrow n = \frac{-19 \pm (19)^2 - 4(1)(92 - k^2)}{2(1)}$$

$$= \frac{-19 \pm \sqrt{361 - 368 + 4k^2}}{2(1)} = \frac{-19 \pm \sqrt{-7 + 4k^2}}{2(1)}$$

Now,  $n$  will attain integer value only if  $-7 + 4k^2$  is a perfect square of odd integer.

$$\Rightarrow 4k^2 - 7 = (2x+1)^2$$

$$\Rightarrow 4k^2 - (2x+1)^2 = 7$$

$$\Rightarrow (2k+2x+1)(2k-2x-1) = 7$$

$$\Rightarrow (2k+2x+1)(2k-2x-1) = 7 \times 1$$

Hence

$$(2k-2x-1) = 1 \dots \dots \dots \text{(i)}$$

$$(2k-2x+1) = 7 \dots \dots \dots \text{(ii)}$$

Adding (i) and (ii)

$$\Rightarrow 4k = 8$$

$$\Rightarrow k = 2$$

Put the value of  $k$  in (i)

$$\Rightarrow 4 - 2x - 1 = 1$$

$$\Rightarrow -2x = 1 - 3 = -2$$

$$\Rightarrow x = 1$$

$$\text{Now, } n^2 + 19n + 92 = 4$$

$$\Rightarrow n^2 + 19n + 88 = 0$$

$$\Rightarrow n^2 + 11n + 8n + 88 = 0$$

$$\Rightarrow n(n+11) + 8(n+11) = 0$$

$$\Rightarrow (n+11)(n+8) = 0$$

$$\Rightarrow n = -11 \text{ Or } n = -8$$

Hence, Required Sum =  $-11 - 8 = -19$

23. (C) Consider  $a = \sqrt{7 + 4\sqrt{3}}$

$$\Rightarrow a = \sqrt{7 + 4\sqrt{3}} = \sqrt{4 + 3 + 4\sqrt{3}}$$

$$= \sqrt{(2)^2 + (\sqrt{3})^2 + 2 \times 2 \times \sqrt{3}} = \sqrt{(2 + \sqrt{3})^2}$$

$$= 2 + \sqrt{3}$$

Now

$$a + \frac{1}{a} = 2 + \sqrt{3} + \frac{1}{2 + \sqrt{3}}$$

$$= 2 + \sqrt{3} + \frac{1}{2 + \sqrt{3}} \times \frac{2 - \sqrt{3}}{2 - \sqrt{3}}$$

$$= 2 + \sqrt{3} + 2 - \sqrt{3} = 4$$

24. (D) If  $(b - 6)$  is one root of the quadratic equation  $x^2 - 6x + b = 0$ , where  $b$  is an integer,  
 $\Rightarrow b^2 - 17b + 72 = 0$   
 $\Rightarrow b^2 - 8b - 9b + 72 = 0$   
 $\Rightarrow b(b - 8) - 9(b - 8) = 0$   
 $\Rightarrow b(b - 8)(b - 9) = 0$   
 $\Rightarrow b = 8 \text{ or } b = 9$   
Hence, maximum value of  $b^2 = (9)^2 = 81$

25. (A) The equation  $x^2 + px + q = 0$  has roots equal

Hence, maximum value of  $b^2 = (9)^2 = 81$

25. (A) The equation  $x^2 + px + q = 0$  has roots equal to p and q where  $q \neq 0$ .  
 Consider  $x^2 + px + q = 0$

#### **REFERENCES**

$$\Rightarrow 2p \equiv -q \quad \text{(i)}$$

$$\text{Product of roots} = pq = \frac{q}{1} = q$$

$$\Rightarrow p = 1$$

Put the value of p in (i)

$$\Rightarrow q = -2$$

**26.** (A)  $\frac{36}{11} = 3 + \frac{1}{x + \frac{1}{y + \frac{1}{z}}}$

$$\frac{36}{11} = 3 + \frac{3}{11} = 3 + \frac{1}{\frac{11}{3}} = 3 + \frac{1}{3 + \frac{2}{3}}$$

$$= 3 + \frac{1}{3 + \frac{1}{3 + \frac{3}{2}}} = 3 + \frac{1}{3 + \frac{1}{1 + \frac{1}{2}}}$$

$$\text{Hence, } 3 + \frac{1}{x + \frac{1}{y + \frac{1}{z}}} = 3 + \frac{1}{3 + \frac{1}{1 + \frac{1}{2}}}$$

After comparison, We can say that  
 $x = 3$ ,  $y = 1$  and  $z = 2$   
Hence,  $x + y + z = 3 + 1 + 2 = 6$

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24. If  $x^6 + \frac{1}{x^6} = k \left( x^2 + \frac{1}{x^2} \right)$  then k is equal to.

यदि  $x^6 + \frac{1}{x^6} = k \left( x^2 + \frac{1}{x^2} \right)$  है, तो k किसके बराबर हैं ?

(A)  $\left( x^2 - 1 + \frac{1}{x^2} \right)$  (B)  $\left( x^4 - 1 + \frac{1}{x^4} \right)$

(C)  $\left( x^4 + 1 + \frac{1}{x^4} \right)$  (D)  $\left( x^4 - 1 - \frac{1}{x^4} \right)$

25. If the sum of the squares of three consecutive natural numbers is 110, then the sum of their cubes is.

यदि तीन क्रमागत प्राकृतिक संख्याओं के वर्गों का योगफल 110 है, तो उनके घनों का योगफल क्या होगा ?

- (A) 625 (B) 654  
(C) 684 (D) 725

26. If  $a^x = b^y = c^z$  and  $abc = 1$  then the value

of  $\frac{1}{x} + \frac{1}{y} + \frac{1}{z}$  will be equal to.

यदि  $a^x = b^y = c^z$  और  $abc = 1$  है, तो  $\frac{1}{x} + \frac{1}{y} + \frac{1}{z}$  का मान किसके बराबर होगा ?

- (A) -1 (B) 0  
(C) 1 (D) 3

27. If  $\alpha$  and  $\beta$  are the roots of the equation  $ax^2 + bx$

$+ c = 0$  then the value  $\frac{1}{a\alpha + b} + \frac{1}{a\beta + b}$  of is.

यदि  $\alpha$  और  $\beta$  समीकरण  $ax^2 + bx + c = 0$  के मूल हैं तो

$\frac{1}{a\alpha + b} + \frac{1}{a\beta + b}$  इसका मान क्या है ?

- (A)  $\frac{a}{bc}$  (B)  $\frac{b}{ac}$  (C)  $\frac{c}{ab}$  (D)  $\frac{1}{abc}$

28. If  $a = xy^{p-1}$ ,  $b = yz^{q-1}$ ,  $c = zx^{r-1}$  then  $a^{q-r}b^{r-p}c^{p-q}$  is equal to.

यदि  $a = xy^{p-1}$ ,  $b = yz^{q-1}$ ,  $c = zx^{r-1}$  हैं, तो  $a^{q-r}b^{r-p}c^{p-q}$  किसके बराबर हैं ?

- (A) abc (B) xyz  
(C) 0 (D) None of these

29. The minimum value of the expression  $2x^2 + 5x + 5$  is.

जबकि  $2x^2 + 5x + 5$  का न्यूनतम मान क्या है ?

- (A) 1 (B) 2  
(C)  $\frac{P+Q}{PQ}$  (D)  $\frac{PQ}{P+Q}$

30. The remainder when  $3x^3 - 2x^2y - 13xy^2 + 10y^3$  is divided by  $(x - 2y)$  is equal to.

जब  $3x^3 - 2x^2y - 13xy^2 + 10y^3$  को  $(x - 2y)$  से विभाजित किया जाता है, तो शेषफल किसके बराबर होता है ?

- (A) 0 (B) y  
(C)  $y - 5$  (D)  $y + 3$

31. If  $ab + bc + ca = 0$  then the value of  $(b^2 - ca)(c^2 - ab)(c^2 - ab) - ab + (a^2 - bc)$

$\frac{(c^2 - ab) + (a^2 - bc) \times (b^2 - ca)}{(a^2 - bc)(b^2 - ca)(c^2 - ab)}$  is.

यदि  $ab + bc + ca = 0$  है, तो  $(b^2 - ca)(c^2 - ab) + (a^2 - bc)$

$\frac{(c^2 - ab) + (a^2 - bc) \times (b^2 - ca)}{(a^2 - bc)(b^2 - ca)(c^2 - ab)}$  का मान क्या है ?

- (A) -1 (B) 0  
(C) 1 (D) 2

32. The solution of linear inequalities  $x + y \geq 5$  and  $x - y \leq 3$  lies.

रेखिक असमिकाओं  $x + y \geq 5$  और  $x - y \leq 3$  का हल कहाँ स्थित है ?

- (A) Only in the first quadrant  
केवल प्रथम चतुर्थांश में  
(B) In the first and second quadrants  
प्रथम और द्वितीय चतुर्थांशों में  
(C) In the second and third quadrants  
द्वितीय और चतुर्थ चतुर्थांशों में  
(D) In the third and fourth quadrants  
तृतीय और चतुर्थ चतुर्थांशों में

33. It is given that equations  $x^2 - y^2 = 0$  and  $(x - a)^2 + y^2 = 1$  have single positive solution. For this the value of 'a' is.

यह दिया गया है कि समीकरणों  $x^2 - y^2 = 0$  और  $(x - a)^2 + y^2 = 1$  का एकल धनात्मक हल है। इसके लिए 'a' का मान क्या है ?

- (A)  $\sqrt{2}$  (B) 2  
(C)  $-\sqrt{2}$  (D) 1

34. If  $\alpha, \beta$  and  $\gamma$  are the zeros of the polynomial  $f(x) = ax^2 + bx^2 + cx + d$ , then  $\alpha^2 + \beta^2 + \gamma^2$  is equal to.

यदि  $\alpha, \beta$  और  $\gamma$  बहुपद  $f(x) = ax^2 + bx^2 + cx + d$  के शून्य हैं, तो  $\alpha^2 + \beta^2 + \gamma^2$  किसके बराबर हैं ?

- (A)  $\frac{b^2 - ac}{a^2}$  (B)  $\frac{b^2 - 2ac}{a}$   
(C)  $\frac{b^2 + 2ac}{b^2}$  (D)  $\frac{b^2 - 2ac}{a^2}$

## Solution

1. (C) Given,  $a+b=2c$

$$\text{Or } a+b=c+c$$

$$\text{Or } a-c=c-b \dots\dots\dots \text{(i)}$$

$$\text{Now, } \frac{a}{a-c} + \frac{c}{b-c}$$

$$= \frac{a}{c-b} - \frac{c}{c-b} \text{ (from Eq. (i))}$$

$$= \frac{a-c}{c-b}$$

$$= \frac{c-b}{c-b} \text{ (from Eq. (i))}$$

$$= 1$$

2. (B)  $x = y^{1/a} \dots \text{(i)}$ ,  $y = z^{1/b} \dots \text{(ii)}$  and  $z = x^{1/c} \dots \text{(iii)}$

$$\text{Now } x = y^{1/a} \text{ (from Eq. (i))}$$

$$\Rightarrow x = (x^{1/c})^{1/b} \text{ (from Eq. (ii))}$$

$$\Rightarrow x = ((x^{1/c})^{1/b})^{1/a} \text{ (from Eq. (iii))}$$

$$\Rightarrow x = x^{abc}$$

$$\text{Or } abc = 1$$

3. (C)  $2b = a+c$  (given)  $\dots\dots\dots \text{(i)}$

$$\text{Now } x^{b-c} \times (xz)^{1/2} \times z^{c-a} \times z^{a-b} [\because y^2 = xz]$$

$$\Rightarrow x^{b-c} \times (x)^{\left(\frac{c-a}{2}\right)} \times z^{\left(\frac{c-a}{2}\right)} \times z^{a-b}$$

$$\Rightarrow x^{\left(\frac{2b-2c+c-a}{2}\right)} \times z^{\left(\frac{c+a+2a-2b}{2}\right)}$$

$$\Rightarrow x^{\frac{2b-a-c}{2}} \times z^{\frac{(2b+a+c)}{2}}$$

$$= x^0 \times y^0 \quad (\because a+b=2b)$$

$$= 1 \times 1 = 1$$

4. (B) Let the roots of the equation be ' $\alpha$ ' and ' $\beta$ '.  
According to the question.

$$\alpha = \frac{1}{\beta} \dots\dots\dots \text{(i)}$$

From the equation

$$px^2 + x + r = 0$$

$$\alpha \times \beta = \frac{r}{p} \quad (\because \text{product of roots} = c/a)$$

$$\text{or } \beta \times \frac{1}{\beta} = \frac{r}{p} \quad (\text{From Eq.(i)})$$

$$\text{or } r = p$$

5. (A)  $65x - 33y = 97 \dots\dots\dots \text{(i)}$

$$33x - 65y = 1 \dots\dots\dots \text{(ii)}$$

Adding Eqs (i) and (ii) we get

$$x - y = 1 \dots\dots\dots \text{(iii)}$$

Subtracting Eqs (i) and (ii) we get

$$x + y = 3 \dots\dots\dots \text{(iv)}$$

Solving Eqs (iii) and (iv) we get

$$x = 2, y = 1$$

$$\therefore xy = 2 \times 1 = 2$$

6. (A) Let  $\frac{z}{c} = p$

$$\therefore \frac{b}{y} + p = 1 \text{ and } \frac{1}{p} + \frac{x}{a} = 1$$

$$\Rightarrow \frac{b}{y} = 1-p \text{ and } \frac{x}{a} = 1 - \frac{1}{p} = \frac{p-1}{p}$$

$$\Rightarrow \frac{y}{b} = \frac{1}{1-p} \text{ and } \frac{a}{x} = \frac{p}{p-1}$$

Now adding Eqs (i) and (ii) we get

$$\frac{y}{b} + \frac{a}{x} = \frac{1}{1-p} + \frac{p}{p-1}$$

$$\Rightarrow \frac{xy+ab}{bx} = \frac{1}{1-p} - \frac{p}{1-p}$$

$$\Rightarrow \frac{ab+xy}{bx} = \frac{1-p}{1-p} = 1$$

7. (C)  $\frac{a^2-1}{a}=5$

$$\therefore a - \frac{1}{a} = 5$$

Cubing sides we get

$$\left(a - \frac{1}{a}\right)^3 = 5^3$$

$$\Rightarrow a^3 - \frac{1}{a^3} - 3 \left(a - \frac{1}{a}\right) = 125$$

$$[\because (a-b)^3 = a^3 - b^3 - 3ab(a-b)]$$

$$\Rightarrow a^3 - \frac{1}{a^3} = 125 + 3(5) \text{ (frp, Eq (i))}$$

$$\Rightarrow a^3 - \frac{1}{a^3} = 125 + 15 = 140$$

8. (D) Given  $x + y + z = 0$

We have to find the value of

$$(y + z - x)^3 + (z + x - y)^3 + (x + y - z)^3$$

Let  $y + z - x = a$ ,  $z + x - y = b$

and  $x + y - z = c$

$$\therefore a + b + c = y + z - x + z + x - y + x + y - z = 0$$

If  $a + b + c = 0$

then  $a^3 + b^3 + c^3 = 3abc$

$$\therefore (y + z - x)^3 + (z + x - y)^3 + (x + y - z)^3$$

$$= 3(y + z - x)(z + x - y)(x + y - z)$$

$$= 3(-2x)(-2y)(-2z) (\because x + y + z = 0)$$

$$= -24xyz$$

9. (A) As  $(x + 3)$  is a factor of given equation

$$\therefore x = -3$$

$$\text{Now } p(x) = x^3 + 3x^2 + 4x + k$$

$$\therefore p(-3) = 0$$

$$\Rightarrow (-3)^3 + 3(-3)^2 + 4(-3) + k = 0$$

$$\Rightarrow -27 + 27 - 12 + k = 0$$

$$\Rightarrow k = 12$$

10. (B) Given  $p(x) = 3x^3 + 4x^2 - 7$

Putting  $x = 1$

$$\Rightarrow p(1) = 3(1)^3 + 4(1)^2 - 7$$

$$\Rightarrow p(1) = 3 + 4 - 7 = 0$$

Hence  $x = 1$  a zero for polynomial

$$3x^3 + 4x^2 - 7$$

11. (C)  $\alpha$  and  $\beta$  are the roots of the equation  $ax^2 + bx + c = 0$

$$\therefore \text{Sum of roots} = \alpha + \beta = \frac{-b}{a}$$

$$\text{And product of roots} = \alpha\beta = \frac{c}{a}$$

$$\begin{aligned}\therefore (\alpha + 1)(\beta + 1) &= \alpha\beta + \alpha + \beta + 1 \\ &= (\alpha\beta) + (\alpha + \beta) + 1 \\ &= \frac{-b}{a} + \frac{c}{a} + 1\end{aligned}$$

$$= \frac{-b + c + a}{a} = \frac{a - b + c}{a}$$

12. (D)  $p(x) = 3x^3 + kx^2 + 5x - 6$

$$x + 1 = 0$$

$$\therefore x = -1$$

$$p(-1) = 3(-1)^3 + k(-1)^2 + 5(-1) - 6$$

$$= -3 + k - 5 - 6$$

$$= k - 14$$

$$\therefore \text{Remainder} = k - 14$$

But remainder = -7 (given)

$$\therefore k - 14 = -7$$

$$\therefore k = -7 + 14 = 7$$

13. (C) We have

degree of  $f(x) = p$

degree of  $g(x) = q$

degree  $(f(x) + g(x)) = \max$

$(p,q), p \neq q$

degree  $(f(x) - g(x)) = p$  or  $q, p = q$

degree  $(f(x) - g(x)) = \text{less than or equal to}$   
 $\max(p,q) p = q$

$\therefore \text{degree } (f(x) \pm g(x)) = \text{less than or equal to}$   
 $\max(p,q)$

$$14. (A) \frac{\sqrt{5} - \sqrt{3}}{\sqrt{5} + \sqrt{3}} + \frac{\sqrt{5} + \sqrt{3}}{\sqrt{5} - \sqrt{3}}$$

$$= \frac{(\sqrt{5} - \sqrt{3})^2 - (\sqrt{5} + \sqrt{3})^2}{(\sqrt{5})^2 - (\sqrt{3})^2}$$

$(\because (a+b)(a-b) = a^2 - b^2)$

$$= \frac{(5+3-2\sqrt{15}) - (5+3+2\sqrt{15})}{2}$$

$(\because (a+b)^2 = a^2 + 2ab + b^2$   
 $\text{and } (a-b)^2 = a^2 - 2ab + b^2)$

$$= \frac{8-2\sqrt{15}-8-2\sqrt{15}}{2} = \frac{-4\sqrt{15}}{2} = -2\sqrt{15}$$

15. (C)

$$\begin{aligned}& \frac{1}{1+x^{1-a}+x^{c-a}} + \frac{1}{1+x^{a-b}+x^{c-b}} + \frac{1}{1+x^{a-c}+x^{b-c}} \\&= \frac{1}{1+\frac{x^b}{x^a}+\frac{x^c}{x^a}} + \frac{1}{1+\frac{x^a}{x^b}+\frac{x^c}{x^b}} + \frac{1}{1+\frac{x^a}{x^c}+\frac{x^b}{x^c}} \\&= \frac{x^a}{x^a+x^b+x^c} + \frac{x^b}{x^a+x^b+x^c} + \frac{x^c}{x^a+x^b+x^c} \\&= \frac{x^a+x^b+x^c}{x^a+x^b+x^c} = 1\end{aligned}$$

16. (A)  $p(x) = ax^2 + bx + c$

for  $x = 0$

$$p(0) = a(0)^2 + b(0) + c \Rightarrow c = 3$$

for  $x - 1 = 0$  i.e.  $x = 1$

$$p(1) = 6$$

$$\therefore a(1)^2 + b(1) + c = 6$$

$$a + b + 3 = 6$$

$$\Rightarrow a + b = 3$$

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- 17.** (C) Let the two numbers be  $x$  and  $y$

$\therefore$  Arithmetic mean = 10  
and geometric mean = 0

$$\therefore \frac{x+y}{2} = 10 \text{ and } \sqrt{xy} = 8$$

$$\therefore x+y = 20 \quad \dots \dots \dots \text{(i)}$$

and  $xy = 64 \quad \dots \dots \dots \text{(ii)}$

From Eq (ii)  $xy = 64$

$$\therefore x(20-x) = 64 \text{ (from Eq. (i))}$$

$$20x - x^2 = 64$$

$$\Rightarrow x^2 - 20x + 64 = 0$$

$$\Rightarrow x^2 - 16x - 4x + 64 = 0$$

$$\Rightarrow x(x-16) - 4(x-16) = 0$$

$$\Rightarrow (x-4)(x-16) = 0$$

$$\therefore x = 4$$

$$\text{Or } x = 16$$

$$\text{And } y = 16 \text{ or } y = 4$$

- 18.** (B) Let the side of square be  $x$  cm

$$\therefore \text{New side of square} = x + 8 \text{ cm}$$

According to the question

$$(x+8)^2 - x^2 = 120$$

( $\because$  Area of square = side<sup>2</sup>)

$$\Rightarrow x^2 + 64 + 2(8)x - x^2 = 120$$

( $\because (a+b)^2 = a^2 + 2ab + b^2$ )

$$\Rightarrow 16x = 120 - 64$$

$$x = \frac{56}{16} = 3.5 \text{ cm}$$

Hence side of square = 3.5 cm.

- 19.** (A) Given  $x = y^a$

$$\text{Or } x = (Z^b)^a \text{ (as } y = z^b)$$

$$\text{Or } x = ((x^b)^a)^a \text{ (as } y = z^b)$$

$$\text{Or } x = x^{abc}$$

$$\text{Or, } abc = 1$$

- 20.** (A) Given  $x = 2 + 2^{2/3} + 2^{1/3}$

$$\Rightarrow x - 2 = 2^{2/3} + 2^{1/3}$$

Cubing both sides we get

$$(x-2)^3 = (2^{2/3} + 2^{1/3})^3$$

$$\Rightarrow x^3 - 2^3 - 3(x)(2)(x-2)$$

$$= (2^{2/3})^3 + (2^{1/3})^3 + 3(2)^{2/3}(2)^{1/3}(2^{2/3} + 2^{1/3})$$

$$(\because (a-b)^3 = a^3 - b^3 - 3ab(a-b)(a+b)^3 = a^3 + b^3 + 3ab(a+b))$$

$$\Rightarrow x^3 - 8 - 6x^2 + 12x = 2^2 + 2 + 6(x-2)$$

$$\Rightarrow x^3 - 6x^2 + 12x = 6 + 8 + 6x - 12$$

$$\Rightarrow x^3 - 6x^2 - 6x = 2$$

- 21.** (C) Given  $x^2 - 6x - 27 > 0$

$$\text{Or } x^2 - 9x + 3x - 27 > 0$$

$$(x+3)(x-9) > 0$$

Now for  $(x+3)(x-9)$  to be greater than 0.  
Either  $(x+3)$  and  $(x-9)$  must be greater than 0.

Or both  $(x+3)$  and  $(x-9)$  must be less than 0.

$$\therefore x > 9 \text{ and } x < -3$$

- 22.** (C) Given HCF of polynomials =  $x + 3$

LCM of polynomials

$$= x^3 - 9x^2 - x + 105$$

$$\text{One polynomial} = x^2 - 9x^2 - x + 105$$

We know that  $(\text{HCF} \times \text{LCM})$  of two number = Product of two number

$\therefore$  Other polynomial

$$= \frac{(x+3)(x^3 - 9x^2 - x + 105)}{x^2 - 4x - 21}$$

$$= \frac{(x+3)(x^3 - 9x^2 - x + 105)}{(x-7)(x+3)}$$

$$= \frac{x^3 - 9x^2 - x + 105}{x-7}$$

$$\Rightarrow \text{Other polynometral} = x^2 - 2x = 15$$

- 23.** (C) Given  $\alpha + \beta = -\frac{q}{p}$   $\alpha\beta = \frac{r}{p}$

and  $1 < p < q < r$

$$\text{From option (a)} \quad \frac{1}{\alpha + \beta} = \frac{1}{-\frac{q}{p}} = \frac{-p}{q}$$

Option (B)

$$\frac{1}{\alpha} + \frac{1}{\beta} = \frac{\alpha + \beta}{\alpha\beta} = \frac{-p}{q}$$

Option (C)

$$\frac{-1}{\alpha\beta} = \frac{-p}{r}$$

Option (D)

$$\frac{\alpha\beta}{\alpha + \beta} = \frac{r}{p} \times \left( \frac{-p}{q} \right) = \frac{-r}{q}$$

Now except (d) in all other options the numerator is smaller than denominator

$\therefore$  Option (b) is smallest

Now from option (A) and (C) i.e.  $\frac{-p}{q}$

and  $\frac{-p}{q}, \frac{-p}{q}$  greater as  $r > q$

Now from option (C) and (B) i.e.  $\frac{-p}{r}$  and  $\frac{-q}{r}$

$\frac{-p}{r}$  is greater as  $q > p$

$\therefore -\frac{1}{\alpha\beta}$  is greatest

24. (B) We know that

$$a^3 + b^3 = (a+b)(a^2 - ab + b^2)$$

$$\therefore x^6 + \frac{1}{x^6} = (x^2)^3 + \left(\frac{1}{x^2}\right)^3$$

$$= \left(x^2 + \frac{1}{x^2}\right) \left(x^4 - 1 + \frac{1}{x^4}\right)$$

$$\therefore k = x^4 - 1 + \frac{1}{x^4}$$

25. (C) Let the three consecutive natural numbers be

$$(x-1), x, (x+1)$$

According to the question

$$\Rightarrow (x-1)^2 + x^2 + (x+1)^2 = 110$$

$$\because (a-b)^2 = a^2 + b^2 - 2ab$$

$$(a+b)^2 = a^2 + b^2 + 2ab$$

$$\Rightarrow x^2 + 1 - 2x + x^2 + x^2 + 1 + 2x = 110$$

$$\Rightarrow 3x^2 = 110 - 2$$

$$\Rightarrow x^2 = \frac{108}{3} = 36$$

$\therefore$  The numbers are  $(6-1), 6, (6+1)$

i.e. 5, 6 and 7

Now sum of their cubes

$$= 5^3 + 6^3 + 7^3$$

$$= 125 + 216 + 343 = 684$$

26. (B) Given  $a^x = b^y = c^z = k$  (let)

and  $abc = 1$

Now,  $a^x = k$

Or  $x = k^{1/x}$

Similarly  $b = k^{1/y}$  and  $c = k^{1/z}$

Now  $abc = 1$  or  $k^{1/x} \cdot k^{1/y} \cdot k^{1/z} = 1$

$$\text{Or } k^{\left(\frac{1}{x} + \frac{1}{y} + \frac{1}{z}\right)} = 1$$

$$\text{Or } k^{\left(\frac{1}{x} + \frac{1}{y} + \frac{1}{z}\right)} = k^0$$

$$\text{Or } \frac{1}{x} + \frac{1}{y} + \frac{1}{z} = 0$$

27. (B) We have  $\alpha, \beta$  are the roots of the equation

$$ax^2 + bx + c = 0$$

$$\therefore \alpha + \beta = \frac{-b}{a}, \alpha\beta = \frac{c}{a}$$

$$\text{Now } \frac{1}{a\alpha + b} + \frac{1}{a\beta + b}$$

$$= \frac{a\alpha + b + a\beta + b}{(a\alpha + b)(a\beta + b)}$$

$$= \frac{a(\alpha + \beta) + 2b}{a^2(\alpha\beta) + ab(\alpha + \beta) + b^2}$$

$$= \frac{a\left(\frac{-b}{a}\right) + 2b}{a^2\left(\frac{c}{a}\right) + ab\left(\frac{-b}{a}\right) + b^2} = \frac{b}{ac}$$

28. (D) We have

$$a = xy^{p-1}, b = yz^{q-1}, c = zx^{r-1}$$

$$\text{Now } a^{q-r}, b^{r-p}, c^{p-q}$$

$$= (xy^{p-1})^{q-r}(yz^{q-1})^{r-p}(zx^{r-1})^{p-q}$$

$$= x^{q-r}y^{(p-1)(q-r)}y^{r-p}z^{(q-1)(r-p)}z^{p-q}x^{(r-1)(p-q)}$$

$$= x^{(q-r)+(p-1)(q-r)}y^{(p-1)(q-r)+r-p}z^{(q-1)(r-p)+p-q}$$

$$= x^{q+r+p+r-p}y^{pq pr qr pr qr}z^{qr pq qr+pr+pq}$$

$$= x^{2q+p+r(p-q-1)}y^{2r+q+p(q-r-1)}z^{2p+r+q(r-p-1)}$$

29. (B) Let

$$y = 2x^2 + 5x + 5$$

$$\Rightarrow y = 2\left(x^2 + \frac{5}{2}x + \frac{5}{2}\right)$$

$$\Rightarrow y = 2\left(x^2 + \frac{5}{2}x + \frac{25}{16}\right) + 5 - \frac{25}{8}$$

$$\Rightarrow y = 2\left(x + \frac{5}{4}\right)^2 + \frac{15}{8}$$

$\therefore$  Minimum value of  $y = \frac{15}{8}$

30. (A)  $3x^3 - 2x^2y - 13xy^2 + 10y^3$

And  $g(x) = x - 2y$

When  $f(x)$  is divided by  $g(x)$

$$\therefore f(2y) = 3(2y)^3 - 2(2y)^2y - 132(2y)^2 + 10y^3$$

$$f(2y) = 24y^3 - 8y^3 - 26y^3 + 10y^3$$

$$f(2y) = 0$$

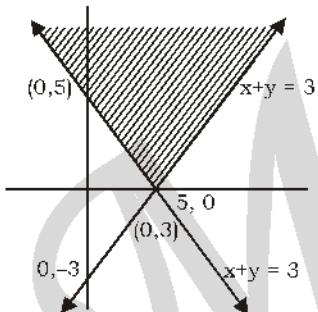
Hence remainder = 0

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31. (B) We have  $ab + bc + ca = 0$   
Now

$$\begin{aligned} & \frac{(b^2 - ca)(c^2 - ab) + (a^2 - bc)(c^2 - ab)}{(a^2 - bc)(b^2 - ca)(c^2 - ab)} \\ &= \frac{1}{a^2 - bc} + \frac{1}{b^2 - ca} + \frac{1}{c^2 - ab} \\ &= \frac{1}{a^2 + B + c} + \frac{1}{b^2 + ab + bc} + \frac{1}{c^2 + ab + ca} \\ &= \frac{1}{a(a + B + c)} + \frac{1}{b(b + a + c)} + \frac{1}{c(c + a + b)} \\ &= \frac{1}{(a + B + c)} \left[ \frac{1}{a} + \frac{1}{b} + \frac{1}{c} \right] \\ &= \frac{1}{(a + B + c)} \left( \frac{ab + bc + ca}{abc} \right) = 0 \end{aligned}$$

32. (B) We have  
 $x + y \geq 5$  and  $x - y \leq 3$   
The graph of liner equalities are below



Clearly, from graph solution lies in first and second quadrant

33. (A) We have  $x^2 - y^2$  and  $(x - a)^2 + y^2 = 1$   
 $\Rightarrow x^2 - y^2 = 0$   
 $\Rightarrow x^2 = y^2$

Put the value  $y^2$  in we get

$$\begin{aligned} & (x - a)^2 + x^2 = 1 \\ & \Rightarrow 2x^2 - 2ax + a^2 - 1 = 0 \end{aligned}$$

Equation have single positive solution

$$\therefore D = 0$$

$$\Rightarrow 4a^2 - 4(a^2 - 1)(2) = 0$$

$$\Rightarrow 4a^2 - 8a^2 + 8 = 0$$

$$\Rightarrow a = \sqrt{2}$$

34. (D) We have

$$f(x) = ax^3 + bx^2 + cx + d$$

$$\alpha, \beta, \gamma = -\frac{b}{a}$$

$$\alpha\beta\gamma = -\frac{d}{a}$$

$$(\alpha + \beta + \gamma)^2 = \alpha^2 + \beta^2 + \gamma^2 + 2(\alpha\beta + \beta\gamma + \gamma\alpha)$$

$$\Rightarrow \left(-\frac{b}{a}\right)^2 = \alpha^2 + \beta^2 + \gamma^2 + \frac{2c}{a}$$

$$\Rightarrow \alpha^2 + \beta^2 + \gamma^2 + \frac{b^2}{a^2} - \frac{2c}{a} = \frac{b^2 - 2ac}{a^2}$$



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**CDS [2017-II]**

23. What is the value of  $\alpha$  ( $\alpha \neq 0$ ) for which  $x^2 - 5x + \alpha$  and  $x^2 - 7x + 2\alpha$  have a common factor ?  
 $\alpha$  ( $\alpha \neq 0$ ) का वह मान क्या है, जिसके लिए  $x^2 - 5x + \alpha$  और  $x^2 - 7x + 2\alpha$  का एक सार्व गुणनखण्ड होता है ?  
 (A) 6 (B) 4  
 (C) 3 (D) 2
24. What are the factors of  $x^3 + 4x^2 - 11x - 30$ ?  
 $x^3 + 4x^2 - 11x - 30$  के गुणनखण्ड क्या हैं ?  
 (A)  $(x - 2), (x + 3)$  and  $(x + 5)$   
 (B)  $(x + 2), (x + 3)$  and  $(x - 5)$   
 (C)  $(x - 2), (x + 3)$  and  $(x + 5)$   
 (D)  $(x + 2), (x - 3)$  and  $(x - 5)$
25. What is the positive value of  $m$  for which the roots of the equation  $12x^2 + mx + 5 = 0$  are in the ratio  $3 : 2$ ?  
 $m$  का वह धनात्मक मान क्या है, जिसके लिए समीकरण  $12x^2 + mx + 5 = 0$  के मूल  $3 : 2$  के अनुपात में हैं ?  
 (A)  $5\sqrt{10}$  (B)  $\frac{5\sqrt{10}}{12}$  (C)  $\frac{5}{12}$  (D)  $\frac{12}{6}$
26. Let  $f(x)$  and  $g(x)$  be two polynomials (with real coefficients) have degrees 3 and 4 respectively. What is the degree of  $f(x)g(x)$ ?  
 माना  $f(x)$  और  $g(x)$  दो बहुपद (वास्तविक गुणांकों के साथ) हैं, जिनकी घात क्रमशः 3 और 4 हैं।  $f(x)g(x)$  की घात क्या है ?  
 (A) 12 (B) 7  
 (C) 7 (D) 3
27. If  $5x^3 + 5x^2 - 6x + 9$  is divided by  $(x + 3)$  then the remainder is.  
 यदि  $5x^3 + 5x^2 - 6x + 9$  को  $(x + 3)$  से विभाजित किया जाता है, तो शेषफल क्या है ?  
 (A) 135 (B) -135  
 (C) 63 (D) -63
28. The product of two non-zero expression is  $(x + y + z)p^3$ . If their HCF is  $p^2$ . If their LCM is.  
 दो शून्येतर व्यंजकों का गुणनफल  $(x + y + z)p^3$  है। यदि उनका महत्तम समापवर्तक  $p^2$  है तो उनका लघुत्तम समापवर्त्य क्या है ?  
 (A)  $(x + y + z)$  (B)  $(x + y + z)p^2$   
 (C)  $(x + y + z)p^5$  (D)  $(x + y + z)p$
29. The quotient of  $8x^3 - y^3$  when divided by  $2xy + 4x^2 + y^2$  is.  
 $8x^3 - y^3$  को  $2xy + 4x^2 + y^2$  से विभाजित करने पर भागफल क्या होगा ?  
 (A)  $2x + y$  (B)  $x + 2y$   
 (C)  $2x - y$  (D)  $4x - y$

30. If  $(x + 2)$  is a common factor of  $x^2 + ax + b$  and  $x^2 + bx + a$  then the ratio  $a : b$  is equal to.  
 यदि  $(x + 2)$ ,  $x^2 + ax + b$  और  $x^2 + bx + a$  का एक सार्वगुणनखण्ड है जो अनुपात  $a : b$  किसके बराबर है ?  
 (A) 1 (B) 2  
 (C) 3 (D) 4
31. Let  $f(x) = a_0x^n + a_1x^{n-1} + a_2x^{n-2} + \dots + a_{n-1}x + a_n$  where  $a_0, a_1, a_2, \dots, a_n$  are real numbers. If  $f(x)$  is divided by  $(ax - b)$  by are real numbers.  
 मान लीजिए  $f(x) = a_0x^n + a_1x^{n-1} + a_2x^{n-2} + \dots + a_{n-1}x + a_n$ , जहाँ  $a_0, a_1, a_2, \dots, a_n$  वास्तविक संख्याएँ हैं। यदि  $f(x)$  को  $(ax - b)$  से विभाजित किया जाए तो शेषफल क्या होगा ?  
 (A)  $f\left(\frac{b}{a}\right)$  (B)  $r\left(-\frac{b}{a}\right)$   
 (C)  $r\left(\frac{a}{b}\right)$  (D)  $r\left(-\frac{a}{b}\right)$
32. The product of the polynomials  $(x + 2)$ ,  $(x - 2)$ ,  $(x^2 - 2x^2 + 4x - 8)$  and  $(x^3 + 2x^2 + 4x + 8)$  is.  
 बहुपदों  $(x + 2)$ ,  $(x - 2)$ ,  $(x^2 - 2x^2 + 4x - 8)$  और  $(x^3 + 2x^2 + 4x + 8)$  का गुणनफल क्या है ?  
 (A)  $x^8 - 256$  (B)  $(x^4 - 16)^2$   
 (C)  $(x^4 + 16)^2$  (D)  $(x^2 - 4)^4$
33. The factors of  $x(x + 2)(x + 3)(x + 5) - 72$  are.  
 $x(x + 2)(x + 3)(x + 5) - 72$  के गुणनखण्ड हैं  
 (A)  $x, (x + 3), (x + 4)$  and  $(x - 6)$   
 (B)  $(x - 1), (x + 6)$  and  $(x^2 - 2x - 12)$   
 (C)  $(x - 1), (x + 6)$  and  $(x^2 + 5x + 12)$   
 (D)  $(x + 1), (x - 6)$  and  $(x^2 - 5x - 12)$
34. If the HCF of polynomials  $f(x) = (x - 1)(x^2 + 3x + a)$  and  $g(x) = (x + 2)(x^2 + 2x + b)$  is  $(x^2 + x - 2)$  then what are the values of  $a$  and  $b$  respectively ?  
 यदि बहुपद  $f(x) = (x - 1)(x^2 + 3x + a)$  और  $g(x) = (x + 2)(x^2 + 2x + b)$  का महत्तम समापवर्तक  $(x^2 + x - 2)$  है, तो  $a$  और  $b$  के मान क्रमशः क्या हैं ?  
 (A) 2, 2 (B) 2, -3  
 (C) -1, -3 (D) -2, -1
35. If the roots of the equation  $a(b - c)x^2 + b(c - a)x + c(a - b) = 0$  are equal then which one of the following is correct ?  
 यदि समीकरण  $a(b - c)x^2 + b(c - a)x + c(a - b) = 0$  के मूल बराबर हैं, तो निम्नलिखित में से कौन-सा सही है ?  
 (A)  $2b = a + c$  (B)  $b^2 = ac$   
 (C)  $\frac{2}{b} = \frac{1}{a} + \frac{1}{c}$  (D)  $\frac{1}{b} = \frac{1}{a} + \frac{1}{c}$

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36. The non-zero of the equation  $\frac{a-x^2}{bx} - \frac{b-x}{c} = \frac{c-x}{b} - \frac{b-x^2}{cx}$  where  $b \neq 0, c \neq 0$  is.

समीकरण  $\frac{a-x^2}{bx} - \frac{b-x}{c} = \frac{c-x}{b} - \frac{b-x^2}{cx}$  जहाँ  $b \neq 0, c \neq 0$ , शून्येतर हल क्या हैं ?

- (A)  $\frac{b^2+ac}{b^2+c^2}$       (B)  $\frac{b^2-ac}{b^2-c^2}$   
 (C)  $\frac{b^2-ac}{b^2+c^2}$       (D)  $\frac{b^2+ac}{b^2-c^2}$

37. If  $k$  is an integer then  $x^2 + 7x - 14\left(k^2 - \frac{7}{8}\right) = 0$  has.

यदि  $k$  एक पूर्णांक हैं, तो  $x^2 + 7x - 14\left(k^2 - \frac{7}{8}\right) = 0$  का/के  
 (A) Both integral roots / दोनों मूल पूर्णांक हैं  
 (B) At least one integral root  
 कम-से-कम एक मूल पूर्णांक हैं  
 (C) No integral root / कोई भी मूल पूर्णांक नहीं हैं  
 (D) Both positive integral roots  
 दोनों मूल धन पूर्णांक हैं

38. What is the value of  $u$  in the system of equations  $3(2u+v) = 7uv$ ,  $3(u+3v) = 11uv$  ?

समीकरण निकाय  $3(2u+v) = 7uv$ ,  $3(u+3v) = 11uv$  में  $u$  का मान क्या हैं ?

- (A) 1      (B)  $\frac{1}{4}$       (C)  $\frac{1}{2}$       (D) 2

39. Five years ago, Ram was three times as old as Shyam. Four years from now, Ram will be only twice as old as Shyam. What is the present age of Ram ?

पाँच वर्ष पहले, राम की आयु, श्याम की आयु की तीन गुनी थी। अब से चार वर्ष बाद, राम की आयु, श्याम की आयु की केवल दोगुनी होगी। राम की वर्तमान आयु क्या है ?

- (A) 30 years  
 (B) 32 years  
 (C) 36 years  
 (D) 40 years

40. If  $ab + bc + ca = 0$  then what is the value

$$\text{of } \frac{a^2}{a^2-bc} + \frac{b^2}{b^2-ca} + \frac{c^2}{c^2-ab} ?$$

यदि  $ab + bc + ca = 0$  है तो  $\frac{a^2}{a^2-bc} + \frac{b^2}{b^2-ca} + \frac{c^2}{c^2-ab}$  का मान क्या है ?

- (A) 3      (B) 0  
 (C) 1      (D) -1

41. What  $\frac{(x-y)(y-z)(z-x)}{(x-y)^3 + (y-z)^3 + (z-x)^3}$  equal to ?

$$\frac{(x-y)(y-z)(z-x)}{(x-y)^3 + (y-z)^3 + (z-x)^3} \text{ किसके बराबर हैं ?}$$

- (A)  $-\frac{1}{3}$       (B)  $\frac{1}{3}$       (C) 3      (D) -3

**Solution**

1. (B)  $\sqrt{\frac{0.064 \times 6.25}{0.081 \times 4.84}}$

$$= \sqrt{\frac{64 \times 10^{-3} \times 625 \times 10^{-2}}{81 \times 10^{-3} \times 484 \times 10^{-2}}} \\ = \sqrt{\frac{64 \times 625}{81 \times 484}} = \frac{8 \times 25}{9 \times 22} = \frac{100}{99}$$

2. (C) We have  $(x+4)$  as a factor  
 ∴ Put  $x = -4$  in all the options

$$(a) (-4)^2 - 7(-4) + 44 \\ = 16 + 28 + 44 = 88 \neq 0$$

$$(b) (-4)^2 + 7(-4) - 44 \\ = 16 - 28 - 44 = -56 \neq 0$$

$$(c) (-4)^2 - 7(-4) - 44 \\ = 16 + 28 - 44 = 0$$

$$(d) (-4)^2 + 7(-4) + 44 \\ = 16 - 28 + 44 = 32 \neq 0$$

∴  $(x+4)$  is a factor of  $x^2 - 7x - 44$

3. (d) We have  $2x^2 + 6x + k = 0$   
 ∴  $\alpha + \beta = -\frac{6}{2} = -3$  and  $\alpha\beta = \frac{k}{2}$

$$\text{Now } \frac{\alpha}{\beta} + \frac{\beta}{\alpha} = \frac{\alpha^2 + \beta^2}{\alpha\beta}$$



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$$\text{Again } \frac{y}{x} = \frac{t^{\frac{t}{t-1}}}{\frac{t}{t-1}} = t^{\frac{t}{t-1} - 1} = t^{\frac{1}{t-1}} = t$$

$$\Rightarrow \frac{y}{x} = t \quad \dots \dots \dots \text{(ii)}$$

From Eqs (i) and (ii) we get  $y = x^{y/x}$   
 $\Rightarrow y^x = x^y$

9. (D) We have  $A : B = 3 : 4$

$$\Rightarrow \frac{A}{B} = \frac{3}{4} \Rightarrow A = \frac{3}{4}B$$

Now

$$\frac{3A^2 + 4B}{3A - 4B^2} = \frac{3\left(\frac{3}{4}B\right)^2 + 4B}{3\left(\frac{3}{4}B\right) + 4B^2}$$

$$= \frac{\frac{27}{16}B^2 + 4B}{\frac{9}{4}B - 4B^2} = \frac{\left[\frac{27B^2 + 64B}{16}\right]}{\left[\frac{9B - 16B^2}{4}\right]}$$

$$= \frac{27B^2 + 64B}{4(9B - 16B^2)} = \frac{27B + 64}{4(9 - 16B)}$$

But we don't have the value of B

$\therefore$  The value of given expression cannot be determined

10. (B) We have

$$x = 2 + 2^{2/3} + 2^{1/3} \quad \dots \dots \dots \text{(i)}$$

$$\Rightarrow x - 2 = 2^{1/3}(2^{1/3} + 1)$$

On cubing both the sides we get

$$(x - 2)^3 = 2(2^{1/3} + 1)^3$$

$$\Rightarrow x^3 - 3(x^2)(2) + 3(x)(2)^2 - 8$$

$$= 2[(2^{1/3})^3 + 3(2^{1/3})^2(1) + 3(2^{1/3})(1) + (1)^3]$$

$$\Rightarrow x^3 - 6x^2 + 12x - 8 = 2$$

$$[2 + 32^{2/3} + 32^{1/3} + 1]$$

$$\Rightarrow x^3 - 6x^2 + 12x - 8 = 2$$

$$[3 + 32^{2/3} + 32^{1/3}]$$

$$\Rightarrow x^3 - 6x^2 + 12x - 8 = 6[1 + 2^{2/3} + 2^{1/3}]$$

$$\Rightarrow x^3 - 6x^2 + 12x - 8 = 6[1 + x - 2]$$

[From Eqs (i)]

$$\Rightarrow x^3 - 6x^2 + 12x - 8 = 6(x - 1)$$

$$\Rightarrow x^3 - 6x^2 + 12x - 8 = 6x - 6$$

$$\Rightarrow x^3 - 6x^2 + 6x + 6x = 2$$

11. (C) We have  $\sqrt{\frac{x}{y}} = \frac{24}{5} + \sqrt{\frac{y}{x}}$

$$\text{Let } \sqrt{\frac{x}{y}} = z$$

$$\therefore z = \frac{24}{5} + \frac{1}{z}$$

$$\Rightarrow z = \frac{24z + 5}{5z}$$

$$\Rightarrow 5z^2 - 24z - 5 = 0$$

$$\Rightarrow 5z^2 - 25z + z - 5 = 0$$

$$\Rightarrow 5z(z - 5) + 1(z - 5) = 0$$

$$\Rightarrow (z - 5)(5z + 1) = 0$$

$$\Rightarrow z = 5 \text{ or } -\frac{1}{5} \Rightarrow \sqrt{\frac{x}{y}} = 5 \text{ or } -\frac{1}{5}$$

$$\Rightarrow \sqrt{\frac{x}{y}} = 5 \left[ \because \sqrt{\frac{x}{y}} \neq -\frac{1}{5} \right]$$

$$\Rightarrow x = 25y \quad \dots \dots \dots \text{(i)}$$

Again we have  $x + y = 26$

$$\Rightarrow 25y + y = 26 \quad [\text{From Eqs (i)}]$$

$$\Rightarrow 26y = 26 \Rightarrow y = 1$$

$$\therefore x = 25$$

$$\therefore xy = 25 \times 1 = 25$$

12. (A) We have  $\alpha$  and  $\beta$  are the roots of the equation  $x^2 + px + q = 0$

$$\therefore \alpha + \beta = -p \text{ and } \alpha\beta = q$$

$$\text{Now } \alpha^2 + \beta^2 = (\alpha + \beta)^2 - 2\alpha\beta$$

$$= (-p)^2 - 2(q) = p^2 - 2q$$

13. (B) We have  $a^3 = 335 + b^3$

$$\Rightarrow a^3 - b^3 = 335 \quad \dots \dots \dots \text{(i)}$$

$$\text{and } a = 5 + b \Rightarrow a - b = 5 \quad \dots \dots \dots \text{(ii)}$$

$$\text{Now } (a - b)^3 = a^3 - b^3 - 3ab(a - b)$$

$$\Rightarrow (5)^3 = 335 - 3ab(5)$$

$\therefore$  From Eqs (i) and (ii)]

$$\Rightarrow 125 = 335 - 15ab \Rightarrow ab = 14$$

Again

$$(a + b)^2 = (a - b)^2 + 4ab$$

$$= (5)^2 + 4(14) = 25 + 56$$

$$(a + b)^2 = 81$$

$$\therefore a + b = 9$$

14. (C) We have

$$9^x \cdot 3^y = 2187 \Rightarrow (3^2)^x \cdot 3^y = 2187$$

$$\Rightarrow 3^{2x+y} = 3^7 \Rightarrow 2x + y = 7 \quad \dots \dots \dots \text{(i)}$$

Again

$$2^{3x} \cdot 2^{2y} - 4^{xy} = 0$$

$$\Rightarrow 2^{3x} \cdot 2^{2y} = 4^{xy}$$

$$\Rightarrow 2^{3x+2y} = (2^2)^{xy}$$

$$\Rightarrow 3x + 2y = 2xy \dots\dots\dots(ii)$$

From Eqs (i) and (ii)

$$3x + 2(7 - 2x) = 2x(7 - 2x)$$

$$\Rightarrow 3x + 14 - 4x = 14x - 4x^2$$

$$\Rightarrow 4x^2 - 15x + 14 = 0$$

$$\Rightarrow (x - 2)(4x - 7) = 0$$

$$\Rightarrow x = 2, \frac{7}{4}$$

$$\therefore y = 3, \frac{7}{2}$$

$$\therefore x + y = 5 \text{ or } \frac{21}{4}$$

15. (B) For the system of linear equations

$$a_1x + b_1y + c_1 = 0 \text{ and}$$

$$a_2x + b_2y + c_2 = 0$$

has unique solution

$$\frac{a_1}{a_2} \neq \frac{b_1}{b_2}$$

We have

$$kx + 3y + 1 = 0$$

$$2x + y + 3 = 0$$

For unique solution

$$\frac{k}{2} \neq \frac{3}{1} \Rightarrow k \neq 6$$

16. (C) Let the speed of B be x m/s. Then according to the question

$$\frac{96}{x} - \frac{100}{\left(\frac{5}{3}\right)} = 12$$

$$\Rightarrow \frac{96}{x} - 60 = 12 \Rightarrow \frac{96}{x} = 72$$

$$\Rightarrow x = \frac{4}{3}$$

$$\therefore \text{Speed of B is } \frac{4}{3} \text{ m/s}$$

17. (A) We have

$$5^{1+x} + 5^{1-x} = 26$$

$$\Rightarrow 5 \cdot 5^x + 5 \cdot 5^{-x} = 26$$

$$\Rightarrow 5 \cdot 5^x + \frac{5}{5^x} = 26$$

Let  $5^x = y$

$$\therefore 5y + \frac{5}{y} = 26 \Rightarrow 5y^2 - 26y + 5 = 0$$

$$\Rightarrow 5y^2 - 25y - y + 5 = 0$$

$$\Rightarrow 5y(y - 5) - 1(y - 5) = 0$$

$$\Rightarrow (y - 5)(5y - 1) = 0 \Rightarrow y = 5, \frac{1}{5}$$

$$\Rightarrow 5^x = 5 \text{ or } 5^{-1} \Rightarrow x = 1 \text{ or } -1$$

18. (A) We know that

$$a^3 + b^3 = (a + b)^3 - 3ab(a + b)$$

$$= (5)^3 - 3 \times 6 \times 5 = 125 - 90 = 35$$

19. (A) We have

$$x^3 + 8 = (x)^3 + (2)^3$$

$$= (x + 2)\{(x)^2 - (x)(2) + (2^2)\}$$

$$= (x + 2)(x^2 - 2x + 4)$$

$$x^2 + 5x + 6 = x^2 + 2x + 3x + 6$$

$$= x(x + 2) + 3(x + 2)$$

$$= (x + 2)(x + 3)$$

$$\text{and } x^3 + 4x^2 + 4x = x(x^2 + 4x + 4)$$

$$= x(x + 2)^2$$

$\therefore \text{LCM}$

$$= x(x + 2)^2(x + 3)(x^2 - 2x + 4)$$

$$20. (A) \sqrt[3]{\frac{12}{125}} = \sqrt[3]{\frac{4 \times 125 + 12}{125}}$$

$$= \sqrt[3]{\frac{500 + 12}{125}} = \sqrt[3]{\frac{512}{125}} = \sqrt[3]{\left(\frac{8}{5}\right)^3}$$

$$= \left[\left(\frac{8}{5}\right)^3\right]^{\frac{1}{3}} = \left(\frac{8}{5}\right)^{\frac{1}{3}} = \frac{8}{5} = 1\frac{3}{5}$$

21. (B) Let quadratic equation be

$$ax^2 + bx + c = 0$$

If  $\alpha$  and  $\beta$  are roots then,

$$\alpha + \beta = -\frac{b}{a} \text{ and } \alpha\beta = \frac{c}{a}$$

Since Aman made a mistake in writing down the constant term.

$$\therefore \alpha + \beta = 4 + 3 = 7$$

and Alok made a mistake in writing down the coefficient of  $x$ .

$$\therefore \alpha\beta = 3 \times 2 = 6$$

So equation will be

$$x^2 - (\alpha + \beta)x + \alpha\beta = 0$$

$$\Rightarrow x^2 - 7x + 6 = 0$$

$$\Rightarrow (x - 6)(x - 1) = 0$$

$$\Rightarrow x = 6, 1$$

22. (C) We have

$$2x + 4y = 6$$

$$\text{and } 4x + 8y = 8$$

$$a_1 = 2, b_1 = 4, c_1 = -6$$

$$\therefore a_2 = 4, b_2 = 8, c_2 = -8$$

$$\text{Now } \frac{a_1}{a_2} = \frac{2}{4} = \frac{1}{2}, \frac{b_1}{b_2} = \frac{4}{8} = \frac{1}{2}$$

$$\frac{c_1}{c_2} = \frac{-6}{-8} = \frac{3}{4}$$

$$\text{Since } \frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$$

$\therefore$  System of equation is inconsistent

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- 23.** (A) We have

$x^2 - 5x + \alpha$  and  $x^3 - 7x + 2\alpha$  have a common factor

Let

$$\begin{aligned} x^2 - 5x + \alpha &= (x-a)(x-b) = x^2 - (a+b)x + ab \\ \text{and } x^3 - 7x + 2\alpha &= (x-a)(x-c) \\ &= x^2 - (a+c)(x-c) \end{aligned}$$

By comparing we get

$$\begin{aligned} a+b &= 5, ab = \alpha \\ a+c &= 7, ac = 2\alpha \\ \Rightarrow ac &= 2(ab) \Rightarrow c = 2b \\ a+b &= 5, a+2b = 7 \end{aligned}$$

Solving these equation we get

$$\begin{aligned} a &= 3, b = 2 \\ \therefore \alpha &= ab = 3 \times 2 = 6 \end{aligned}$$

- 24.** (C) We have

$$\begin{aligned} x^3 + 4x^2 - 11x - 30 &= (x+2)(x-3)(x+5) \\ \therefore \text{Factor of } x^3 + 4x^2 - 11x - 30 &= (x+2)(x-3) \text{ and } (x+5) \end{aligned}$$

- 25.** (A) We have  $12x^2 + mx + 5 = 0$

Let  $\alpha, \beta$  are the roots of equations

$$\therefore \alpha + \beta = -\frac{m}{12} \text{ and } \alpha\beta = \frac{5}{12}$$

$$\text{given } \frac{\alpha}{\beta} = \frac{3}{2} \Rightarrow \alpha = \frac{3\beta}{2}$$

$$\therefore \left(\frac{3\beta}{2}\right)(\beta) = \frac{5}{12} \Rightarrow \beta^2 = \frac{10}{36}$$

$$\Rightarrow \beta = \frac{\sqrt{10}}{6} \text{ and } \alpha = \frac{3\sqrt{10}}{12}$$

$$\text{Hence } m = 12 \left( \frac{3\sqrt{10}}{12} + \frac{\sqrt{10}}{6} \right) = 12 \left( \frac{5\sqrt{10}}{12} \right)$$

$$\Rightarrow m = 5\sqrt{10}$$

- 26.** (B) We have

degree of  $f(x) = 3$

degree of  $g(x) = 4$

New degree of  $f(x) g(x) = \text{degree of } f(x) + \text{degree of } g(x) = 3 + 4 = 7$

- 27.** (D) We have

$$f(x) = 5x^2 + 5x^2 - 6x + 9$$

$$g(x) = x + 3 = 0$$

$$\Rightarrow x = -3$$

$$\begin{aligned} f(-3) &= 5(-3)^3 + 5(-3)^2 - 6(-3) + 9 \\ &= -135 + 45 + 18 + 9 = -63 \end{aligned}$$

Hence  $5x^3 + 5x^2 - 6x + 9$  is divided by  $(x+3)$  the remainder is  $-63$ .

- 28.** (D) We know that

Product of two number = LCM of two number  $\times$  H.C.F of two number

$$\therefore (x+y+z)p^3 = p^2 \times \text{L.C.M}$$

$$\text{L.C.M} = (x+y+z)p$$

- 29.** (C) We have

$$\begin{aligned} \therefore 8x^2 - y^3 &= (2x)^3 - (y)^3 \\ &= (2x-y)(4x^2 + 2xy + y^2) \end{aligned}$$

$8x^2 - y^3$  is divided by  $2xy + 4x^2 + y^2$  then quotient =  $2x - y$

- 30.** (A) We have

$x+2$  is factor of  $x^2 + ax + b$

$$\therefore (-2)^2 + (-2)a + b = 0$$

$$\Rightarrow b - 2a = -4 \quad \dots \text{(i)}$$

also  $(x+2)$  is factor of  $x^2 + bx + a$

$$\therefore (-2)^2 + 2b + a = 0$$

$$\Rightarrow a - 2b = -4 \quad \dots \text{(ii)}$$

solving (i) and (ii) we get

$$\therefore a = b = 4$$

$$\therefore a : b = 1$$

- 31.** (A) Consider  $ax - b = 0$

$$\Rightarrow x = \frac{b}{a}$$

Since  $f(x)$  is divided by  $ax - b$  therefore by remainder theorem remainder is given by

$$f\left(\frac{b}{a}\right).$$

- 32.** (B) Let  $f(x)$  be the product of given polynomials then

$$\begin{aligned} f(x) &= (x+2)(x-2) \\ &\quad (x^2 - 2x^2 + 4x - 8) \\ &\quad (x^3 + 2x^2 + 4x + 8) \\ &= (x^2 - 2^2) (x^2(x-2) + 4(x-2)) \\ &\quad (x^2(x+2)(x^2 + 4)) \\ &\quad ((x+2)(x^2 + 4)) \\ &= (x^2 - 4) (x^2 + 4)^2 (x^2 - 2^2) \\ &= (x^2 - 4) (x^2 + 4)^2 (x^2 - 4) \\ &= [(x^2 - 4) (x^2 + 4)]^2 \\ &= (x^2 - 4^2)^2 = (x^4 - 16)^2 \end{aligned}$$

- 33.** (C) Let

$$\begin{aligned} f(x) &= x(x+2)(x+3)(x+5) - 72 \\ &= x(x+2)[x^2 + 8x + 15] - 72 \\ &= x[x^3 + 8x^2 + 15x + 2x^2 + 16x + 30] - 72 \\ &= x(x^3 + 10x^2 + 31x + 30) - 72 \\ &= x^4 + 10x^3 + 31x^2 + 30x - 72 \end{aligned}$$

Clearly  $f(1) = 0$

Also  $f(-6) = 0$

$\therefore (x+6)$  is a factor of  $(x)$

Now to find other factors, let us divide  $f(x)$  by  $(x-1)(x+6)$  i.e., by

$$\begin{array}{r}
 \frac{x^2+5x+12}{x^2+5x-6} \\
 \underline{x^2+5x-6} \quad | x^3+10x^2+31x^2+30x-72 \\
 \quad x^4+5x^3-6x^2 \\
 \quad (-) (-) (+) \\
 \hline
 \quad 5x^3+37x^2+30x-72 \\
 \quad 5x^3+25x^2-30x \\
 \quad (-) (-) (+) \\
 \hline
 \quad 12x^2+60x-72 \\
 \quad 12x^2+60x-72 \\
 \quad (-) (-) (+) \\
 \hline
 \quad 0
 \end{array}$$

34. (B) Let  $h(x) = x^2 + x - 2$

$$\begin{aligned}
 &= x^2 + 2x - x - 2 \\
 &= x(x+2) - 1(x+2) = (x+2)(x-1) \\
 \text{Since } h(x) \text{ is the H.C.F of } f(x) \text{ and } g(x) \\
 \therefore h(x) \text{ completely divides both } f(x) \text{ and } (x-1) \text{ is a factor of } g(x) \\
 \Rightarrow f(-2) = 0 \text{ and } g(1) = 0 \\
 \Rightarrow (-3)(4-6+a) = 0 \\
 \text{and } 3(1+2+b) = 0 \\
 \Rightarrow (a-2) = 0 \text{ and } b+3 = 0 \\
 \Rightarrow a = 2 \text{ and } b = -3
 \end{aligned}$$

35. (C) Given equation is

$$\begin{aligned}
 a(b-c)x^2 + b(c-a)x + c(a-b) &= 0 \\
 \text{Since it has equal roots therefore } D &= 0 \\
 \Rightarrow B^2 - 4AC &= 0 \\
 \Rightarrow (b(c-a))^2 - 4a(b-c)(a-b) &= 0 \\
 \Rightarrow (b(c-a))^2 - 4a(b-c)(a-b) &= 0 \\
 \Rightarrow b^2(c^2 + a^2 - 2ac) &= 0 \\
 4ac(ab - b^2 - ac + bc) &= 0 \\
 \Rightarrow b^2c^2 + b^2a^2 - 2acb^2 - 4a^2bc &+ 4acb^2 + 4a^2c^2 - 4abc^2 = 0 \\
 \Rightarrow (bc)^2 + (ab)^2 + (-2ac)^2 - 2acb^2 &- 4a^2bc - 4abc^2 = 0 \\
 \Rightarrow (bc + ab - 2ac)^2 &= 0 \\
 \Rightarrow bc + ab &= 2ac \\
 \Rightarrow b(a+c) &= 2ac \Rightarrow \frac{1}{a} + \frac{1}{c} = \frac{2}{b}
 \end{aligned}$$

36. (A) Given equation is

$$\begin{aligned}
 \frac{a-x^2}{bx} - \frac{b-x}{c} &= \frac{c-x}{b} - \frac{b-x^2}{cx} \\
 \Rightarrow \frac{a-x^2}{bx} + \frac{b-x^2}{cx} &= \frac{c-x}{b} + \frac{b-x}{c} \\
 \Rightarrow \frac{ac-cx^2+b^2-bx^2}{bcx} &
 \end{aligned}$$

$$\begin{aligned}
 &\Rightarrow \frac{c^2 - cx + b^2 - bx}{bc} \\
 &\Rightarrow \frac{(b^2 + ac) - x^2(b + c)}{bcx} \\
 &\Rightarrow \frac{(b^2 + c^2) - x(b + c)}{bc} \\
 \Rightarrow (b^2 + ac) - x^2(b + c) &= x(b^2 + c^2) - x^2(b + c) \\
 \Rightarrow b^2 + ac &= x(b^2 + c^2) \\
 \Rightarrow x &= \frac{b^2 + ac}{b^2 + c^2}
 \end{aligned}$$

37. (C) Given equation is

$$\begin{aligned}
 x^2 + 7x - 14 \left( k^2 - \frac{7}{8} \right) &= 0 \\
 \Rightarrow x = \sqrt{\frac{-7 \pm 49 + 4(14)\left( k^2 - \frac{7}{8} \right)}{2}} & \\
 \Rightarrow x = \frac{-7 \pm \sqrt{49 + 56k^2 - 49}}{2} & \\
 \Rightarrow x = \frac{-7 \pm \sqrt{56k^2}}{2} & \\
 \Rightarrow x = \frac{-7 \pm 2\sqrt{14k}}{2} &
 \end{aligned}$$

Clearly x can't take any integral value, for any integer k.

- $\therefore$  The given equation has no integral root.  
38. (D) Given system of equations can be re-written as

$$\frac{6}{v} + \frac{3}{u} = 7 \dots \dots \dots \text{(i)}$$

$$\frac{3}{v} + \frac{9}{u} = 11 \dots \dots \dots \text{(ii)}$$

Now let  $\frac{1}{u} = x$  and  $\frac{1}{v} = y$  then above system of equations become

$$3x + 6y = 7 \dots \dots \dots \text{(iii)}$$

$$\text{and } 9x + 3y = 11 \dots \dots \dots \text{(iv)}$$

On multiplying Eq (iii) by 3 and then subtracting eq (iv) from it we get

$$9x + 18 = 21$$

$$9x + 3y = 11$$

$$\underline{\underline{- \quad - \quad -}}$$

$$15y = 10$$

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$$\Rightarrow y = \frac{2}{3}$$

On putting  $y = \frac{2}{3}$  in eq (iv) we get

$$9x + 2 = 11 \Rightarrow x = 1$$

$$\Rightarrow \frac{1}{u} = 1 \quad \left[ \because \frac{1}{u} = x \right]$$

$$\Rightarrow u = 1$$

39. (B) Let the present age of Shyam be  $x$  years and age of Ram be  $y$  years. Then according to question

$$(y - 5) = 3(x - 5) \text{ and } (y + 4) = 2(x + 4)$$

$$\Rightarrow 3x - y = 10 \quad \dots \text{(i)}$$

$$\text{and } 2x - y = -4 \quad \dots \text{(ii)}$$

On subtracting Eq (i) from Eq (ii) we get

$$28 - y = -4 \Rightarrow y = 32$$

Thus present age of Ram is 32 years

40. (C) We have  $ab + bc + ca = 0$

$$\Rightarrow ab + ca = -bc \Rightarrow a = \frac{-bc}{b+c}$$

$$\Rightarrow a^2 = \frac{b^2c^2}{(b+c)^2}$$

Now consider

$$\begin{aligned} & \frac{a^2}{a^2 - bc} + \frac{b^2}{b^2 - ca} + \frac{c^2}{c^2 - ab} \\ &= \frac{\frac{b^2c^2}{(b+c)^2}}{\frac{b^2c^2}{(b+c)^2} - bc} + \frac{b^2}{b^2 - c\left(\frac{-bc}{b+c}\right)} + \frac{c^2}{c^2 - b\left(\frac{-bc}{b+c}\right)} \\ &= \frac{bc}{-(b^2 + c^2 + bc)} + \frac{b(b+c)}{b^2 + bc + c^2} + \frac{c(b+c)}{b^2 + c^2 + bc} \\ &= \frac{-bc + b^2 + bc + c^2 + bc}{b^2 + c^2 + bc} \\ &= \frac{b^2 + bc + c^2}{b^2 + c^2 + bc} = 1 \end{aligned}$$

41. (B) We know that if  $a + b + c = 0$  then

$$a^3 + b^3 + c^3 = 3abc$$

$$\text{Here } (x - y) + (y - z) + (z - x) = 0$$

$$\therefore (x - y)^3 + (y - z)^3 + (z - x)^3 = 3xyz$$

$$= 3(x - y)(y - z)(z - x) \quad \dots \text{(i)}$$

Now consider

$$\frac{(x - y)(y - z)(z - x)}{(x - y)^3 + (y - z)^3 + (z - x)^3}$$

$$= \frac{(x - y)(y - z)(z - x)}{3(x - y)(y - z)(z - x)} \text{ Using (i)} = \frac{1}{3}$$

**CDS [2016-II]**

1. What is the solution of

$$\log_{10} \left[ 1 - \left\{ 1 - (1-x^2)^{-1} \right\}^{-1} \right]^{\frac{1}{2}} = 1 ?$$

$$\log_{10} \left[ 1 - \left\{ 1 - (1-x^2)^{-1} \right\}^{-1} \right]^{\frac{1}{2}} = 1 \text{ का हल क्या हैं?}$$

- (A)  $x = 100$       (B)  $x = 10$   
 (C)  $x = 1$       (D)  $x = 0$

2. If  $\lambda$  is an integer and  $\alpha, \beta$  are the roots of  $4x^2 -$

$$16x + \frac{\lambda}{4} = 0 \text{ such that } 1 < \alpha < 2 \text{ and } 2 < \beta < 3$$

then how many values can  $\lambda$  take?

यदि  $\lambda$  एक पूर्णांक हैं और  $\alpha, \beta$  समीकरण  $4x^2 - 16x + \frac{\lambda}{4} = 0$  के

मूल इस प्रकार हैं कि  $1 < \alpha < 2$  और  $2 < \beta < 3$  हैं, तो  $\lambda$  के कितने मान हो सकते हैं?

- (A) 3      (B) 9  
 (C) 14      (D) 15

3. What is  $\frac{6^2 + 7^2 + 8^2 + 9^2 + 10^2}{\sqrt{7+4\sqrt{3}} - \sqrt{4+2\sqrt{3}}}$  equal to?

$$\frac{6^2 + 7^2 + 8^2 + 9^2 + 10^2}{\sqrt{7+4\sqrt{3}} - \sqrt{4+2\sqrt{3}}} \text{ किसके बराबर हैं?}$$

- (A) 330      (B) 340  
 (C) 355      (D) 366

4. If  $x^2 = y + z$ ,  $y^2 = z + x$  and  $z^2 = x + y$  then what is

$$\text{the value of } \frac{1}{x+1} + \frac{1}{y+1} + \frac{1}{z+1} ?$$

यदि  $x^2 = y + z$ ,  $y^2 = z + x$  और  $z^2 = x + y$  हैं, तो

$$\frac{1}{x+1} + \frac{1}{y+1} + \frac{1}{z+1} \text{ का मान क्या है?}$$

- (A) -1      (B) 1  
 (C) 2      (D) 4

5. What would be the maximum value of Q in the equation  $5P9 + 4R7 + 2Q8 = 1114$ ?

समीकरण  $5P9 + 4R7 + 2Q8 = 1114$  में Q का अधिकतम मान क्या होगा?

- (A) 9      (B) 8  
 (C) 5      (D) 4

6. If  $\alpha$  and  $\beta$  are the two zeros of the polynomial  $25x^2 - 16x + 2$ , then what is a quadratic polynomial whose zeros are  $(2\alpha)^{-1}$  and  $(2\beta)^{-1}$ ?

यदि बहुपद  $25x^2 - 16x + 2$  के बहुपद दो शून्यक  $\alpha$  और  $\beta$  हैं, तो वह दिखात बहुपद क्या होगा जिसके शून्यक  $(2\alpha)^{-1}$  और  $(2\beta)^{-1}$  हैं?

- (A)  $x^2 + 30x + 2$       (B)  $8x^2 - 30x + 25$   
 (C)  $8x^2 - 30x$       (D)  $x^2 + 30x$

7. If  $2p + 3q = 12$  and  $4p^2 + 4pq - 3q^2 = 126$  then what is the value of  $p + 2q$ ?

यदि  $2p + 3q = 12$  और  $4p^2 + 4pq - 3q^2 = 126$  है तो  $p + 2q$  का मान क्या है?

- (A) 5      (B)  $\frac{21}{4}$       (C)  $\frac{25}{4}$       (D)  $\frac{99}{16}$

8. The sides of a triangle are given by  $\sqrt{a^2 + b^2}$ ,  $\sqrt{c^2 + a^2}$  and  $(b + c)$  where  $a, b, c$  are positive. What is the area of the triangle equal to?

किसी त्रिभुज की भुजाओं को  $\sqrt{a^2 + b^2}$ ,  $\sqrt{c^2 + a^2}$  और  $(b + c)$  द्वारा व्यक्त किया गया हैं, जहाँ  $a, b, c$  धनात्मक हैं। त्रिभुज का क्षेत्रफल किसके बराबर है?

$$(A) \frac{\sqrt{a^2 + b^2 + c^2}}{2}$$

$$(B) \frac{\sqrt{a^2b^2 + b^2c^2 + c^2a^2}}{2}$$

$$(C) \frac{a(b+c)}{2}$$

$$(D) \frac{\sqrt{3(a^2b^2 + b^2c^2 + c^2a^2)}}{2}$$

**Solution**

1. (A) As

$$\log_{10} \left[ 1 - \left\{ 1 - (1-x^2)^{-1} \right\}^{-1} \right]^{\frac{1}{2}}$$

$$= \log_{10} \left[ \frac{1}{1 - (1-x^2)^{-1}} \right]^{\frac{1}{2}} = \log_{10} \left| \frac{1}{1 - \left( \frac{x^2}{1+x^2} \right)} \right|^{\frac{1}{2}}$$

$$= \log_{10} \left[ \frac{1}{x^2} \right]^{\frac{1}{2}} = \log_{10} \left[ \frac{1}{x^2} \right]^{\frac{1}{2}} = \log_{10} \frac{1}{x}$$

According to question

$$\log_{10} \frac{1}{x} = 1$$

Hence option = 10

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2. (D) As,  $4x^2 - 16x + \frac{\lambda}{4} = 0$

$$\Rightarrow x^2 - 4x + \frac{\lambda}{16} = 0$$

Sum of roots ( $\alpha + \beta$ ) = 4

$$\text{Product of roots } (\alpha\beta) = \frac{\lambda}{16}$$

As  $1 < \alpha < 2$  ..... (i)

$2 < \beta < 3$  ..... (ii)

From (i) and (ii)

$2 < \alpha\beta < 6$

$1 < \alpha\beta < 3$  [It is not possible because  $\alpha + \beta = 4$ ]

So  $1 \times 3 < \alpha\beta < 2 \times 2$

$3 < \alpha\beta < 4$

$\Rightarrow 3 < \alpha\beta < 4$

$$\Rightarrow 3 < \frac{\lambda}{16} < 4$$

Hence total value of would be 15.

Hence option (D)

3. (A)  $\frac{6^2 + 7^2 + 8^2 + 9^2 + 10^2}{\sqrt{7+4\sqrt{3}} - \sqrt{4+2\sqrt{3}}}$

$$= \frac{36 + 49 + 64 + 81 + 100}{\sqrt{4+3+4\sqrt{3}} + \sqrt{1+3+2\sqrt{3}}}$$

$$= \frac{330}{\sqrt{2^2 + (\sqrt{3})^2 + 2 \times 2 \times \sqrt{3}} - \sqrt{1^2 + (\sqrt{3})^2 + 2 \times 1 \times \sqrt{3}}}$$

$$= \frac{330}{\sqrt{(2+\sqrt{3})^2} - \sqrt{(1+\sqrt{3})^2}} = \frac{330}{2+\sqrt{3}-1-\sqrt{3}}$$

$$= \frac{330}{1} = 330$$

Hence option (A)

4. (B) As  $x^2 = y + z$

Then  $x^2 + x = x + y + z$

$$\Rightarrow x(1+x) = x + y + z$$

$$\Rightarrow \frac{1}{1+x} = \frac{x}{x+y+z}$$

Similarly

$$\frac{1}{1+y} = \frac{y}{x+y+z}$$

$$\frac{1}{1+z} = \frac{z}{x+y+z}$$

So

$$\begin{aligned} & \frac{1}{x+1} + \frac{1}{y+1} + \frac{1}{z+1} \\ &= \frac{x}{x+y+z} + \frac{y}{x+y+z} + \frac{z}{x+y+z} \\ &= \frac{x+y+z}{x+y+z} = 1 \end{aligned}$$

Hence option (B)

5. (A) As

$$5P9 + 3R7 + 2Q8 = 1114 \quad \text{(i)}$$

According to concept of addition

$$9 + 7 + 8 = 24 \quad \text{(ii)}$$

$$5 + 3 + 2 = 10 \quad \text{(iii)}$$

From (i), (ii) and (iii)

We can simply say that

$$2 + P + R + Q = 11 \quad \text{(iv)}$$

Q would be maximum when P and R will be minimum.

So

$$P = R = 0$$

From (iv)

$$2 + 0 + 0 + Q = 11$$

$$\Rightarrow Q = 11 - 2$$

$$\Rightarrow Q = 9$$

Hence option (A)

6. (B) As  $25x^2 - 15x + 2 = 0$  ..... (i)

$$\text{If } \alpha + \beta = -\frac{(-15)}{25} = \frac{3}{5}$$

$$\alpha\beta = \frac{2}{25}$$

If  $(2\alpha)^{-1}$  and  $(2\beta)^{-1}$  would be roots then

$$\text{Sum of roots} = \frac{1}{2\alpha} \times \frac{1}{2\beta}$$

$$= \frac{\alpha + \beta}{2\alpha\beta} = \frac{\frac{3}{5}}{2 \times \frac{2}{25}} = \frac{3}{5} \times \frac{25}{4} = \frac{15}{4}$$

$$\text{Product of roots} = \frac{1}{2\alpha} \times \frac{1}{2\beta}$$

$$= \frac{1}{4\alpha\beta} = \frac{1 \times 25}{4 \times 2} = \frac{25}{8}$$

Quadratic equation be

$$x^2 - (\text{Sum of roots})x + \text{Product of roots} = 0$$

$$\Rightarrow x^2 - \frac{15}{4}x + \frac{25}{8} = 0$$

Hence quadratic polynomial be

$$8x^2 - 30x + 25$$

Hence option (B)

7. (D)  $2p + 3q = 12$  ..... (i)

$$\text{And } 4p^2 + 4pq - 3q^2 = 126$$

$$\Rightarrow (2p)^2 + 2 \times 2p \times q + q^2 - 4q^2 = 126$$

$$\Rightarrow (2p+q)^2 - (2q)^2 = 126$$

$$\Rightarrow (2p + q + 2q)(2p + q - 2q) = 126$$

$$\Rightarrow 12 \times (2p - q) = 126 \quad \text{[From (i)]}$$

From (i) and (ii)

$$4p = 12 - \frac{21}{2} = \frac{3}{2}$$

$$\Rightarrow q = \frac{3}{8}$$

Putting the value of q in (i)

$$2p = 12 - 3q = 12 - 3 \times \frac{3}{8}$$

$$\Rightarrow 2p = \frac{96 - 9}{8} = \frac{87}{8}$$

$$\Rightarrow p = \frac{87}{16}$$

Now

$$p + 2q = \frac{87}{16} + 2 \times \frac{3}{8}$$

$$= \frac{87+12}{16} = \frac{99}{16}$$

Hence option (D)

8. (C)